

Quantum dot spin qubits I: basic concepts

(Slide courtesy : 윤종인, 장원진)

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Outline

Lecture 1. Basics

- Background *Semiconductor quantum dot quantum computing*
- Approach *Basic concepts, experimental details*
- Single spin qubits *1Q, 2Q gates*
- Singlet-Triplet qubits *1Q, 2Q gates*

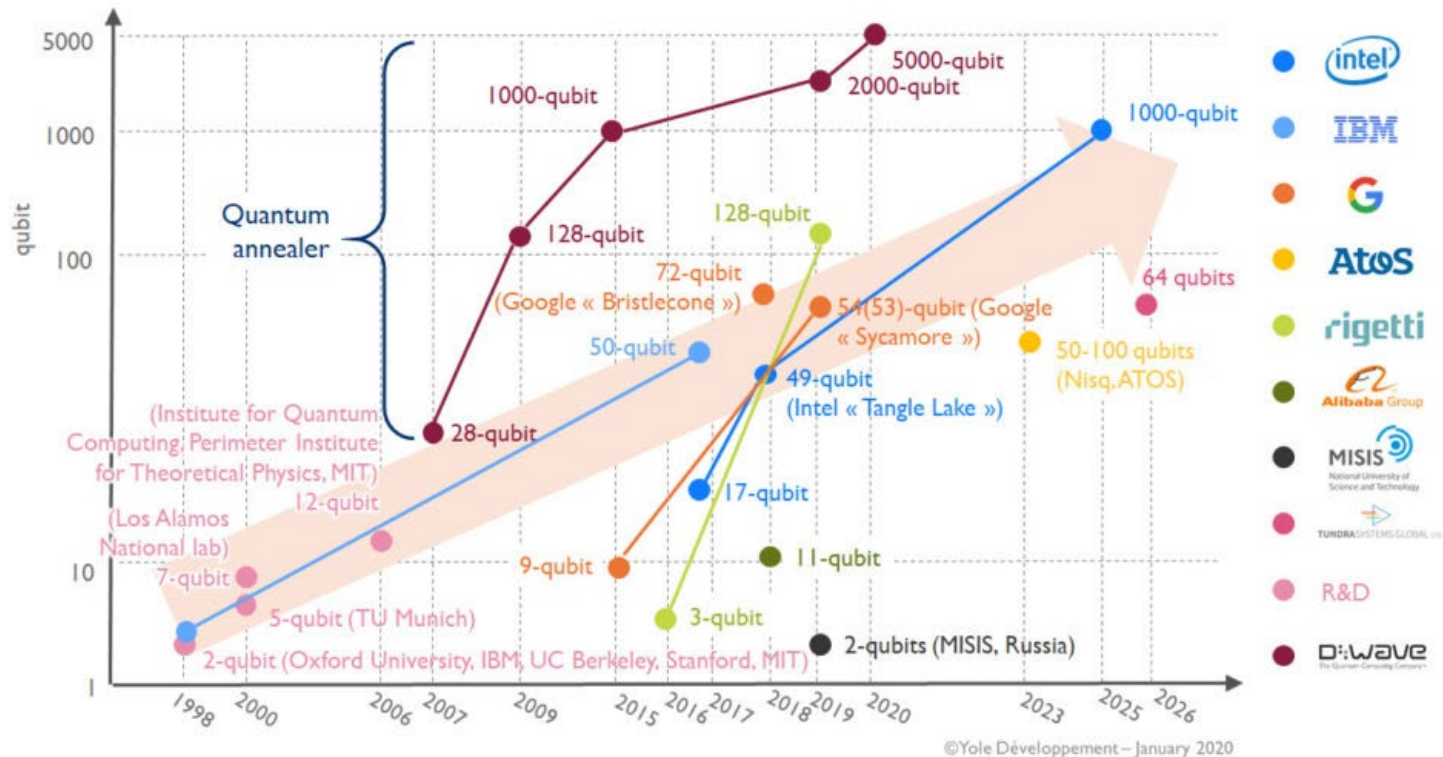
Lecture 2. More than two qubits

- Three, Four, Six qubit operations *Recent achievements*
- Coherent spin shuttling *Linking distant qubits*
- Scaling issue *Hot qubits, integration issue...*

양자컴퓨터 하드웨어 현황과 로드맵

Physical qubit roadmap for quantum computer

(Source: Quantum Technologies 2020 report, Yole Développement)



See also: 주요 하드웨어 개발기관의 로드맵: <https://research.ibm.com/blog/ibm-quantum-roadmap>,

<https://ionq.com/posts/december-09-2020-scaling-quantum-computer-roadmap>, <https://www.eetimes.eu/cea-leti-details-silicon-based-quantum-computing-roadmap/> 등

Quantum mechanical phase coherence



Superposition

N개 집합

$$|\Psi\rangle = \frac{1}{\sqrt{2}} (|0\rangle + |1\rangle)$$



Statistical Mixture

N개 집합

50% 는 $|0\rangle$

50% 는 $|1\rangle$

- 다른 점을 한단어로 ? *'coherence'*: 간섭현상을 보일 수 있는 능력
- 어떻게 구별 ?

Distinguishing superposition vs mixture

Repeated Stern-Gerlach experiment

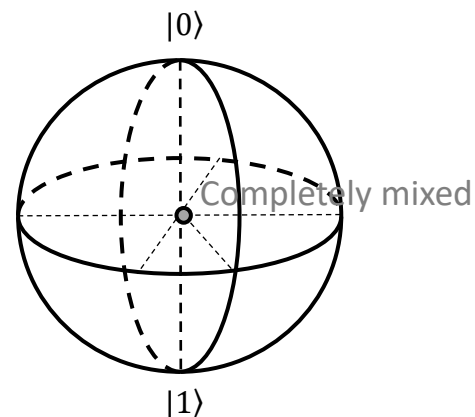
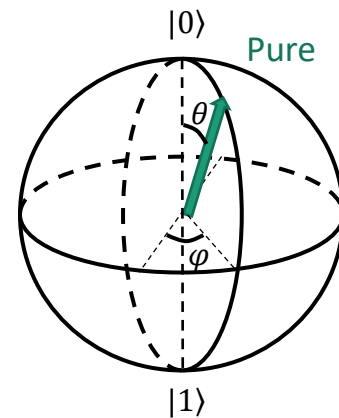
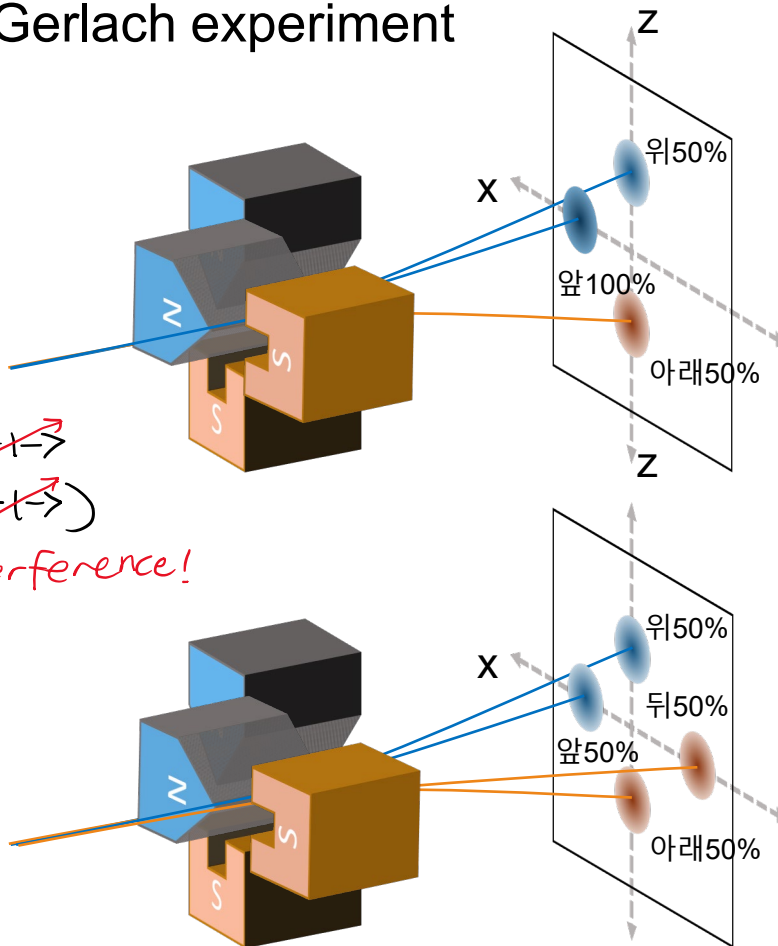
$$|\Psi\rangle = \frac{1}{\sqrt{2}}(|0\rangle + |1\rangle)$$

$$\propto (|+\rangle + |-\rangle)$$

$$(|+\rangle - |-\rangle)$$

interference!

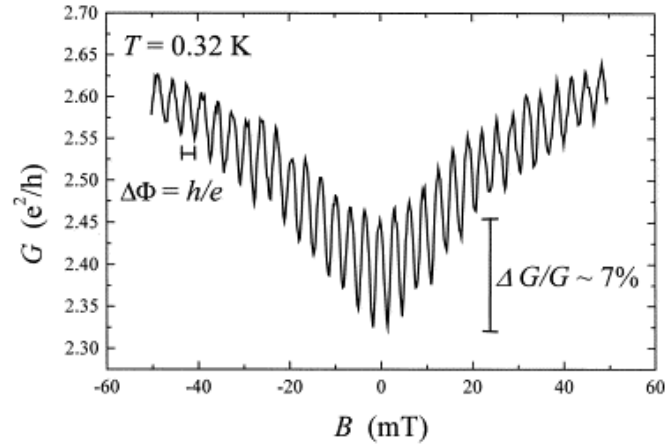
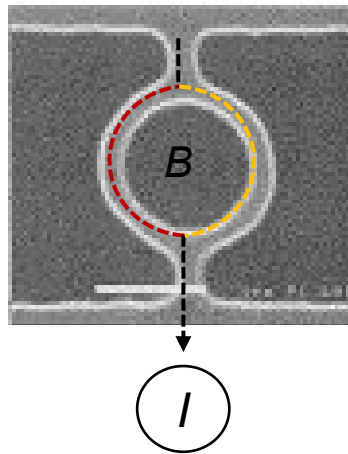
50% 는 $|0\rangle$
50% 는 $|1\rangle$



- 어떻게 구별? **토모그래피: 모든 Measurement basis 에 대해 projection 해본다.**
- Projective reconstruction – interference 는 어디에?**

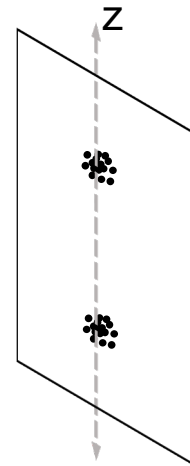
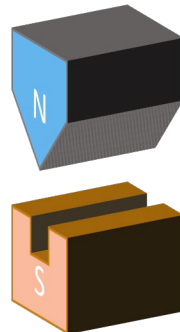
What is *single-shot* measurement ?

What is *NOT* single-shot experiment...



Really what QM textbook describes...

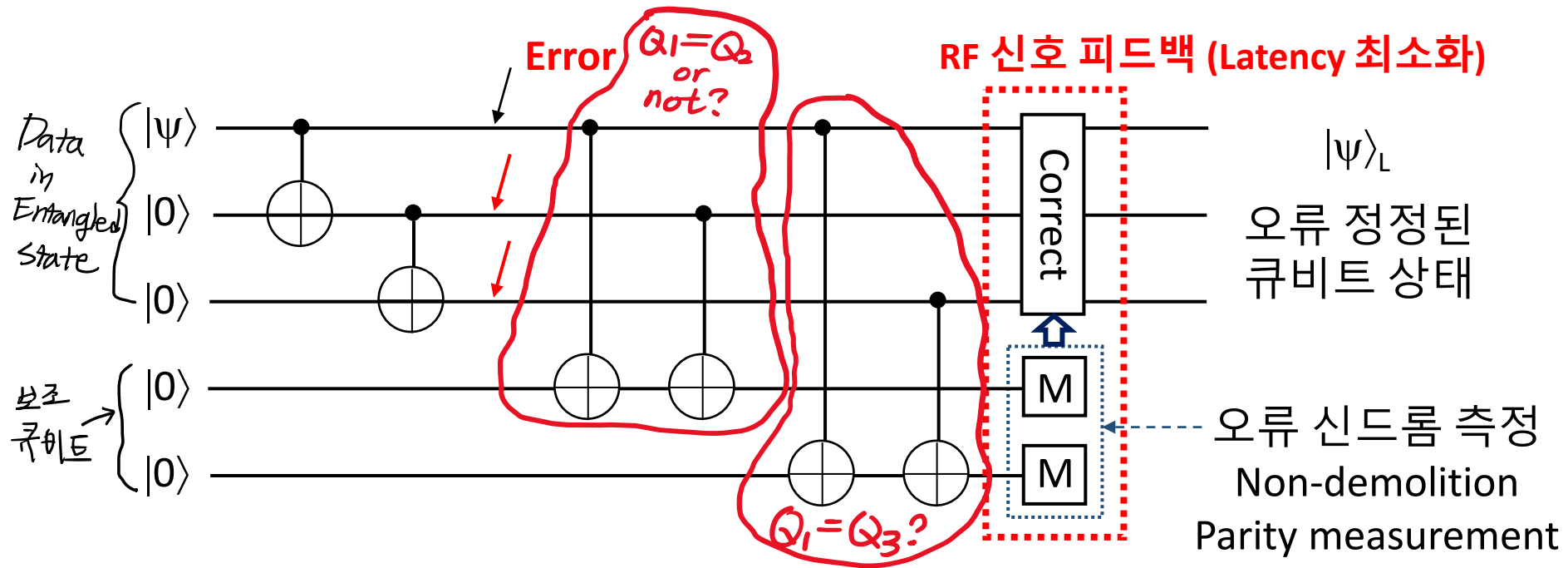
$$P_1 = \#state\ up / N_{total}$$



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Why *single-shot* is important ?

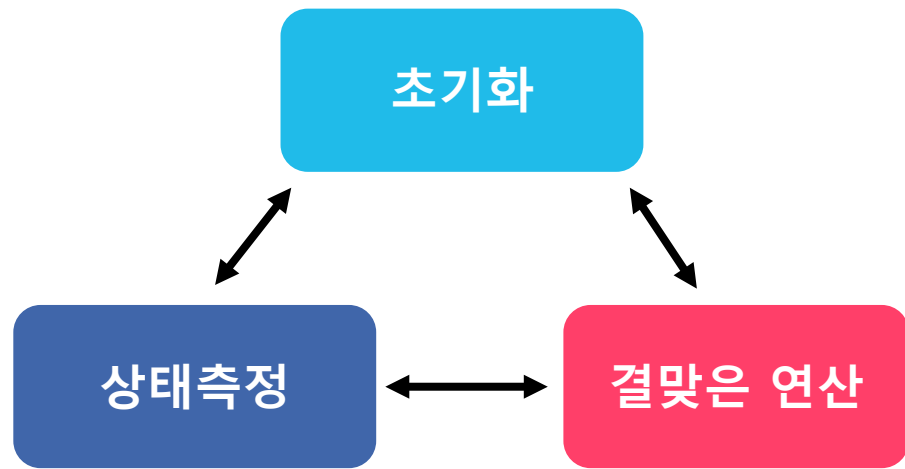
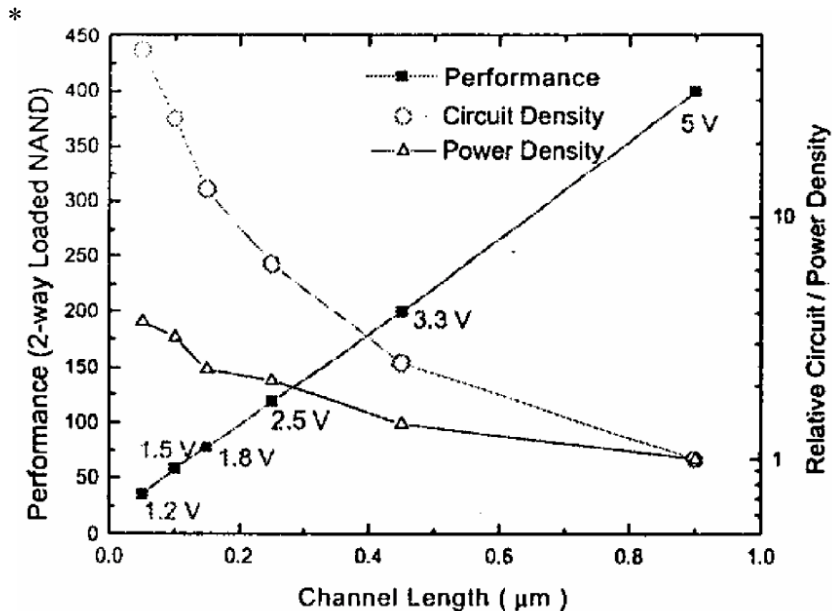
- Ex. Quantum error correction
- 보조 큐비트의 오류 신드롬 측정 후 **고속 피드백으로 실시간 오류 정정 (Single-shot !)**



1

Challenges

양자컴퓨터: 왜 만들기 어렵나?



고전 디지털 컴퓨터

(최근까지는) 트랜지스터를 30% 작게 만들면,

- 43% 동작속도 향상
 - 2x 집적도 향상
 - 30% 누설전류 감소
 - 65% 소모전력 감소
- 작게: 어렵지만..
“일석다조”

양자 컴퓨터

- So far : 극한환경 (극저온 and/or 초고진공)
- (원리적으로) 상충되는 목표,
- 상호작용 증가: 동작속도 향상, but 결맞음 감소
- 강한 상태 측정: SNR 증가, but backaction
- 다중큐비트: crosstalk

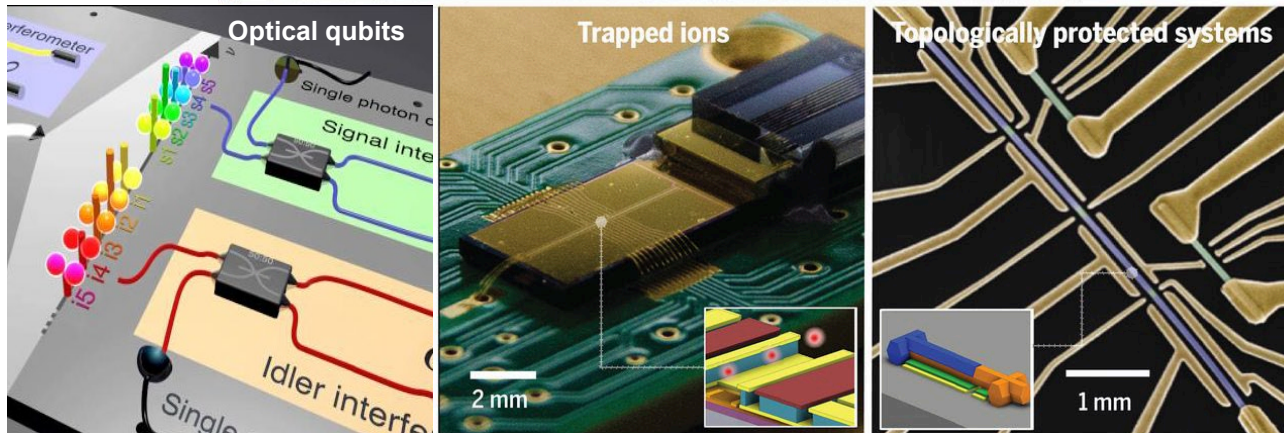
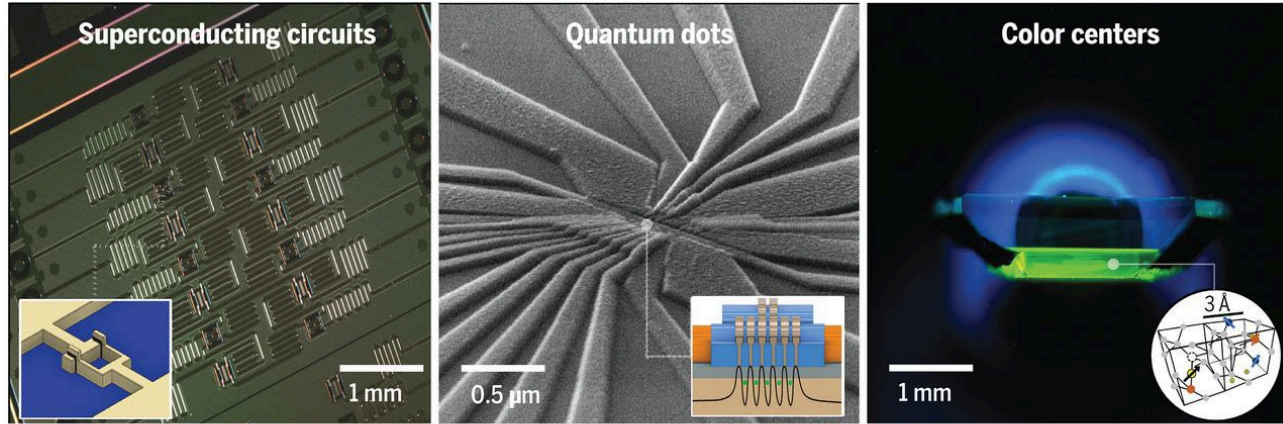
* G. G. Shahidi, “Challenges of CMOS scaling at below 0.1μm,” The 12th International Conference on Microelectronics (2000)

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Background

다양한 양자컴퓨팅 플랫폼

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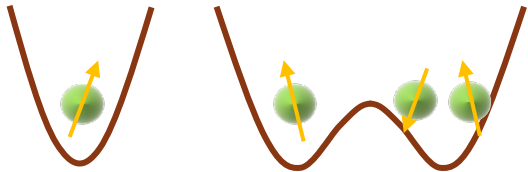


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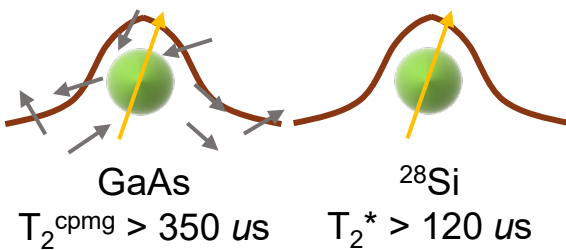
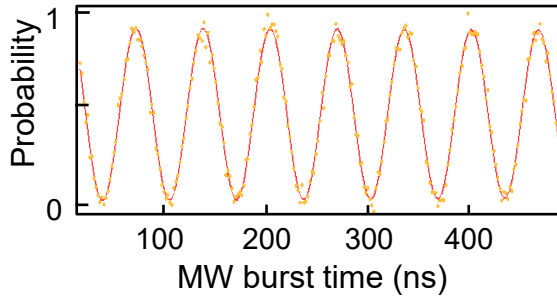
Background

Why semiconductor QDQC?

Coherence



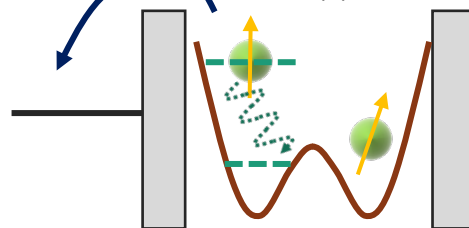
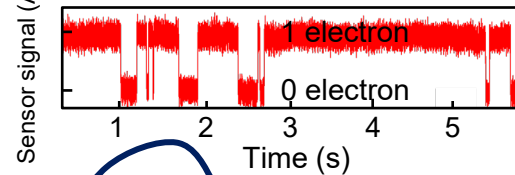
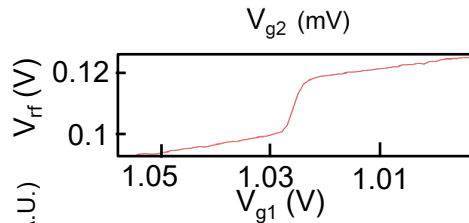
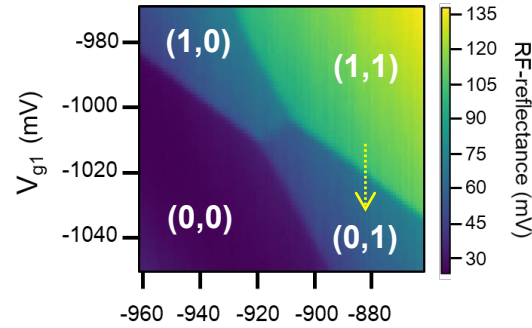
Long-lived spins in semiconductors
 Canonical 2-level system
 Small leakage errors



Nuclear bath spin polarization in GaAs

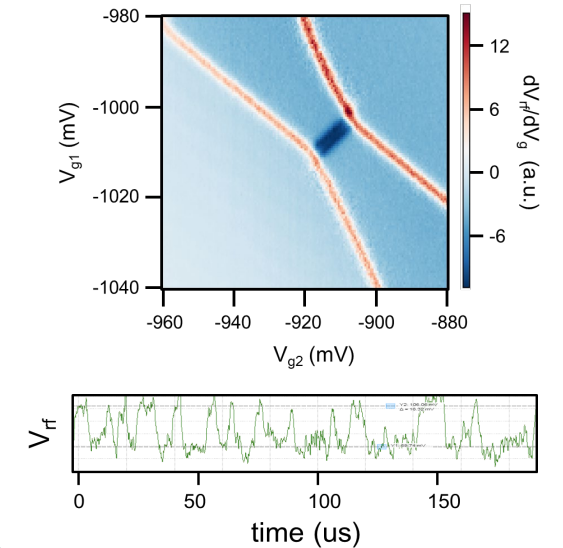
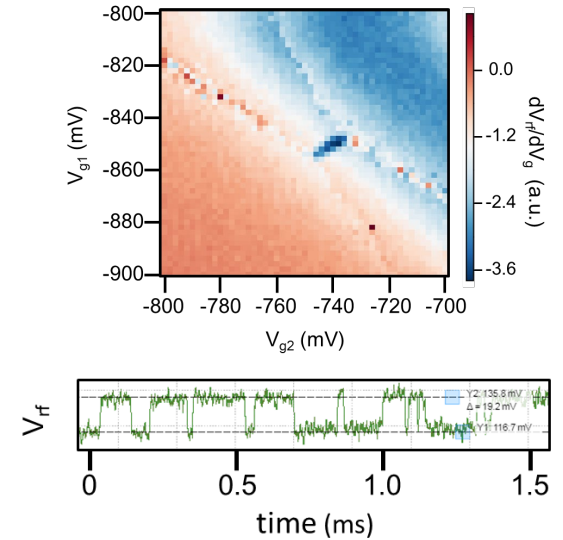
Small spin-orbit coupling & Small hyperfine interaction in purified ^{28}Si

Measurement



Long T_1 time \rightarrow Single-shot measurement straightforward

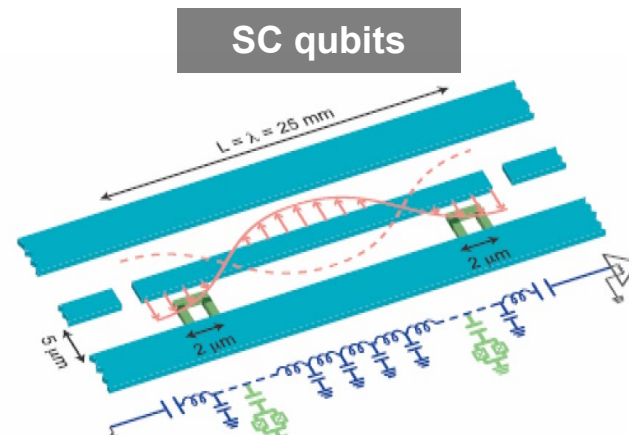
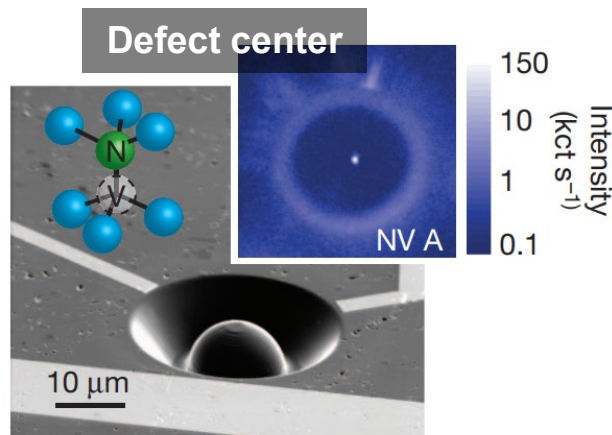
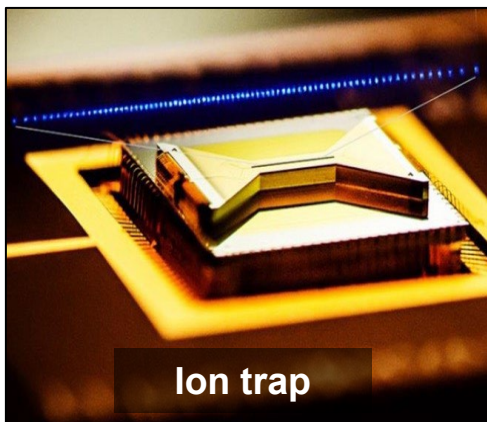
Tunability



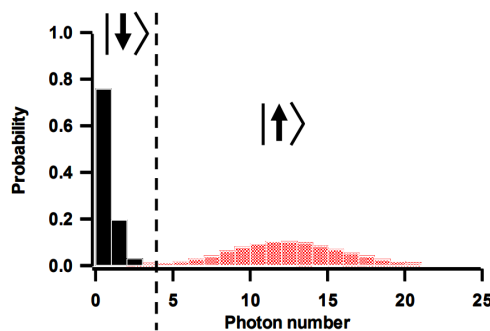
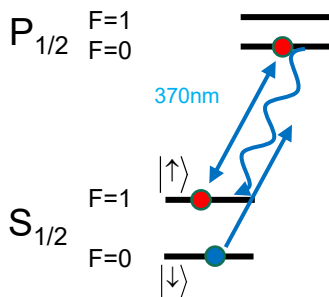
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Approach : detailed description of experiments

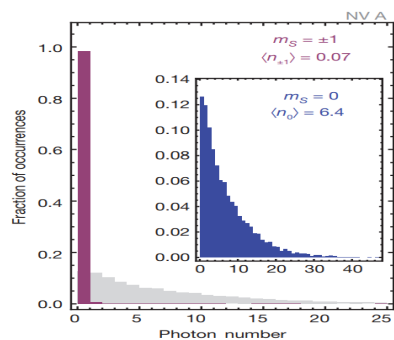
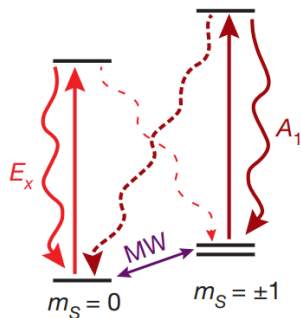
Single-shot measurements in physical systems



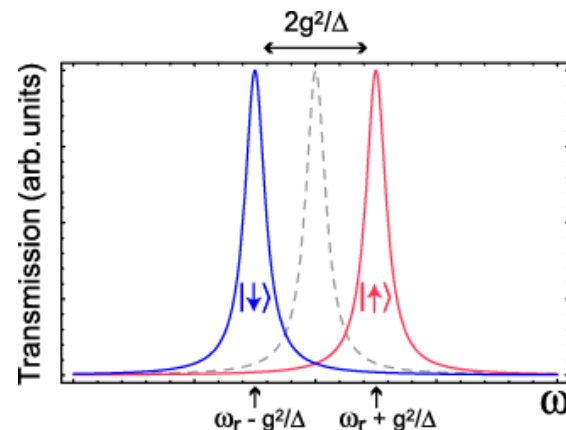
¹⁷¹Yb⁺



Nitrogen-Vacancy color center



Dispersive readout



SNR > 1 in a few us integration time

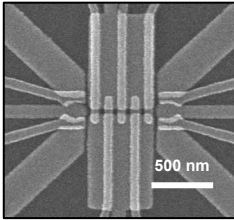
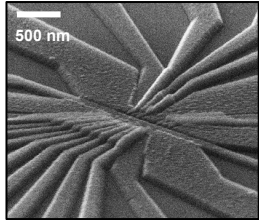
K.Kim group, (Tsinghua univ.)
M.Lee group (POSTECH ERC)
R.Hanson group, (quTech)
IBM, Google.. Etc.

2

Approach : detailed description of experiments

The semiconductor quantum chip

Si QD, Eriksson group, UW



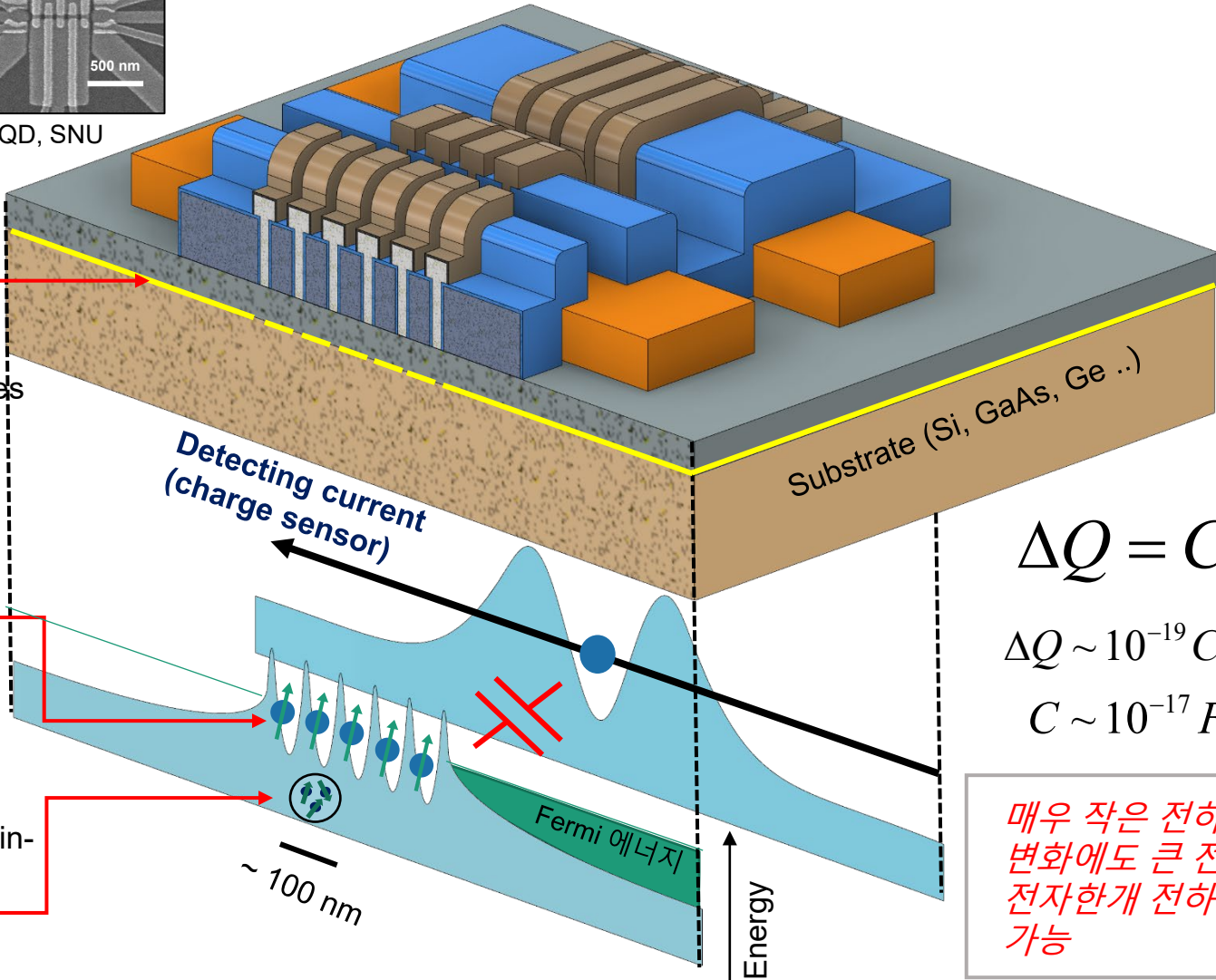
Si QD, SNU

Free Electrons

- Blue: Confinement gates
- Brown: Barrier gates
- Orange: Screening gates

Spin qubit array

Noise sources
(nuclear spins, spin-orbit coupling..)



$$\Delta Q = C \Delta V$$

$$\Delta Q \sim 10^{-19} \text{ Coulomb}$$

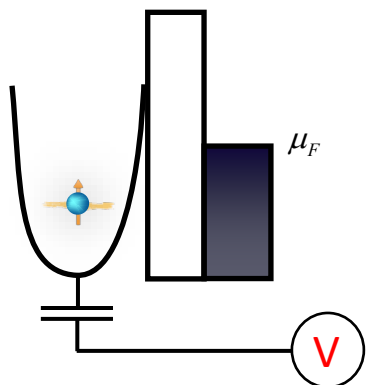
$$C \sim 10^{-17} \text{ Farad}$$

매우 작은 전하량
변화에도 큰 전압변화
전자한개 전하량 측정
가능

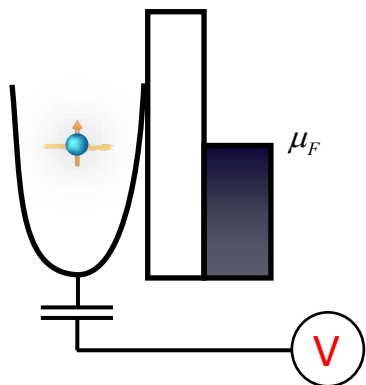
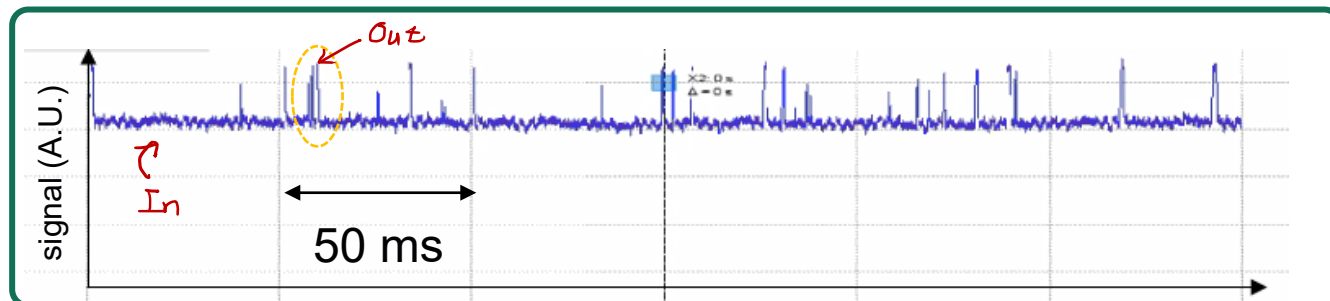
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Approach : detailed description of experiments

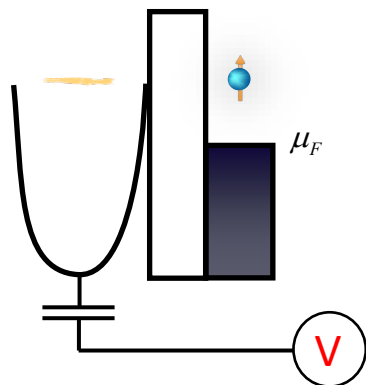
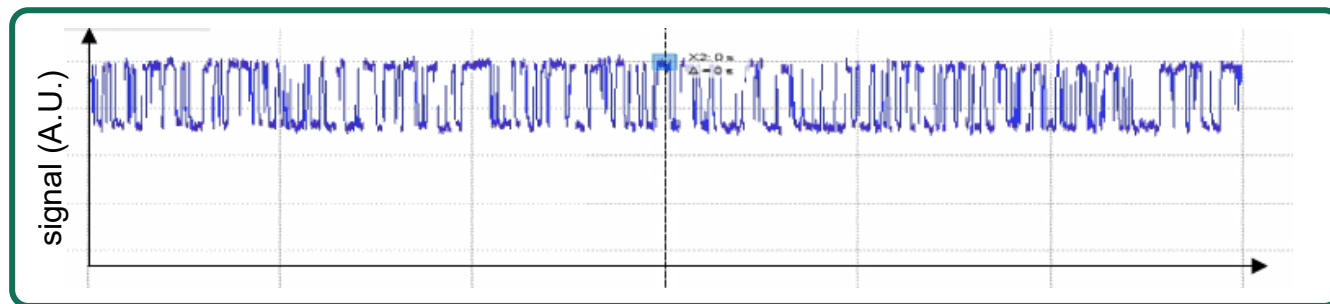
Typical example : watching electron tunneling



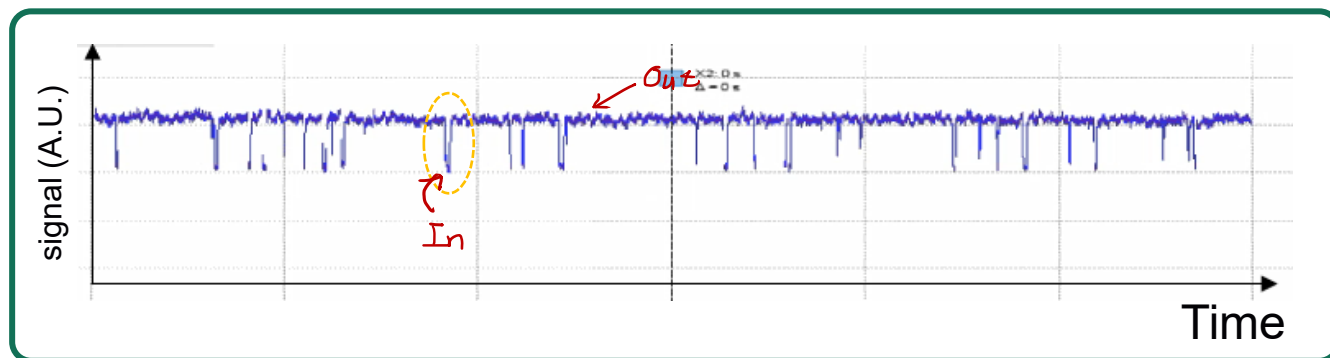
Mostly occupied



Half the time occupied, half the time empty



Mostly empty

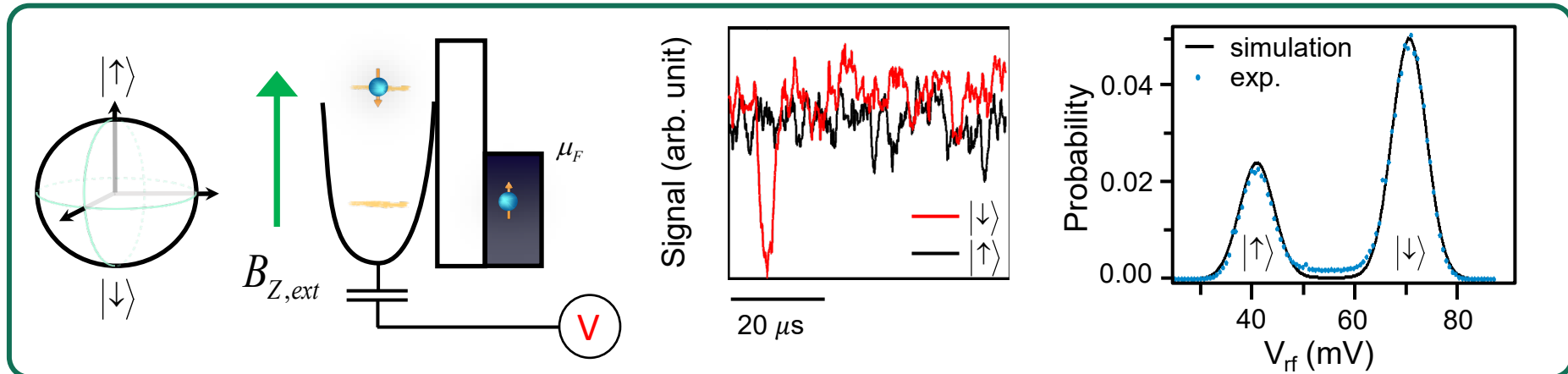


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Fast single-shot measurements

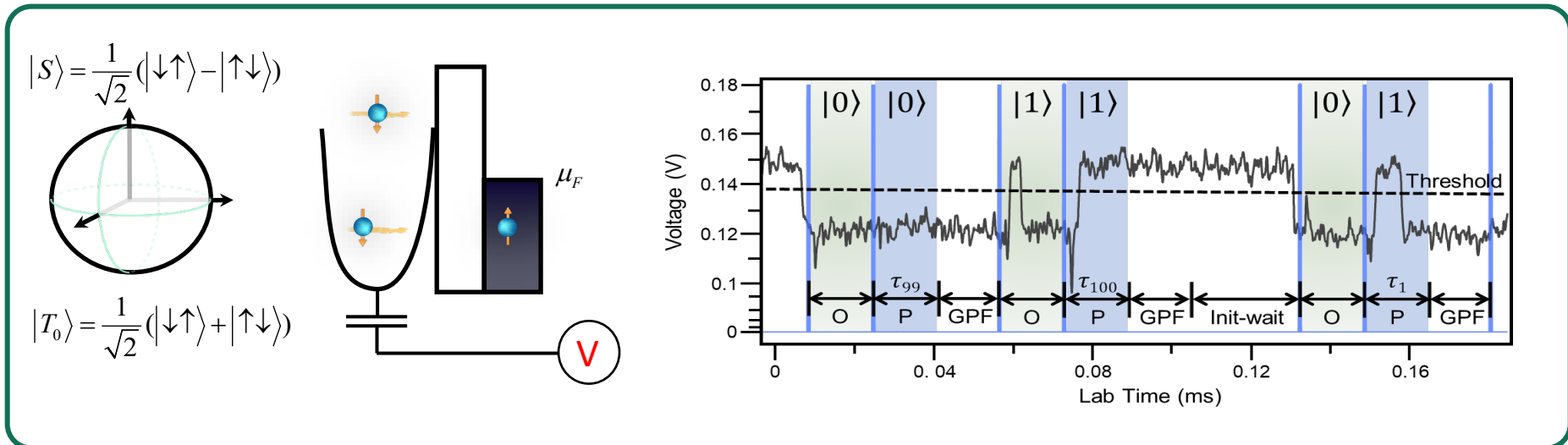
Something (mostly spin) to charge conversion

Single electron spin up-down qubit



Two electron singlet-triplet qubit

W. Jang et al, npj Quant. Inf., APL, Nano Letter.. Etc.



Current state of the art : $SNR \sim 10$ @ $t_{int} = 100$ ns, $F_{meas} > 99.5\%$ ($T_1 / T_{meas} > 500$) - SNU

2

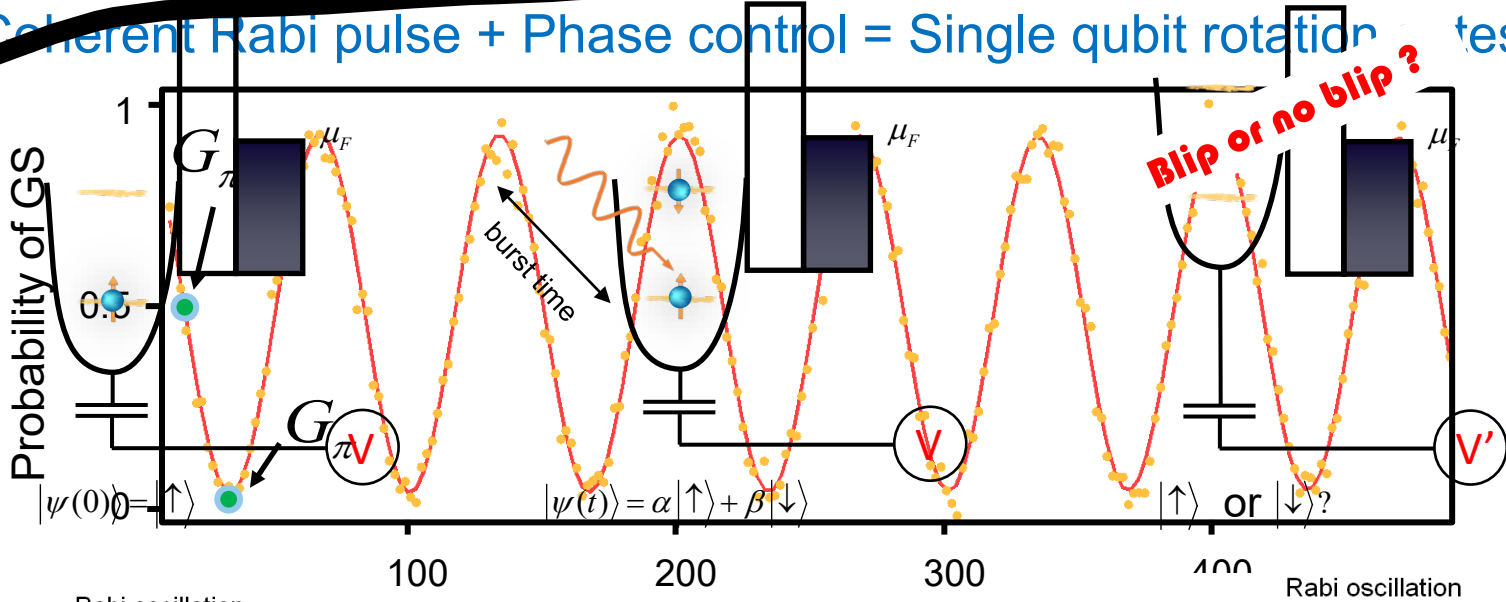
Approach: detailed description of experiments

Missing component : coherent manipulation

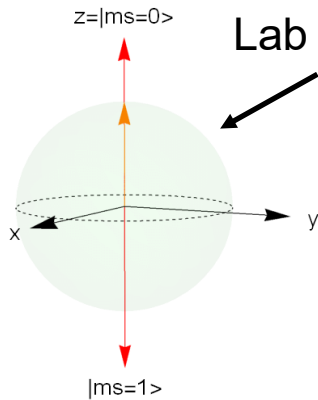
One way is to use resonant electromagnetic radiation...

Coherent Rabi pulse + Phase control = Single qubit rotation gates

Repeat

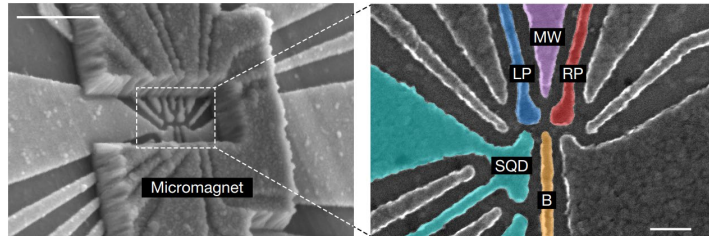


Rabi oscillation

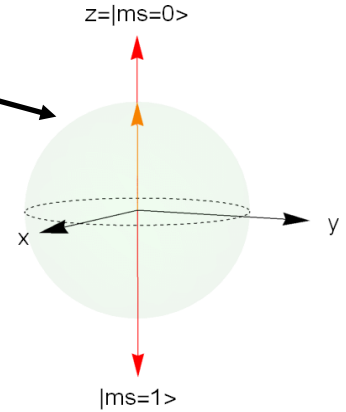


MW burst time (ns)

$$|0\rangle \xrightarrow{H} \frac{|0\rangle + |1\rangle}{\sqrt{2}}$$



Rotating frame

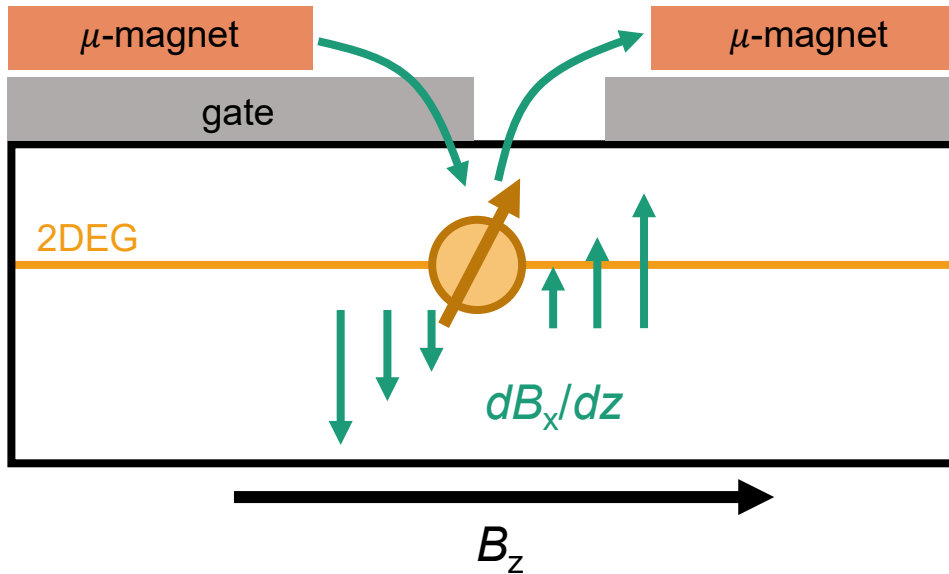


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Approach: detailed description of experiments

Role of micromagnet

Single spin electric dipole spin resonance (EDSR)



Single spin Hamiltonian

$$H = \mathbf{B} \cdot \mathbf{S}$$

$$H = B_z \sigma_z = \begin{bmatrix} B_z/2 & 0 \\ 0 & -B_z/2 \end{bmatrix}$$

$$\begin{aligned} H &= B_z \sigma_z + B_x(z) \sigma_x \\ &= \begin{bmatrix} B_z/2 & B_x(z)/2 \\ B_x(z)/2 & -B_z/2 \end{bmatrix} \end{aligned}$$

Electric driving of the electron wavefunction ($f_{mw} \sim$ zeeman splitting, B_z)

$$H = B_z \sigma_z + \delta B_x \cos(2\pi f_{mw}) \sigma_x = \begin{bmatrix} B_z/2 & \delta B_x \cos(2\pi f_{mw}) \\ \delta B_x \cos(2\pi f_{mw}) & -B_z/2 \end{bmatrix}$$

With the rotating wave approximation...

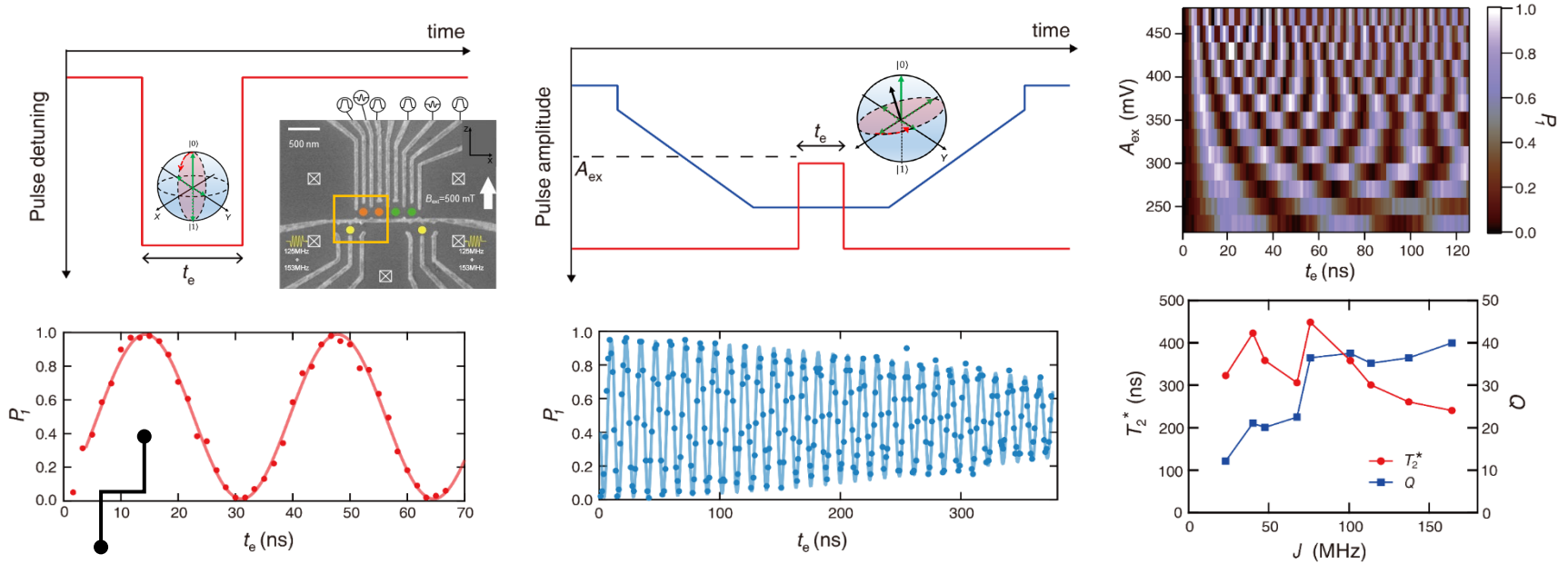
$$H_{rot} = \delta B_x \sigma_x + (B_z - f_{mw}) \sigma_z$$

@ Resonance, $H_{rot} = \delta B_x \sigma_x \rightarrow$ Rotation about the x-axis on the Bloch sphere

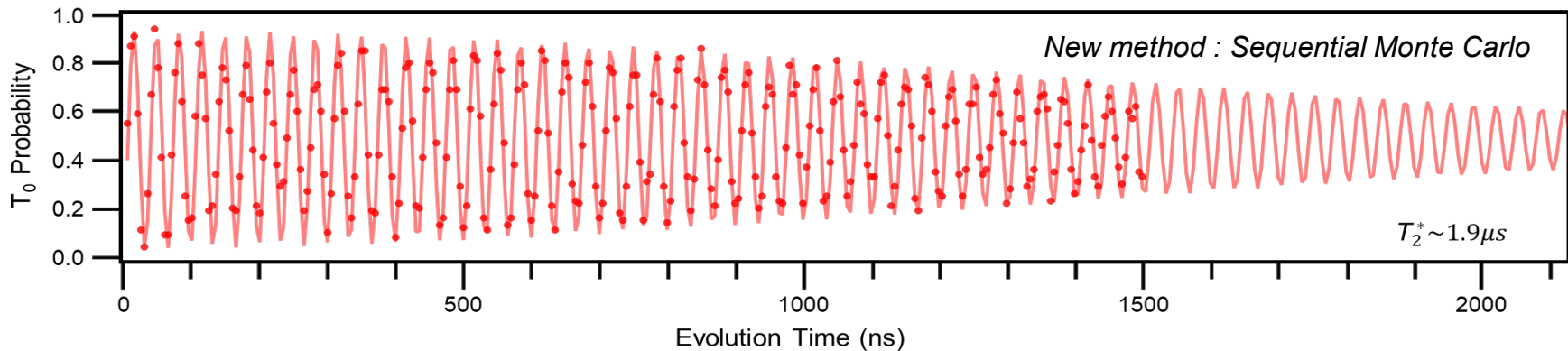
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Fast single-shot measurements

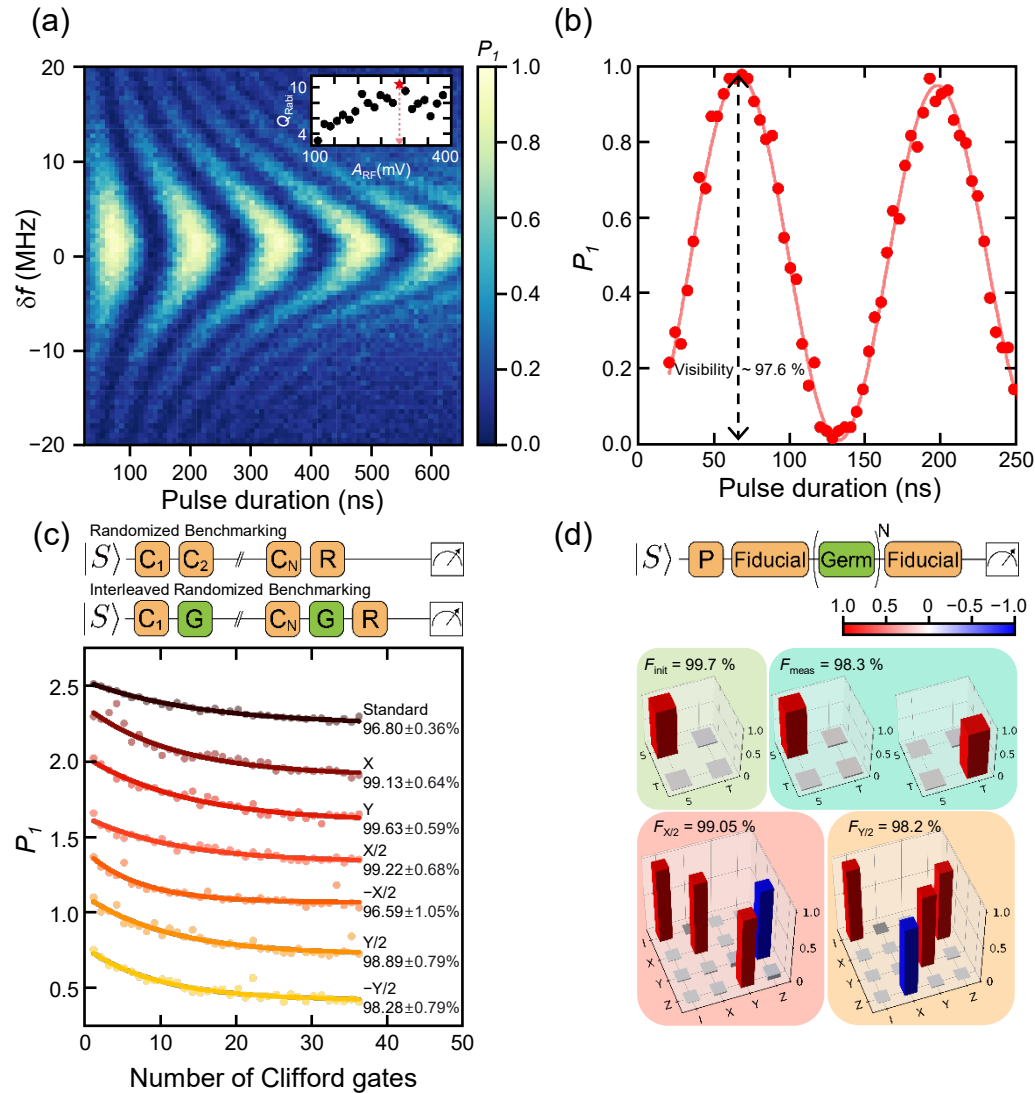
SNU contribution : record high visibility



Record high 98% visibility: > 99% 1Q gate (Bayesian), > 99.9% I, > 99.5 % M



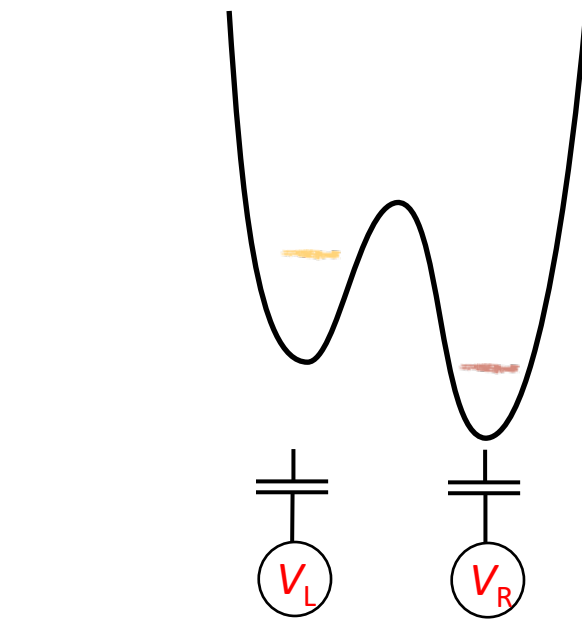
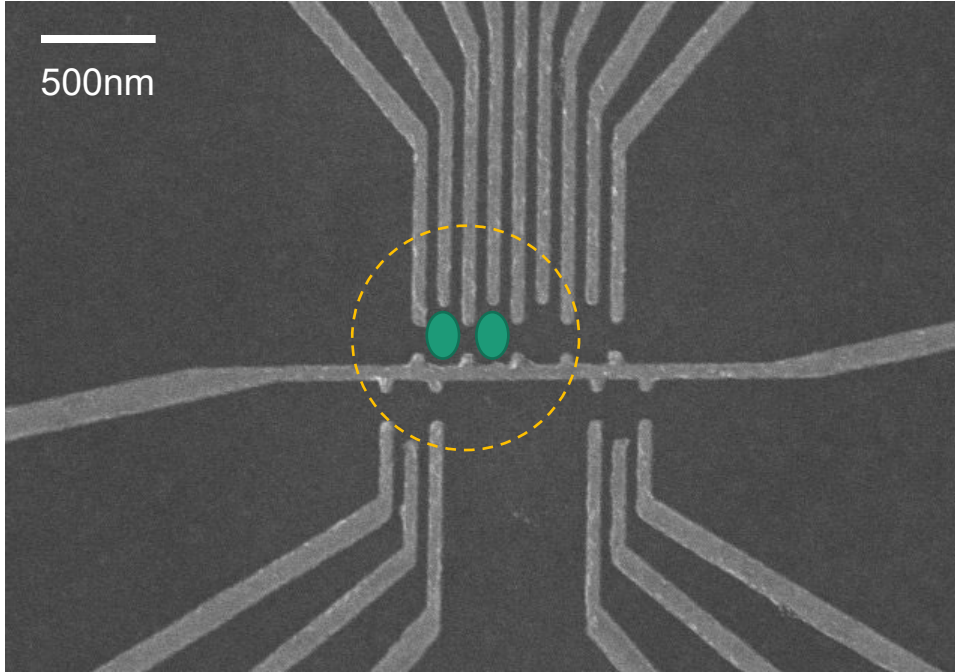
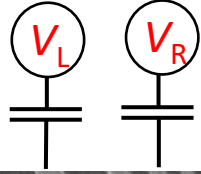
SNU contribution : record high fidelity



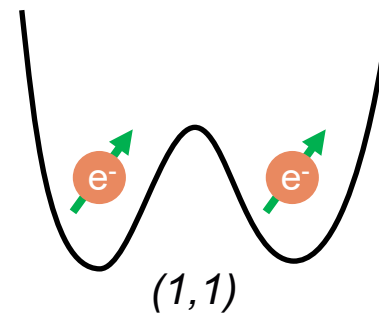
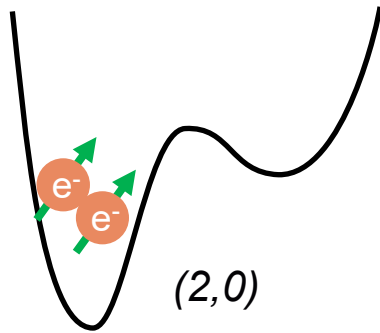
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Approach: detailed description of experiments

Two qubit gates



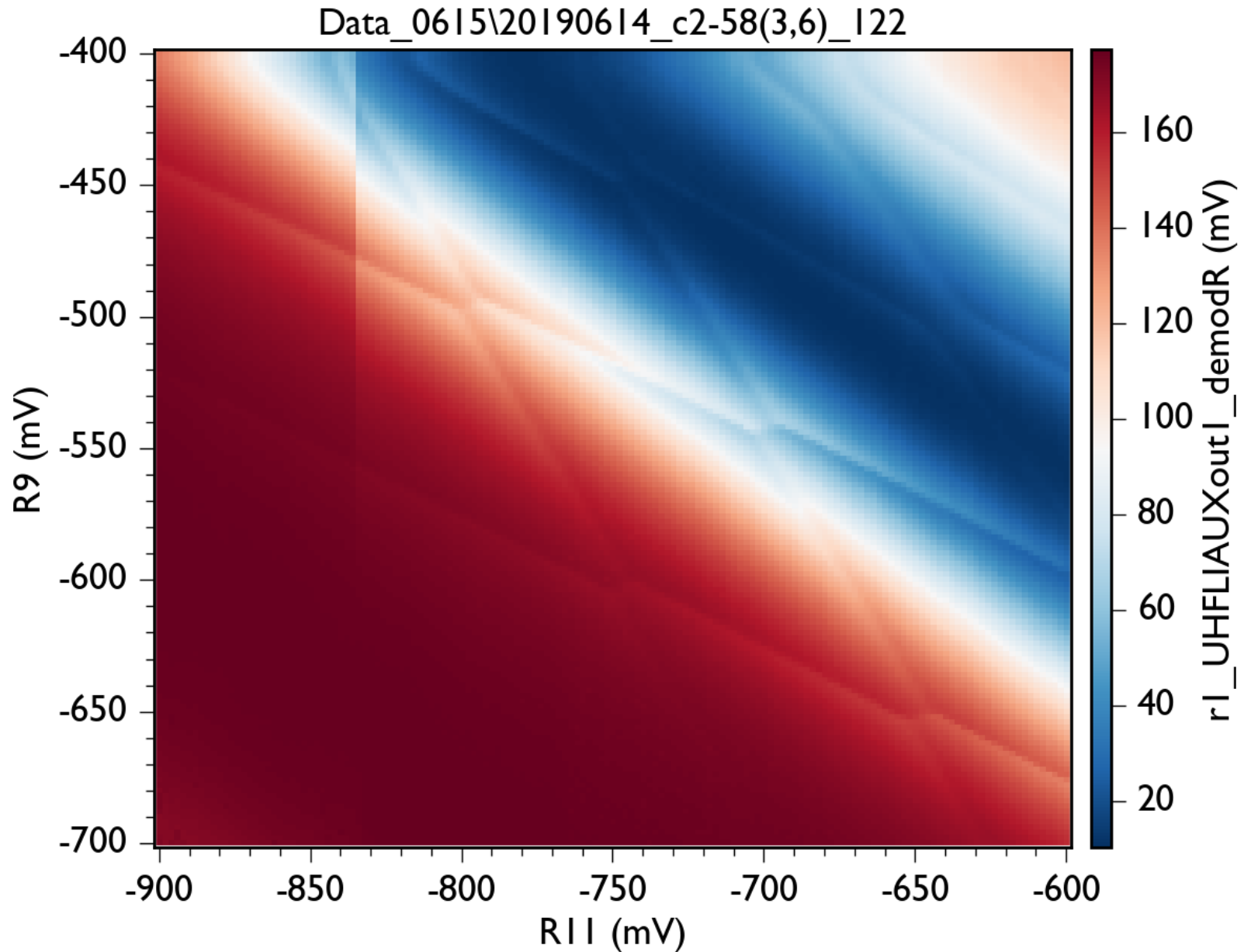
이중 양자점에 전자는 2개



2

Approach: detailed description of experiments

Charge stability diagram



2

Approach: detailed description of experiments

Two electron spin states & position pseudo-spin

Tunneling selection rule : $\Delta S = 0, \Delta S_z = 0$,
start with $|0\rangle_{(2,0)}$

Clebsch
- Gordan coeff.

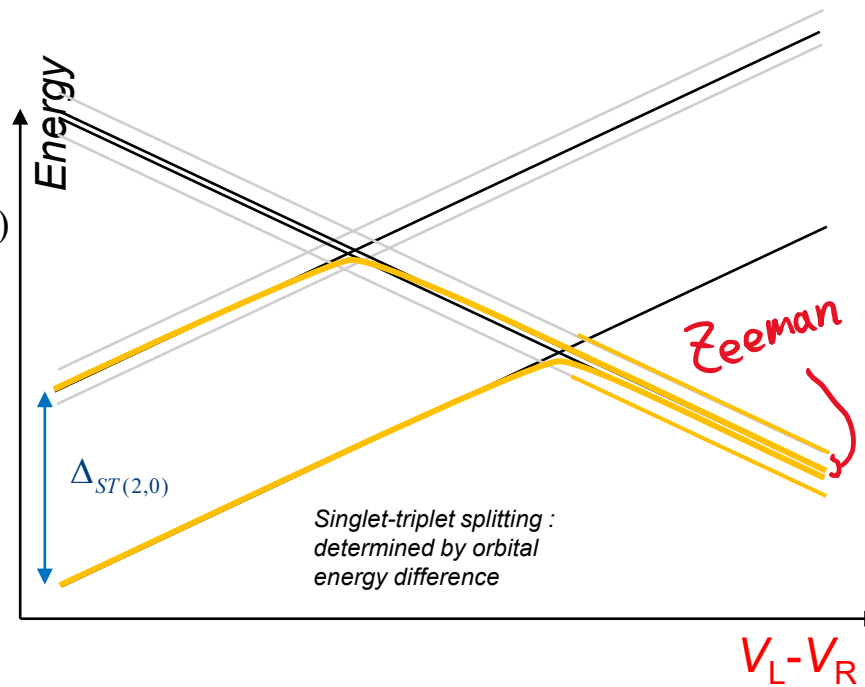
$$|3\rangle_{(2,0)} = |T_-\rangle = |\uparrow\uparrow\rangle$$

$$|2\rangle_{(2,0)} = |T_0\rangle = \frac{1}{\sqrt{2}}(|\downarrow\uparrow\rangle + |\uparrow\downarrow\rangle)$$

$$|1\rangle_{(2,0)} = |T_+\rangle = |\downarrow\downarrow\rangle$$

$$|0\rangle_{(2,0)} = |S\rangle = \frac{1}{\sqrt{2}}(|\downarrow\uparrow\rangle - |\uparrow\downarrow\rangle)$$

$$S_z = 0$$

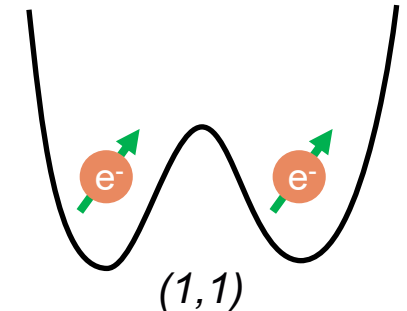
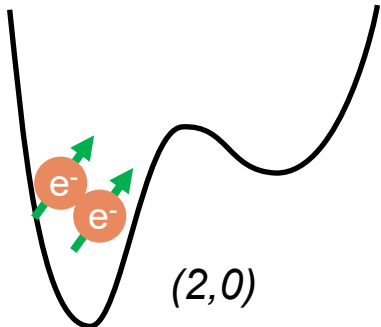


$$|3\rangle_{(1,1)} = |T_-\rangle = |\uparrow\uparrow\rangle$$

$$|2\rangle_{(1,1)} = |T_0\rangle = \frac{1}{\sqrt{2}}(|\downarrow\uparrow\rangle + |\uparrow\downarrow\rangle)$$

$$|1\rangle_{(1,1)} = |S\rangle = \frac{1}{\sqrt{2}}(|\downarrow\uparrow\rangle - |\uparrow\downarrow\rangle)$$

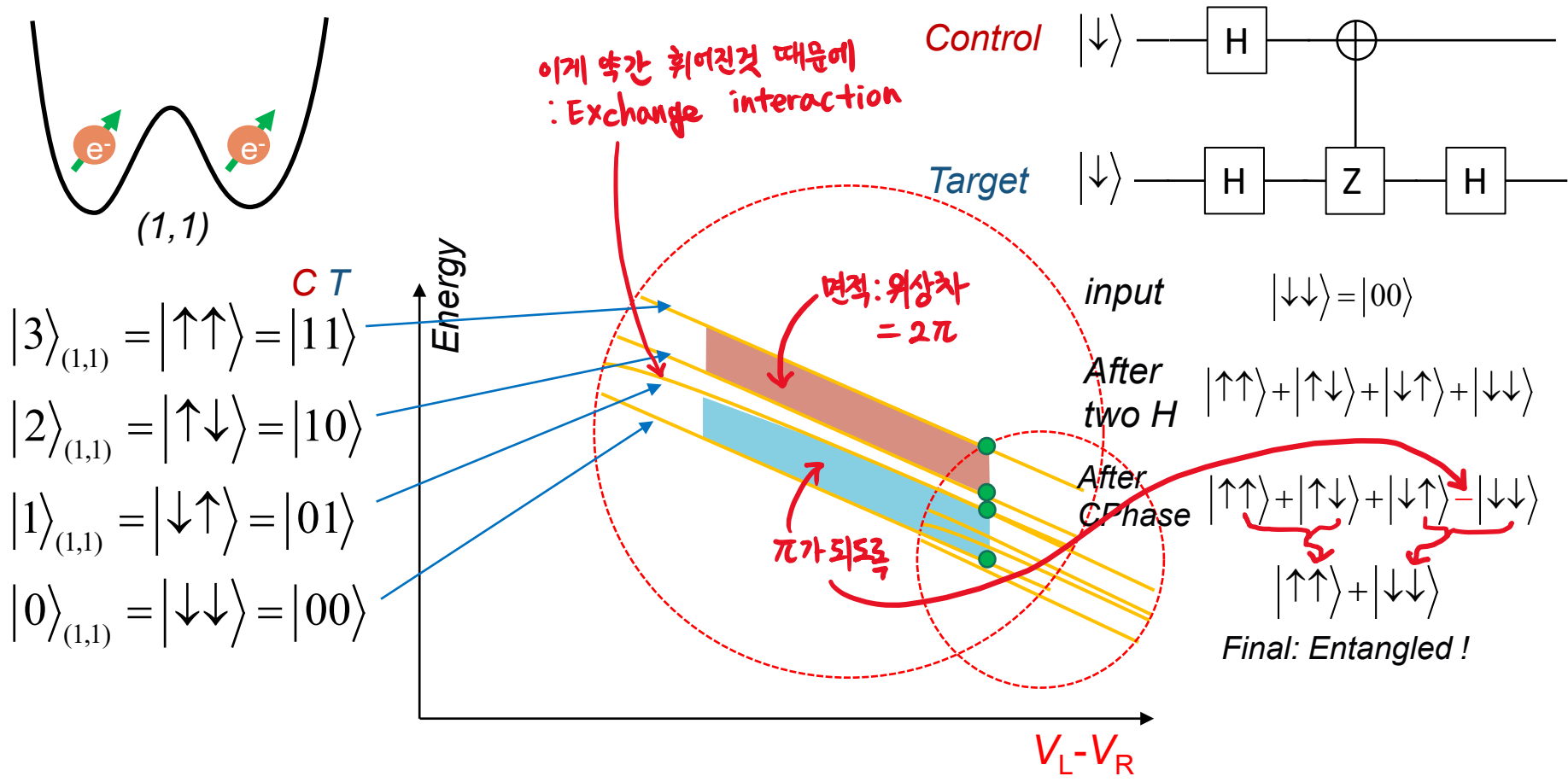
$$|0\rangle_{(1,1)} = |T_+\rangle = |\downarrow\downarrow\rangle$$



2

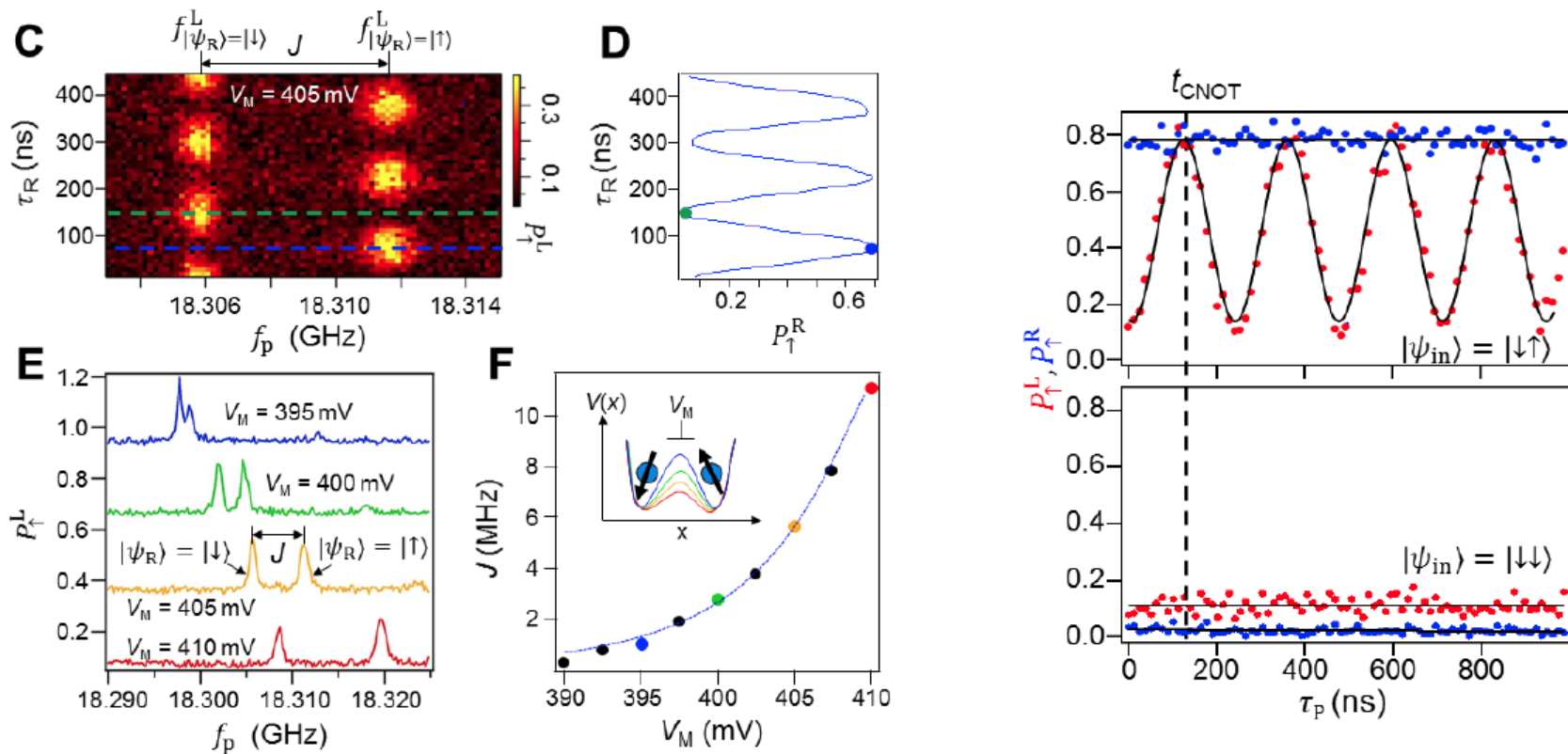
Approach: detailed description of experiments

Essential physics for a QD-based QC



Take home message : 1Q gate 는 자기공명 (Rabi oscillation) 으로, 2Q gate 는 exchange interaction or capacitive coupling 에 의한 controlled phase 로 = Universal gate set for arbitrary quantum operation

Another way : Controlled rotation gate



2

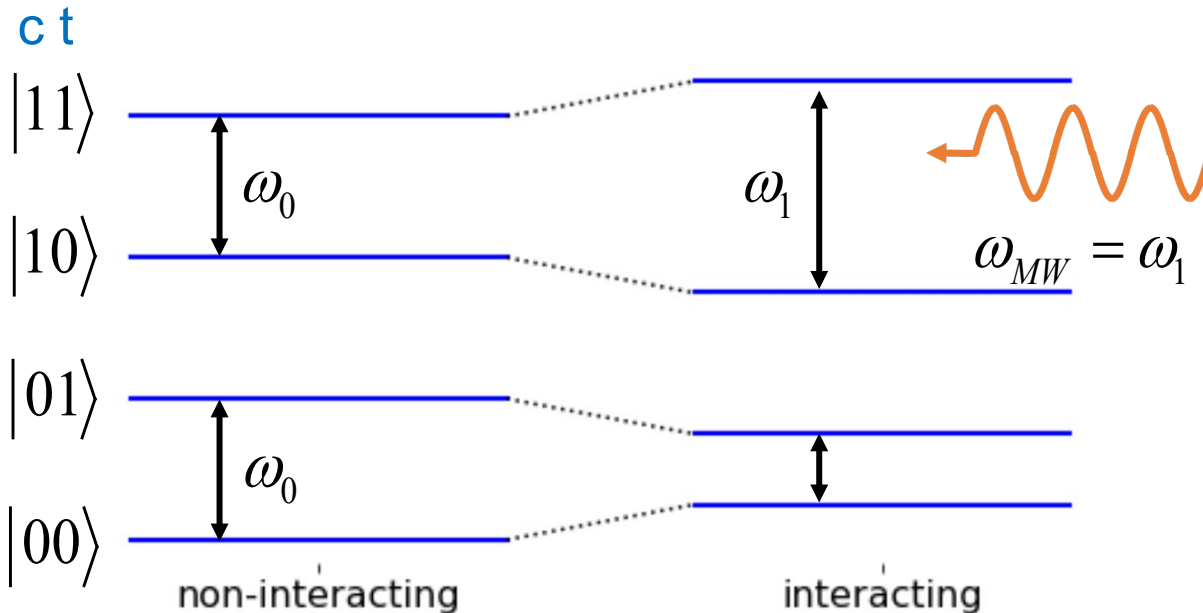
Approach: detailed description of experiments

Another way : Controlled rotation gate

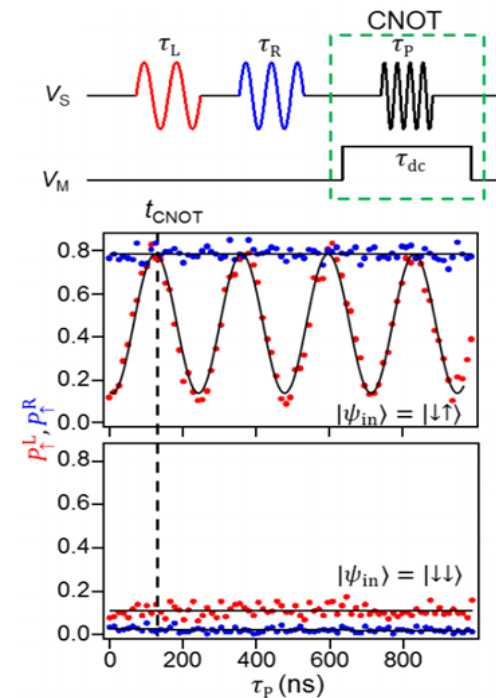
Two qubit gate

Ex. Calibrated Rabi π pulse under two body interaction = CNOT

$$\hat{H} = \frac{\hbar\omega_0}{2} (2\hat{\sigma}_{z1} \otimes I + I \otimes \hat{\sigma}_{z2}) + \hbar g (\hat{\sigma}_{z1} \otimes \hat{\sigma}_{z2})$$



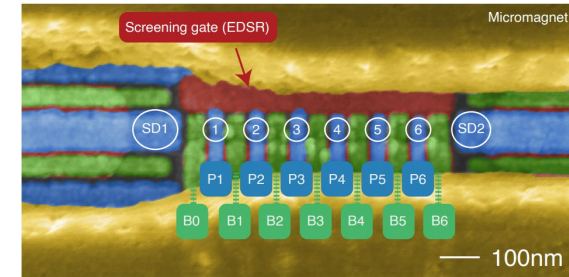
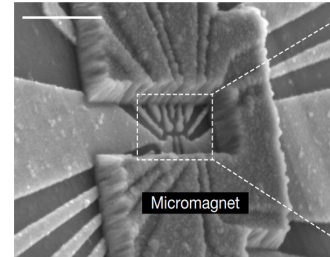
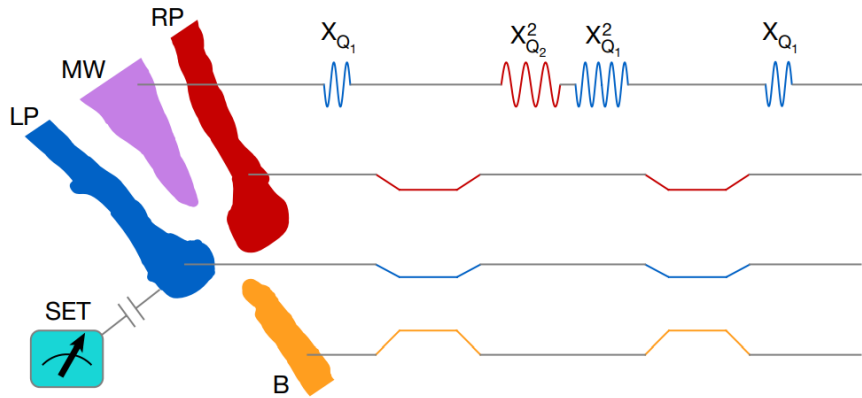
반도체 스핀 큐비트의 예



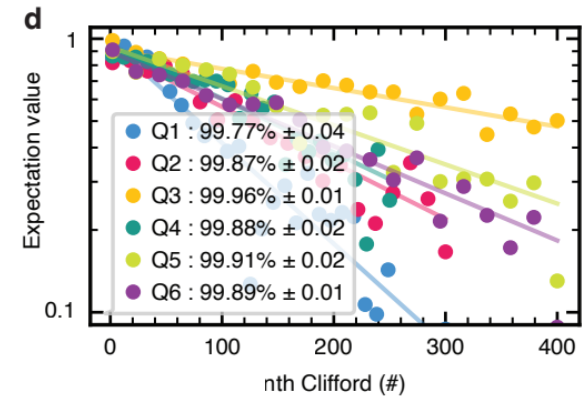
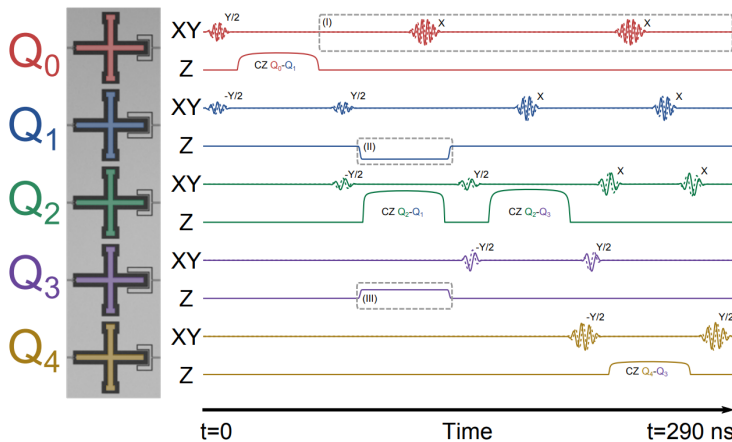
2

Approach: detailed description of experiments

Current state of the art



Cf. 5- SC qubit experiment (UCSB 2014, Nature)



<https://arxiv.org/abs/2202.09252>

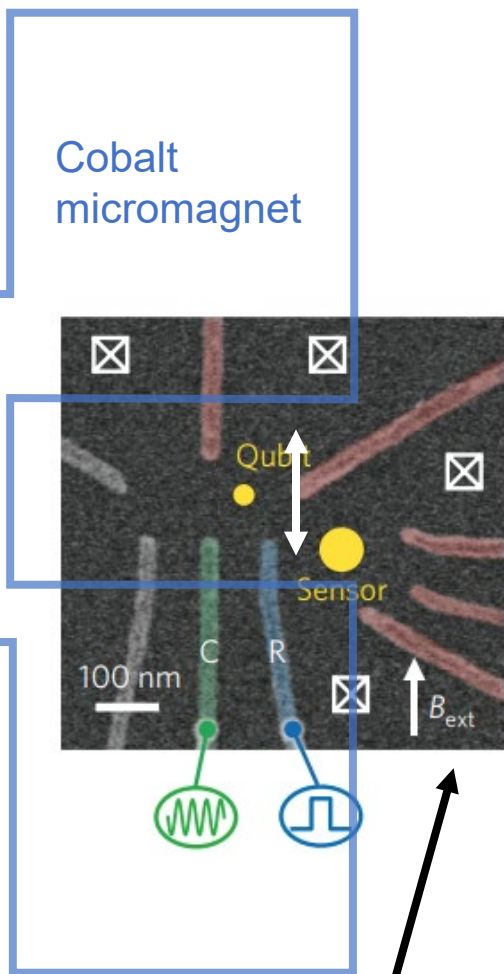
Both 1Q, 2Q gate fidelities exceed surface code error correction threshold.

멀티 큐비트 작동의 자세한 시퀀스 설명은 Lecture 2 에서..

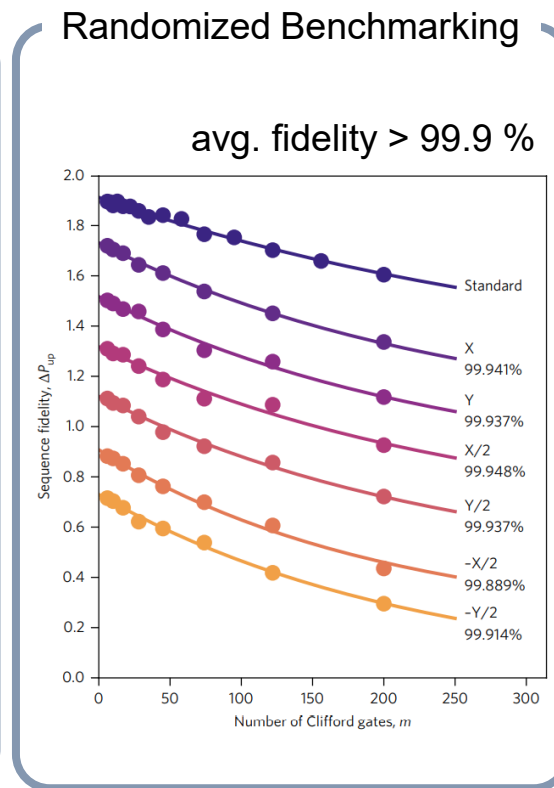
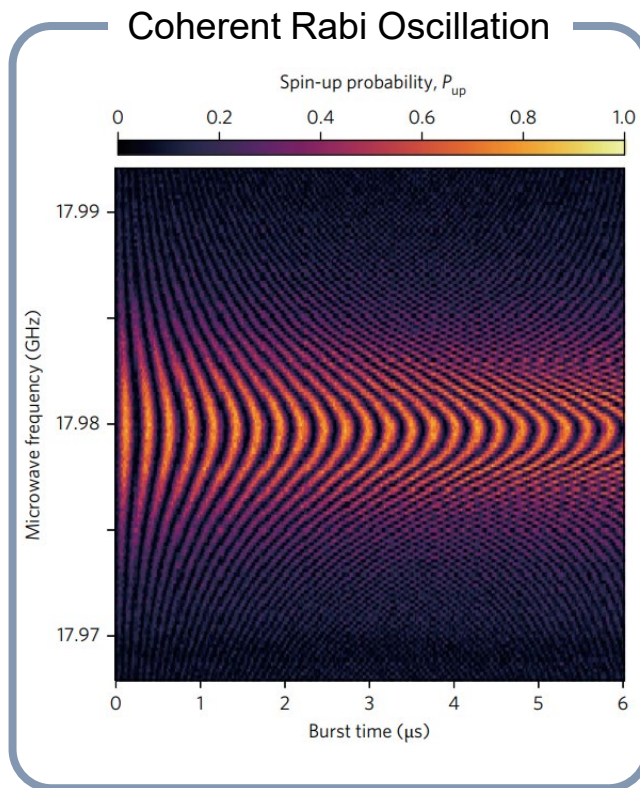
2

Approach: detailed description of experiments

Current state of the art



Purified ^{28}Si



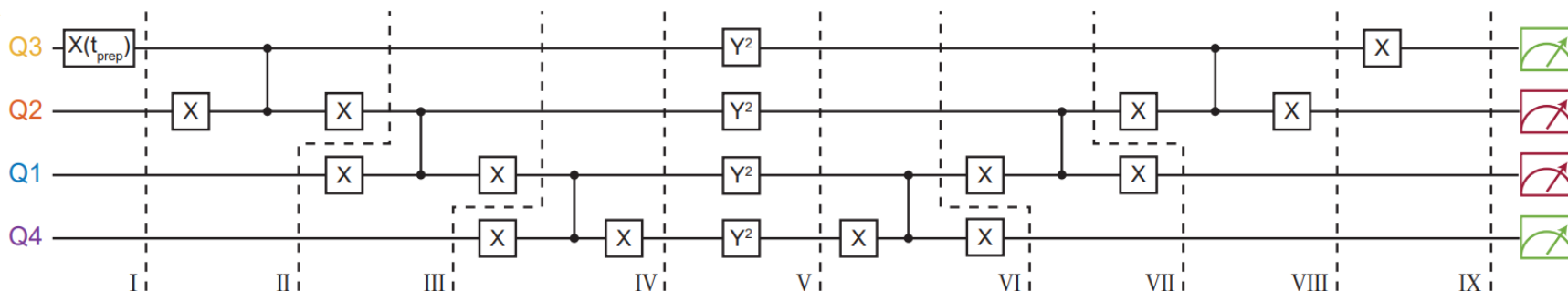
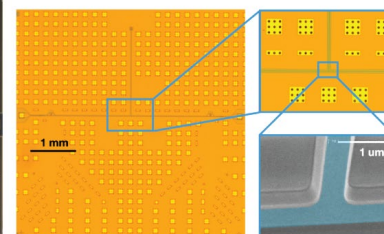
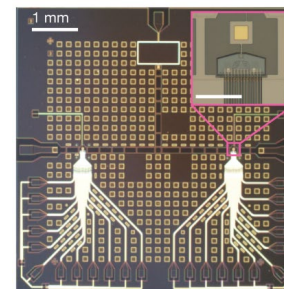
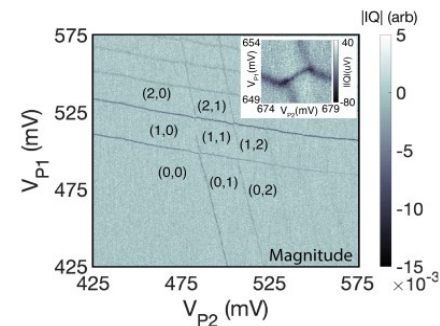
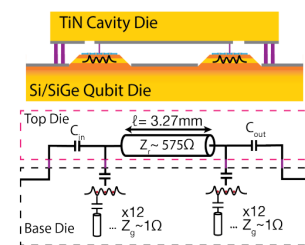
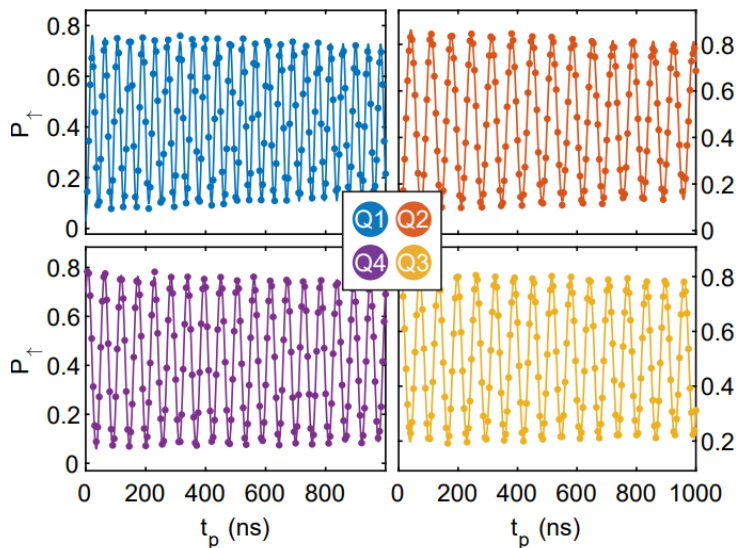
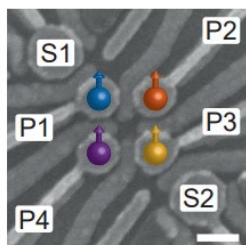
- **High fidelity single qubit control (> 99.9%, confirmed by RB) in the purified ^{28}Si**
- **Charge noise limited coherence (CPMG, Ramsey measurement)**

2

State of the art in single-spin qubits

Example: Si, GaAs, Ge.. Boosting up results

Most recent developments : Germanium 4 qubit processing & 3D integration



Again, 회로설명은 Lecture 2에서..

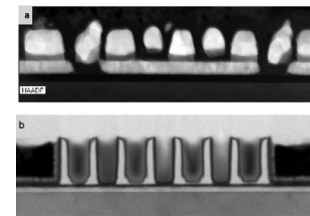
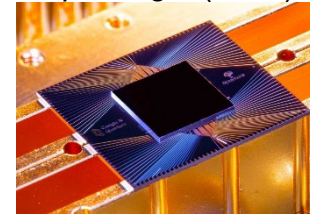
quTech, Delft Sep. 2020
M.Eriksson group UW Nov. 2020

2

State of the art in single-spin qubits

Recent developments of QD-based QC

Sycamore chip Google (2020)

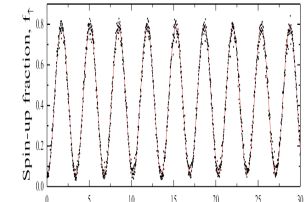
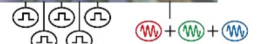
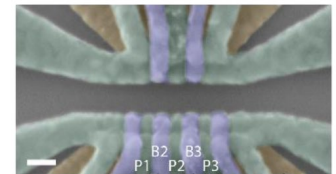


University lab.

Intel 300mm CMOS process

6Q processor in Si (2022)

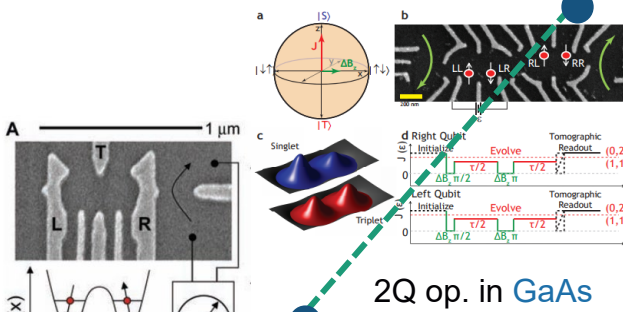
4Q GHZ in Ge
3Q GHZ in Si



Nature Nanotech. 9, 981 (2014)

cf. superconducting qubits

- Koppens et al., Nature. 442 766 (2006)
- Maune et al., Nature. 481 344 (2012)
- Shulman et al., Science 336 202 (2012)
- Watson et al., Nature. 555 633 (2018)
- Hendrickx et al., Nature. 591 580 (2021)
- ... many more.



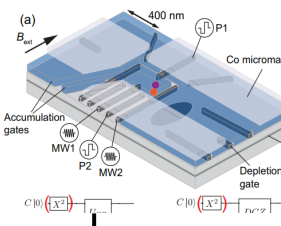
2Q op. in GaAs

1Q op. in GaAs

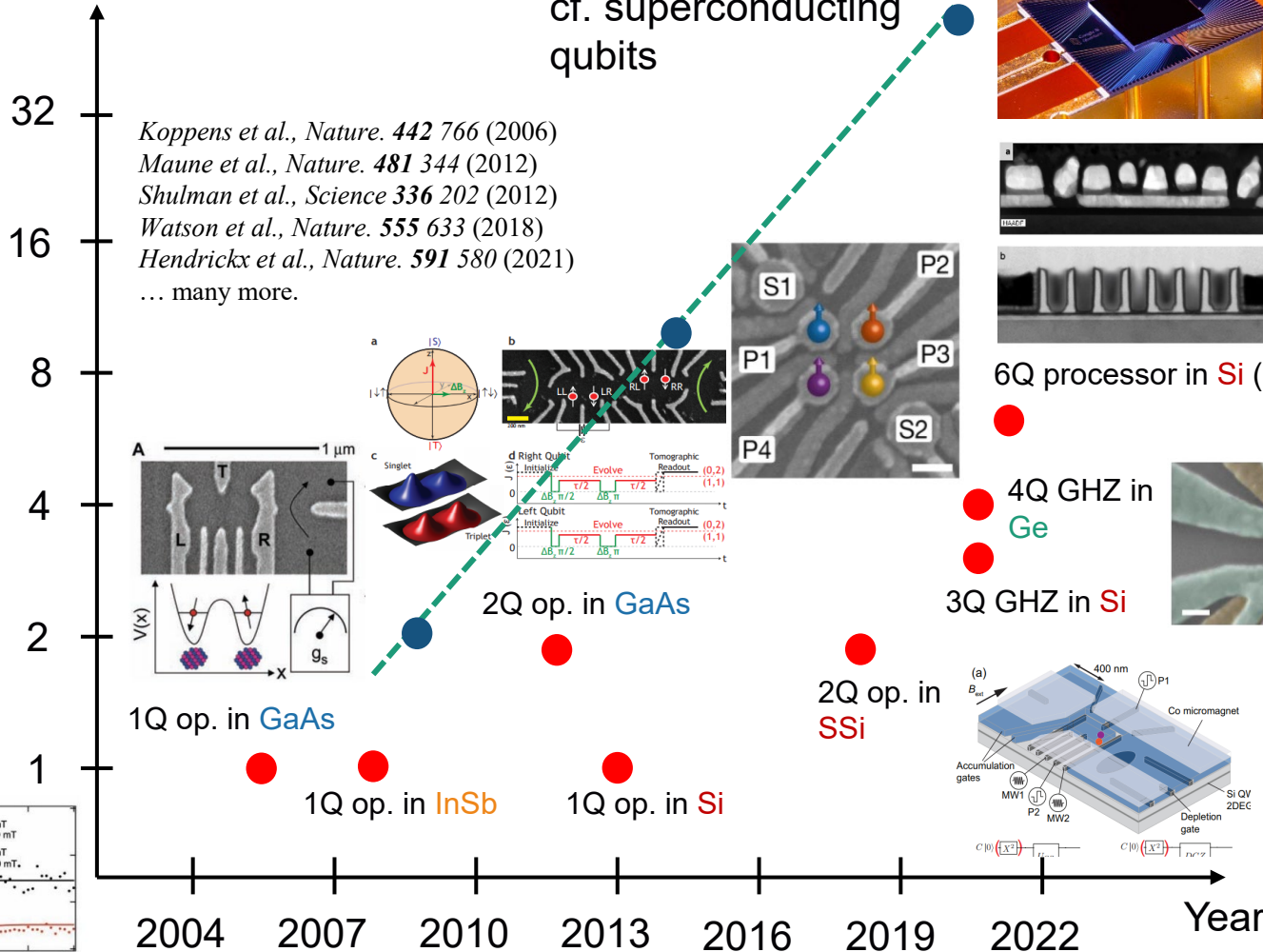
1Q op. in InSb

1Q op. in Si

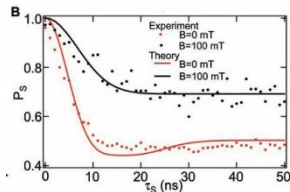
2Q op. in SSi



Fully entangled qubits



Science 309, 2180 (2005)

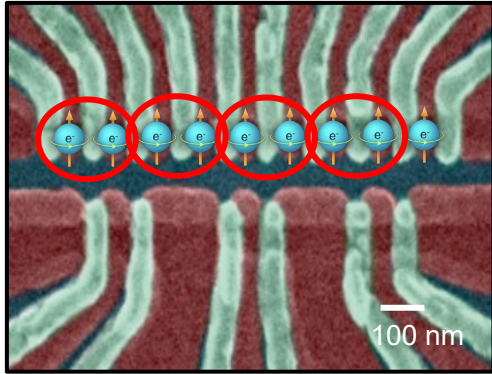


N. P. de Leon, Kohei M. Itoh, Dohun Kim, Karan K. Mehta, Tracy E. Northup, Hanhee Paik, B. S. Palmer, N. Samarth, Sorawis Sangtawesin, D. W. Steuerman "Material challenges and opportunities for quantum computing hardware" - Science. 372, 253 (2021) Review paper

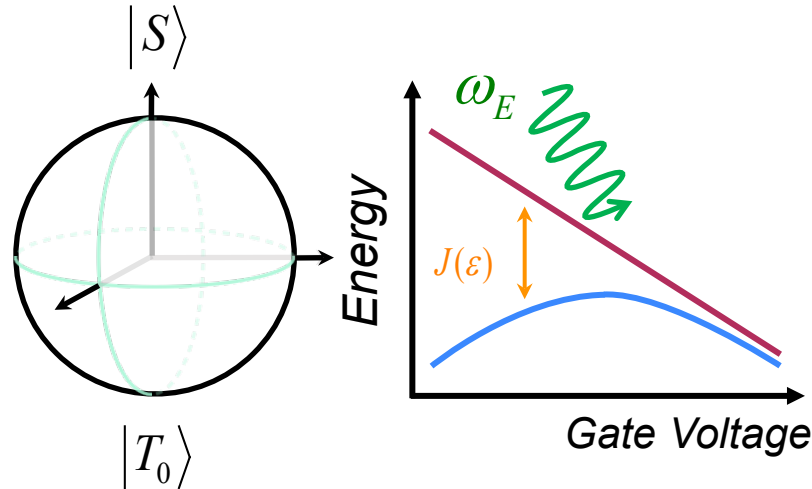
3

Approach : detailed description of experiments

The type of qubit we focus



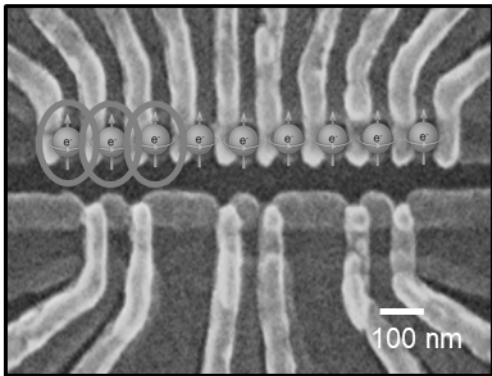
Two electron spin in DQD



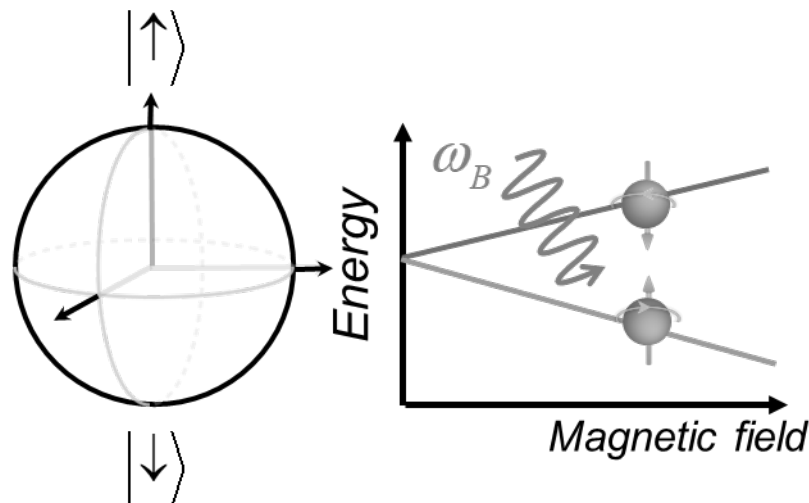
- *E-field control*
- *Fast ~ ns gate*
- *Nucl. polarization*
- *D or Ex coupling*
- *Complexity*
- *Less SNR (improvable)*

For GaAs system

cf. canonical type : single electron spin up-down qubit



Single electron spin



- *Simple*
- *Most coherent*
- *Higher SNR*
- *Exchange coupling*
- *B-field control*
- *slow ~ us gate*

For Si system

3

Singlet-Triplet qubits

Different look at two-spin states

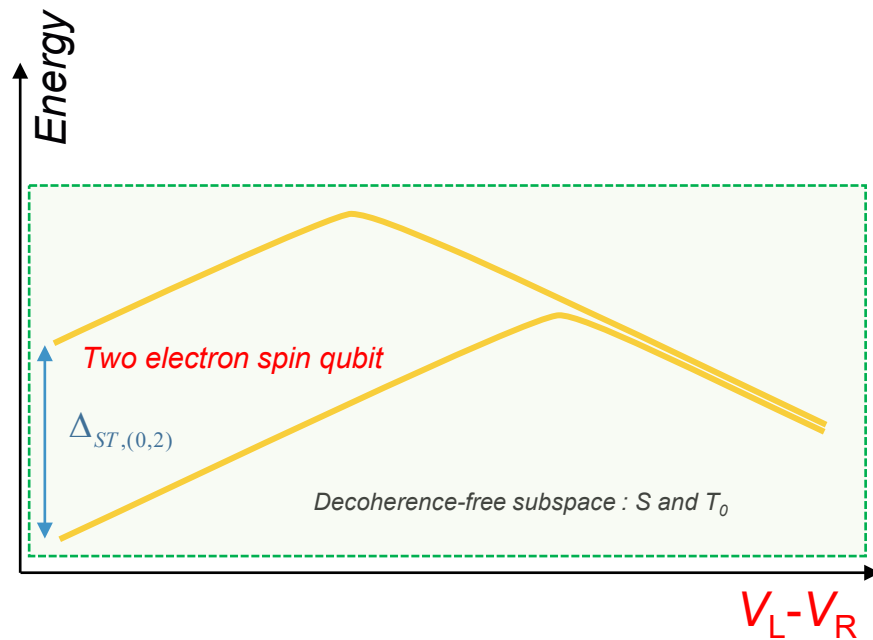
Clebsch
- Gordan coeff.

$$|3\rangle_{(2,0)} = |T_-\rangle = |\uparrow\uparrow\rangle$$

$$|2\rangle_{(2,0)} = |T_0\rangle = \frac{1}{\sqrt{2}}(|\downarrow\uparrow\rangle + |\uparrow\downarrow\rangle)$$

$$|1\rangle_{(2,0)} = |T_+\rangle = |\downarrow\downarrow\rangle$$

$$|0\rangle_{(2,0)} = |S\rangle = \frac{1}{\sqrt{2}}(|\downarrow\uparrow\rangle - |\uparrow\downarrow\rangle)$$

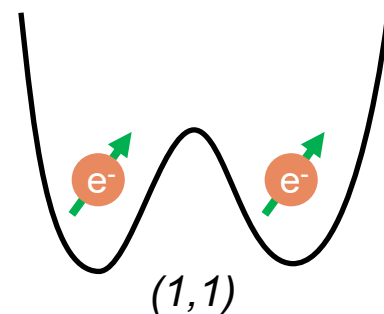
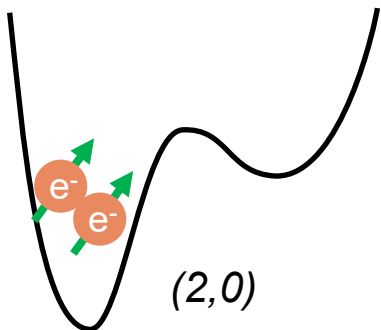


$$|3\rangle_{(1,1)} = |T_-\rangle = |\uparrow\uparrow\rangle$$

$$|2\rangle_{(1,1)} = |T_0\rangle = \frac{1}{\sqrt{2}}(|\downarrow\uparrow\rangle + |\uparrow\downarrow\rangle)$$

$$|1\rangle_{(1,1)} = |S\rangle = \frac{1}{\sqrt{2}}(|\downarrow\uparrow\rangle - |\uparrow\downarrow\rangle)$$

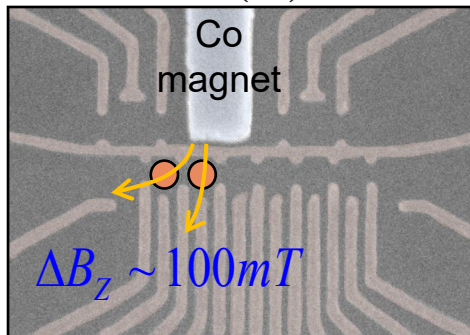
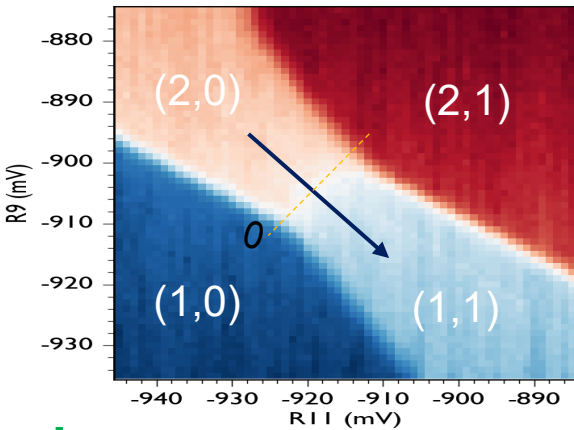
$$|0\rangle_{(1,1)} = |T_+\rangle = |\downarrow\downarrow\rangle$$



3

Approach : detailed description of experiments

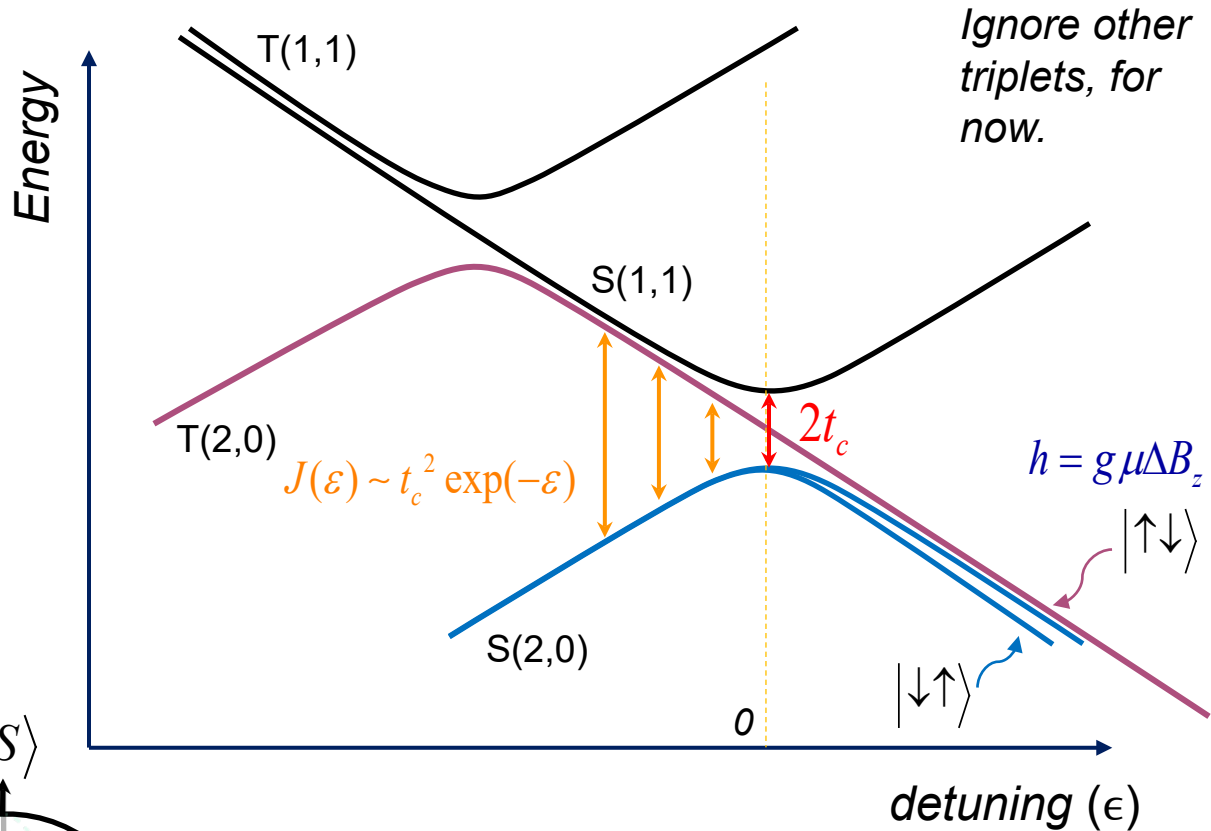
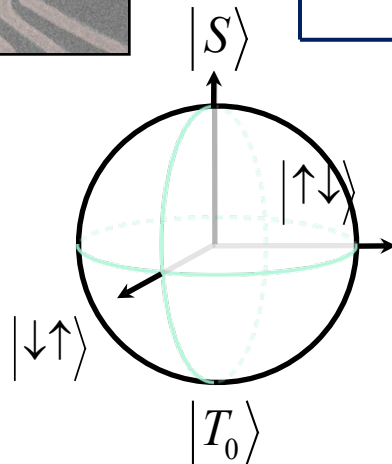
Introduction to DQD - ST qubit



$B_{Z,ext}$

$$H = \begin{bmatrix} J(\epsilon) & h \\ h & 0 \end{bmatrix}$$

$$h = g\mu\Delta B_z$$



Singlet

-Triplet

Qubit

- Two electrons in a DQD
- Voltage dependent Q energy
- J & h determines eigenaxes
- Typical values
 J : 0~30 GHz (0~120 μeV)
 h : 0~1 GHz (0~4 μeV)

3

Singlet-Triplet qubits

Field-gradient-based two electron spin qubits

주요 스펙

- 큐비트 주파수: 수백 MHz
- 검출 주파수: 수백 MHz
- T_1 시간 > 최소 수백 μs
- T_2 시간: 재료에 크게 의존 (뒤에서...)
- 이중 큐비트 속도 : 수~수십 MHz (뒤에서...)

디자인 철학을 공유: operation 때는 잘 숨기고, readout 때는 큰 상호작용

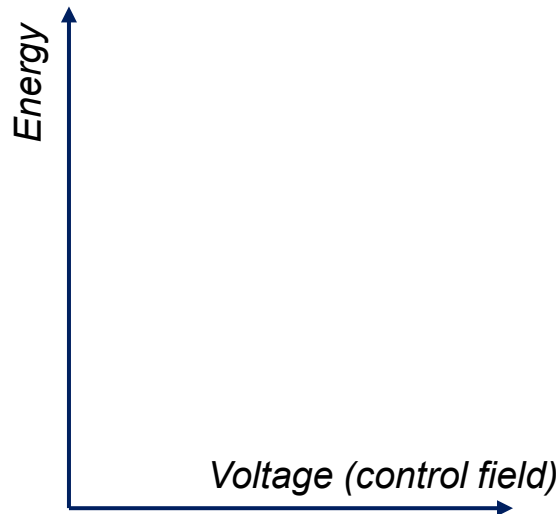
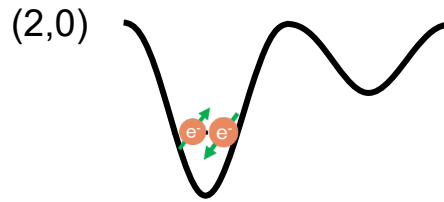
Cf. 초전도 트랜스몬

- 큐비트 주파수: 수 GHz
- 검출 주파수: 수 GHz
- Dispersive readout

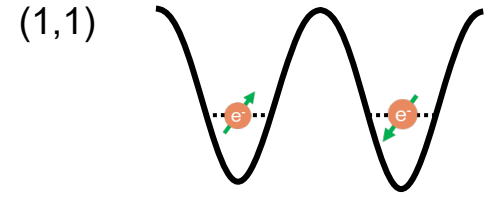
Practicality

- 전기적인 spin 제어
- 큰 튜너빌리티
- < 1 GHz 의 낮은 제어라인 bandwidth 요구도

Qubit 초기화, 측정 영역 빠른 초기화, 스핀-전하 변환



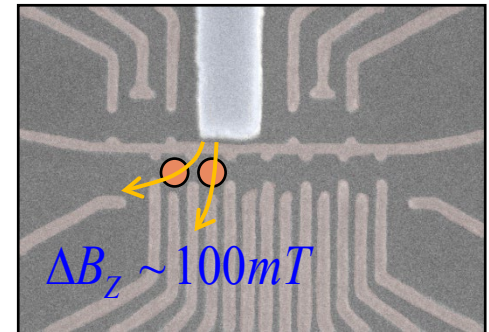
Qubit Operation 영역 긴 결맞음



$$|1\rangle = |\uparrow\downarrow\rangle$$

ΔB_z 에만 의존 (전하잡음 무관)

$$|0\rangle = |\downarrow\uparrow\rangle$$

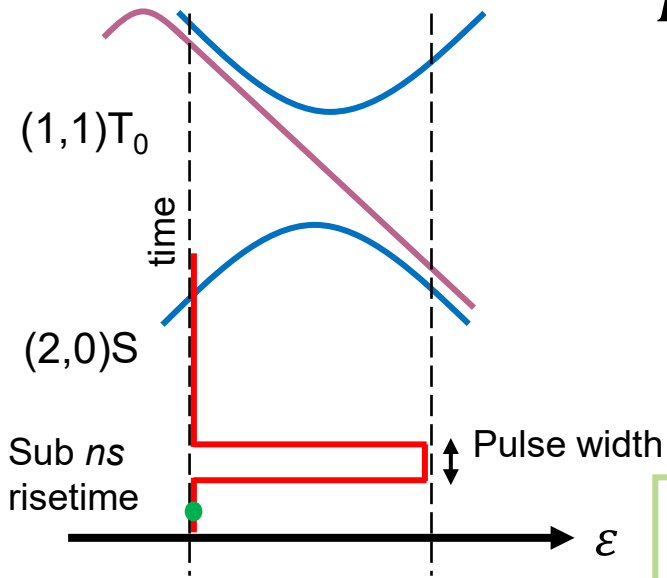


3

Approach : detailed description of experiments

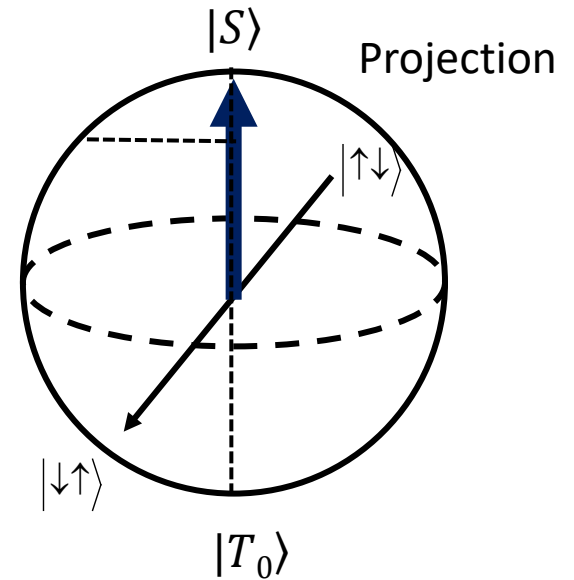
Initialization, Operation & Measurement of STQ

Operation: Voltage pulsing



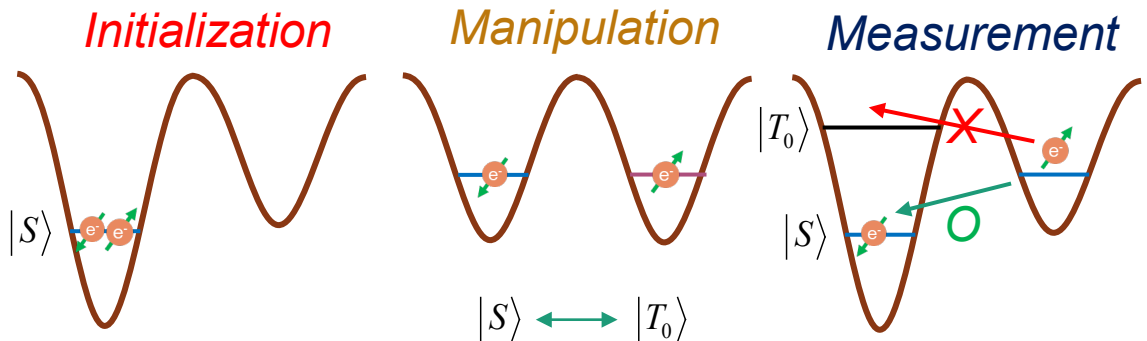
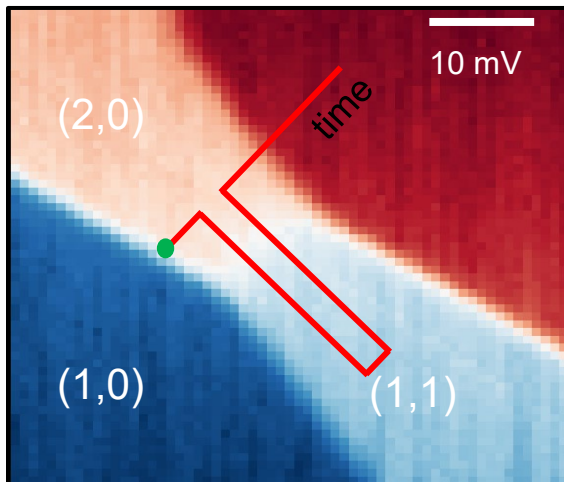
$$H = \begin{bmatrix} J(0\epsilon) & \Delta B \\ \Delta B & 0 \end{bmatrix}$$

Initialization: ST relaxation (μs to ms – also voltage dependent)



Measurement: How to distinguish $|S\rangle$ from $|T_0\rangle$?
Pauli Spin Blockade

Spin to charge conversion
 $|S\rangle$ becomes $(2,0)$
 $|T_0\rangle$ remains in $(1,1)$

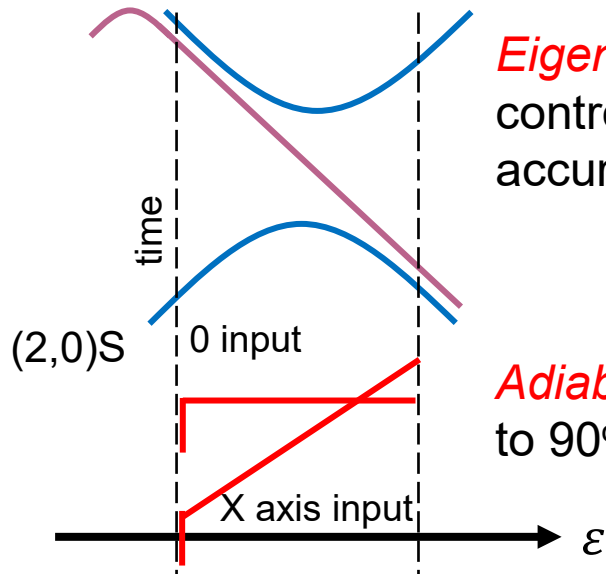


3

Approach : detailed description of experiments

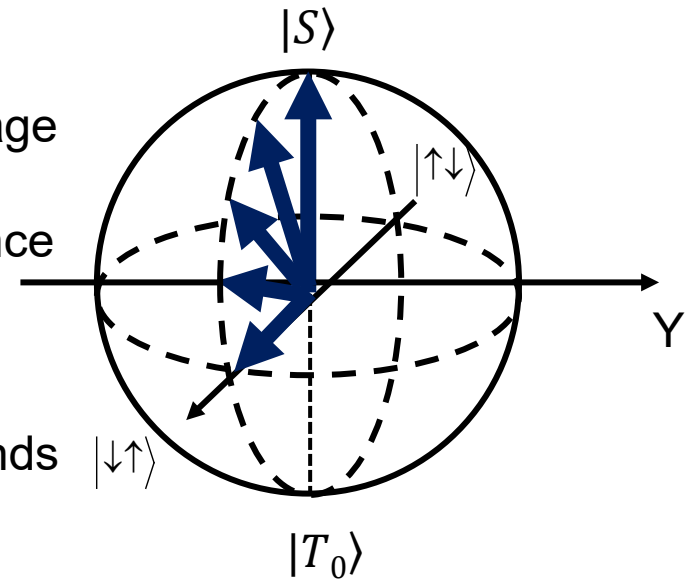
Tomographic sequence of STQ

High fidelity preparation of various input states

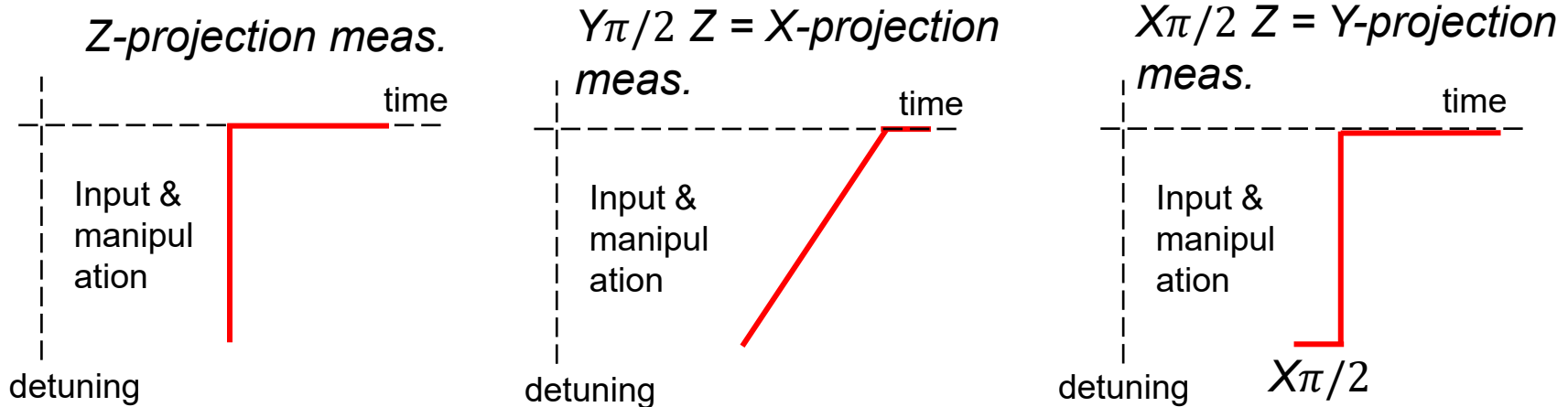


Eigenaxis controllability: Voltage controlled splitting allows accurate tomographic sequence

Adiabatic in & out : Corresponds to 90° rotation around Y axis



Versatile measurement axis rotation



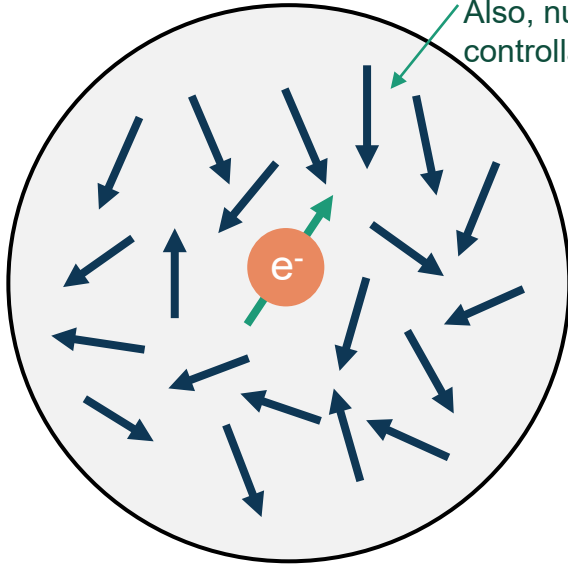
3

Approach: detailed description of experiments

Materials for QD qubits

GaAs

Fluctuating, but slow
enough to keep track
Also, nuclear
controllability



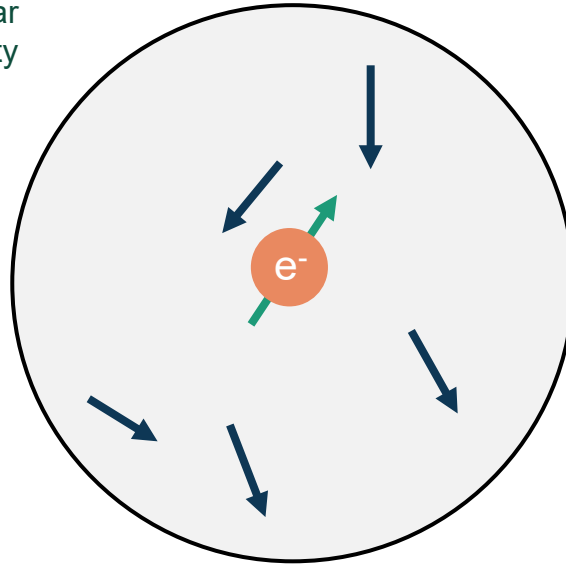
Material advantage

- *Mature growth, Ultra-stability*
- Clean QD formation
- Direct Band-gap – single valley

Major huddle

- *Nuclear control overhead*

^{Nat}Si or ²⁸Si



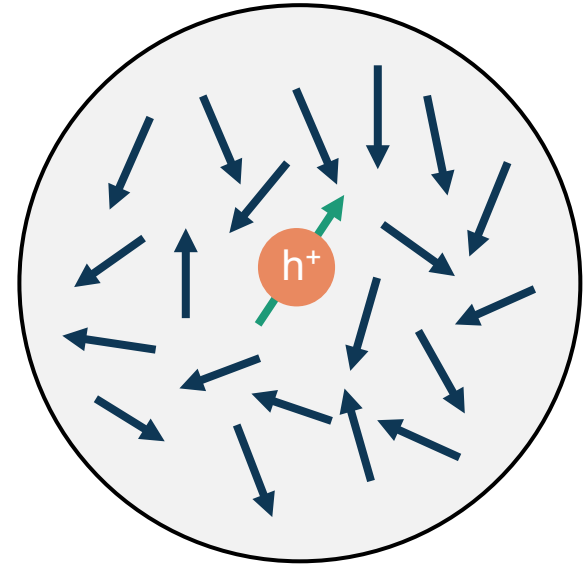
Material advantage

- *Small nuclear spin density*

Major huddle

- *Stringent fab. Req.*
- Unstable charge-traps
- Complicated valley physics

Ge (hole)



Material advantage

- *Hole spin less susceptible to nuclear noise*
- *Electric spin control (spin-orbit)*

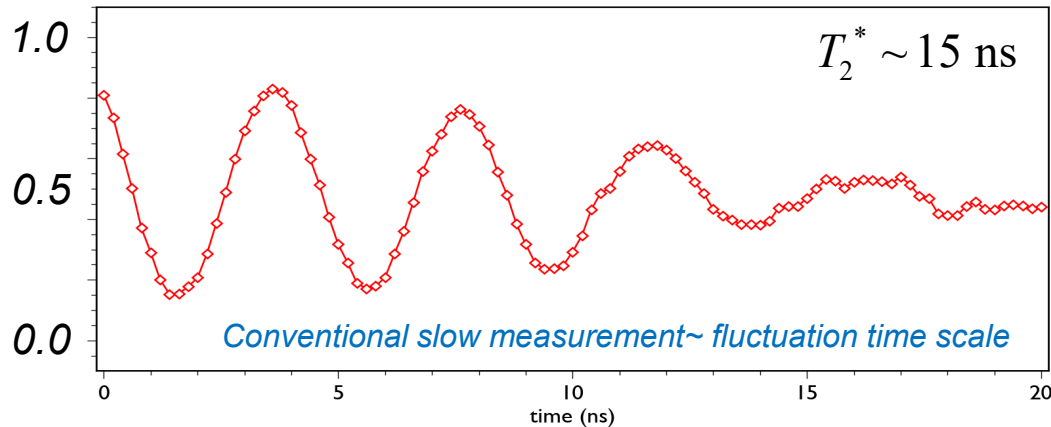
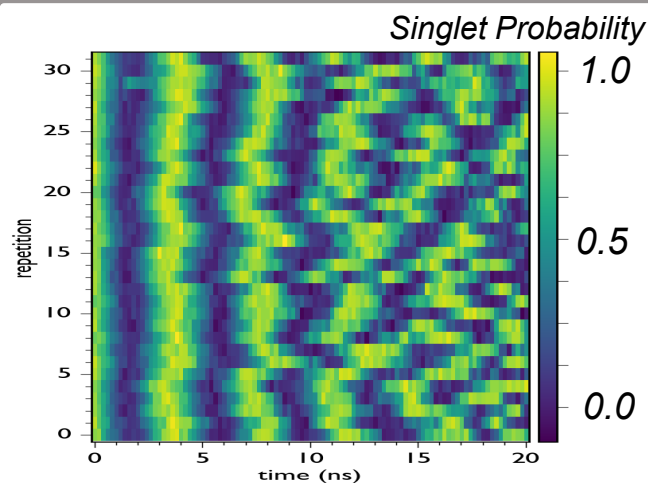
Major huddle

- *Charge noise susceptibility (spin-orbit coupling)*

3

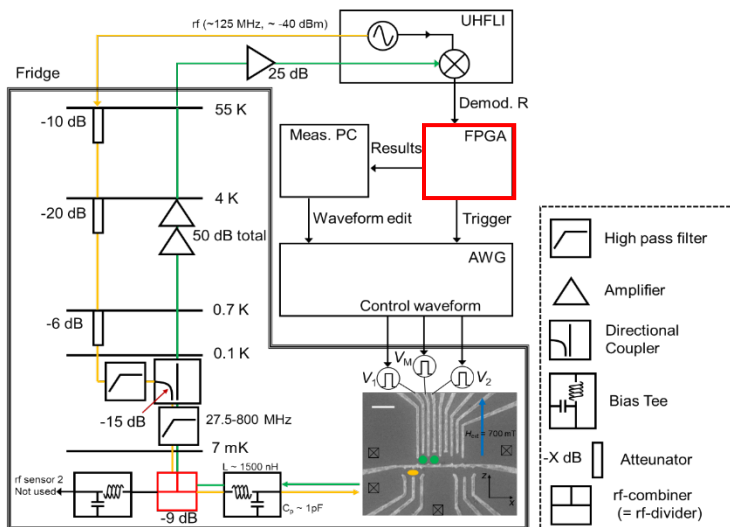
Singlet-Triplet qubits

Real time Hamiltonian Parameter estimation

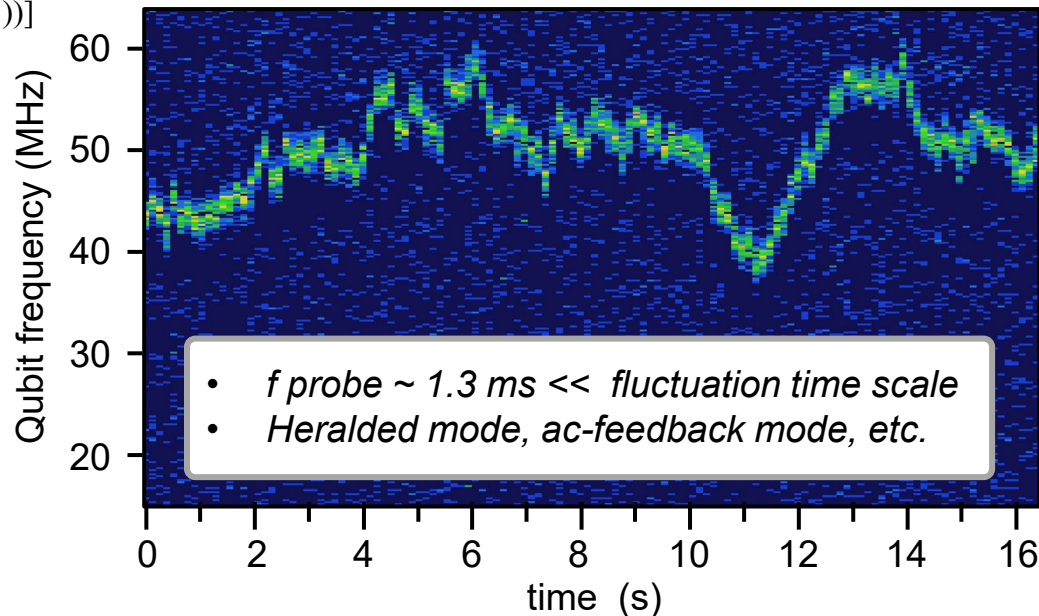


Bayesian inference with FPGA M.D. Shulman et al., *Nature Comm.* 5 5156 (2013)

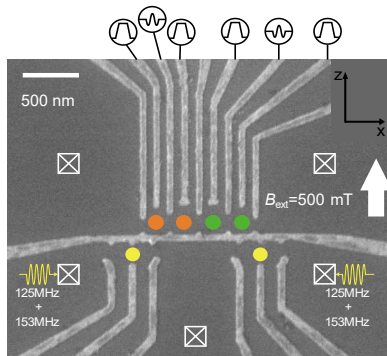
$$P(\Delta B_z | m_N, m_{N-1}, \dots, m_1) = P_0(\Delta B_z) \prod_{k=1}^N \frac{1}{2} [1 + r_k (\alpha + \beta \cos(2\pi \Delta B_z t_k))]$$



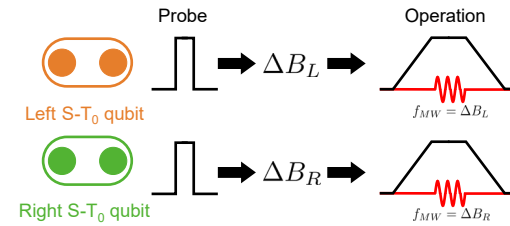
Real-time Qubit frequency tracking



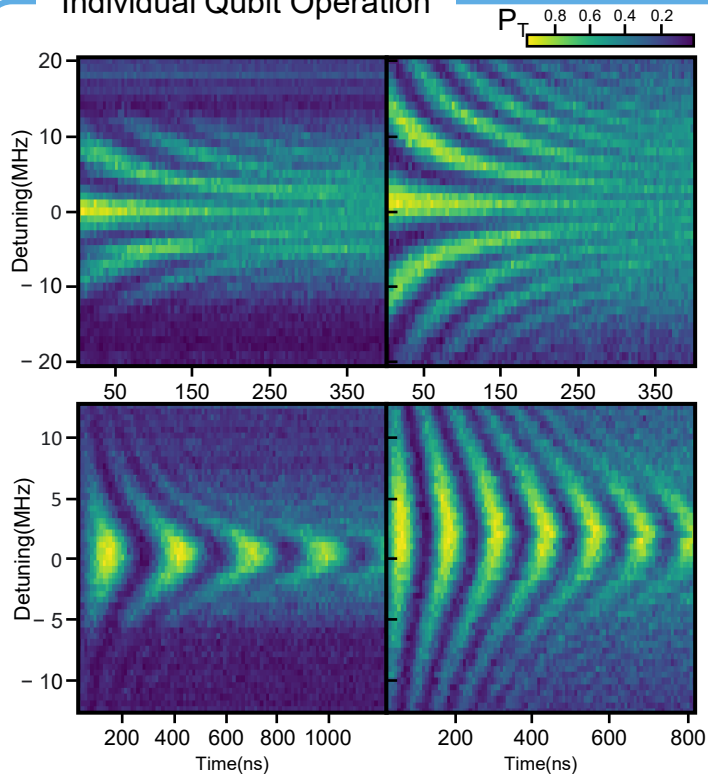
Two ST_0 qubits: Simultaneous Hamiltonian Parameter Estimation



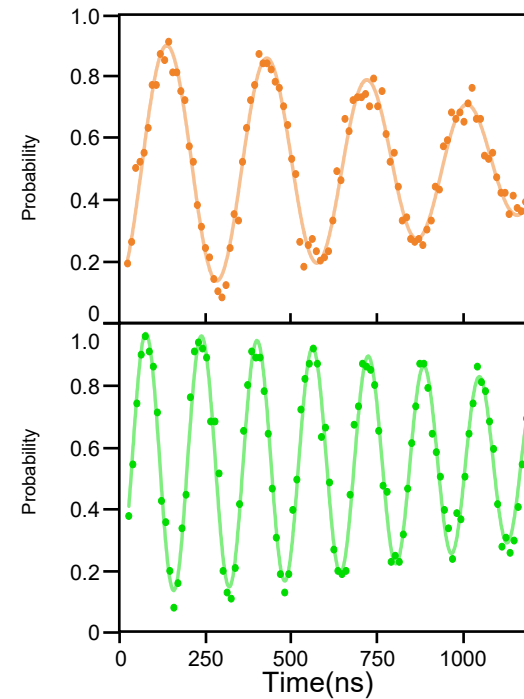
Manuscript in preparation



Individual Qubit Operation



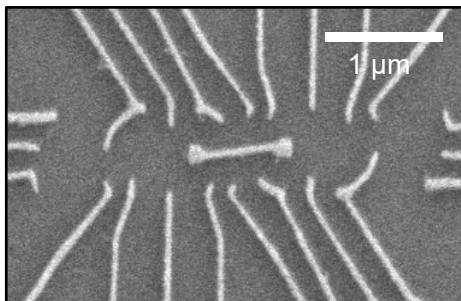
Simultaneous Qubit Driving



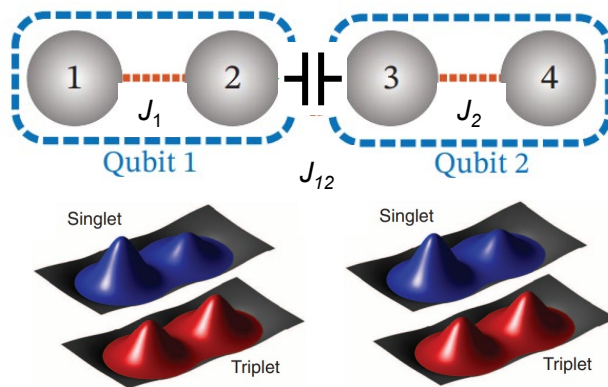
Two qubit interaction

Two qubit gate in two STQs

1. Dipolar interaction - Capacitive : possible but often slow



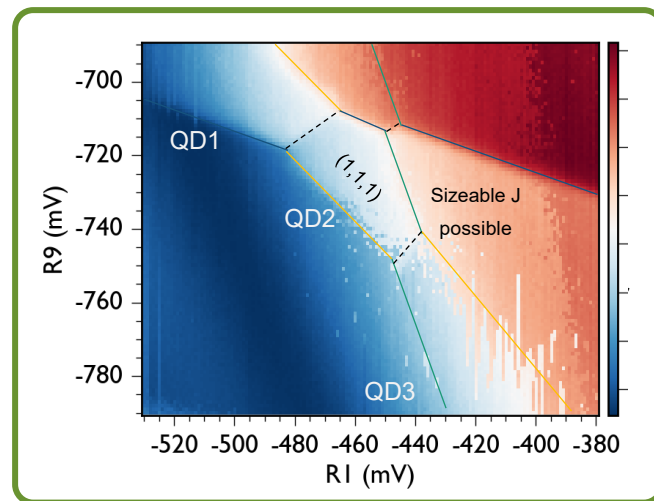
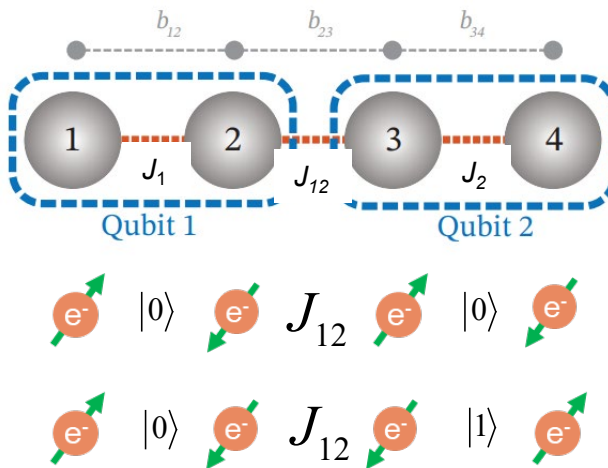
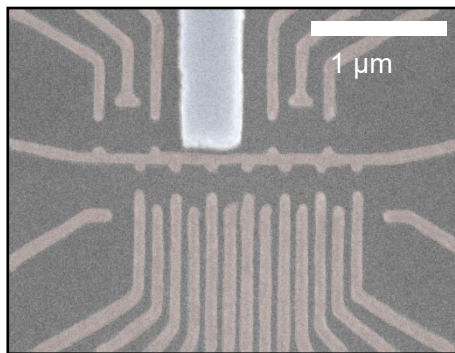
Harvard, *npj. Quant. Inf.* (2017)



Interaction assumed to $\propto A(r)J_{12}J_{34}$ be small

Previously ~ 3 MHz 2Q coupling demonstrated with spin-echo

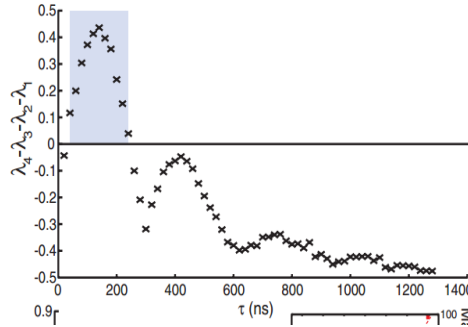
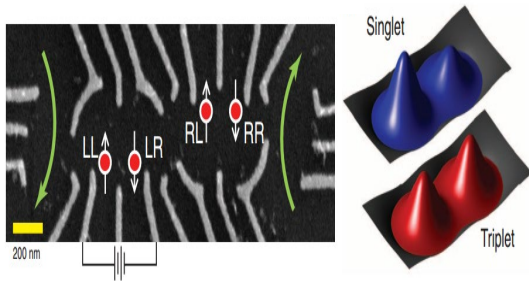
2. Inter Q exchange coupling : intrinsically fast, but leakage



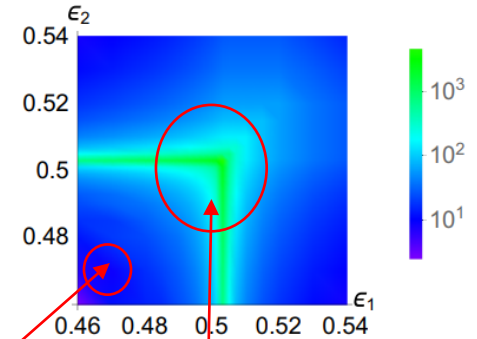
3

Recent contributions by SNU group

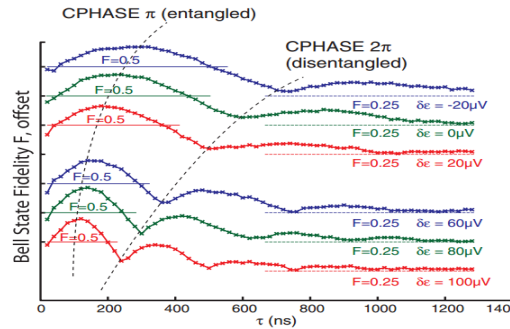
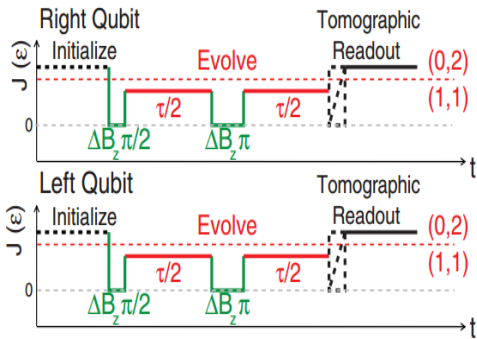
Previous entanglement demonstration



Theory of J_{12}/J_1J_2



VS.



Unexplored area

M. D. Shulman, et al., *Science* **336** 202 (2012)
 D. Buterakos, S. Das Sarma, *Physical Review B* **100**, 075411 (2019)

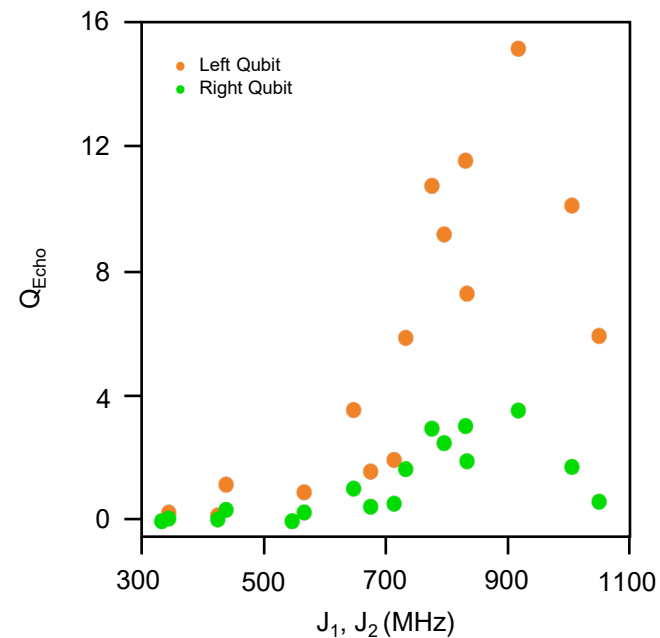
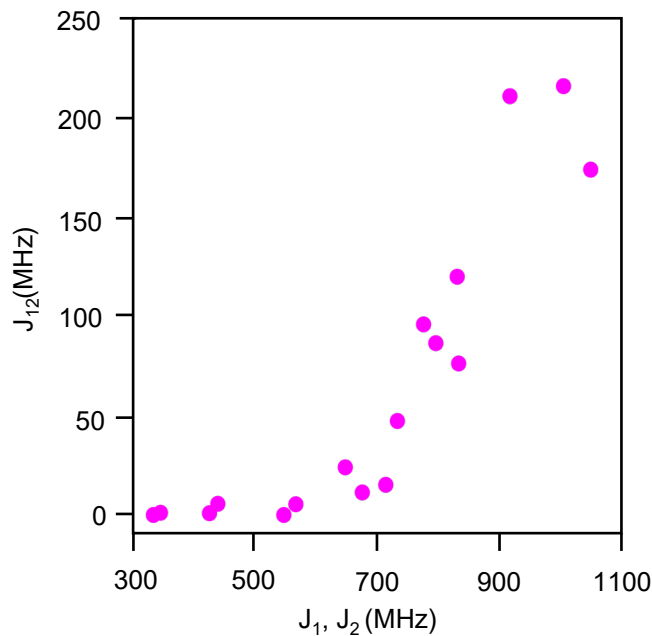
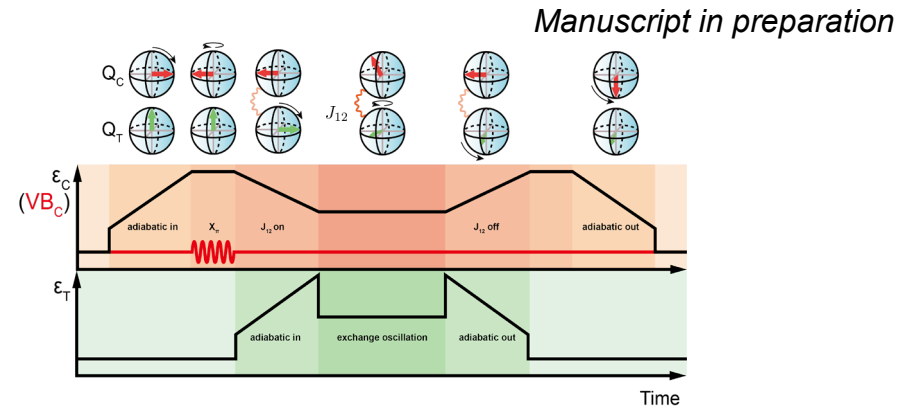
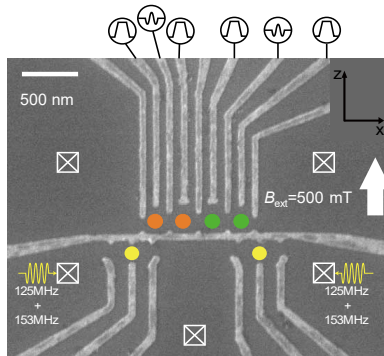
Previous : only at weak dipole-coupling regime

$J_{12} \sim 3 \text{ MHz} @ J_1, J_2 = 300 \text{ MHz} (J_{12} \sim J_1J_2, \text{ bilinear}), \text{ CZ gate fidelity} \sim 70 \%$

3

Recent contributions by SNU group

Strong capacitive coupling regime

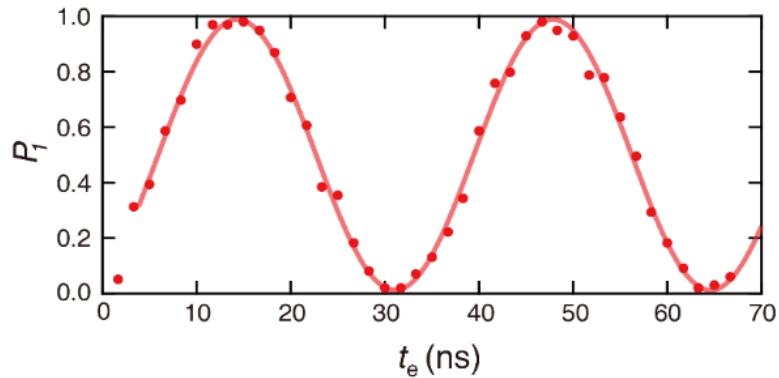


$J_{12} \sim 220$ MHz ($> 20\%$ of J_1 , beyond bilinear regime, CZ gate fidelity $> 90\%$)

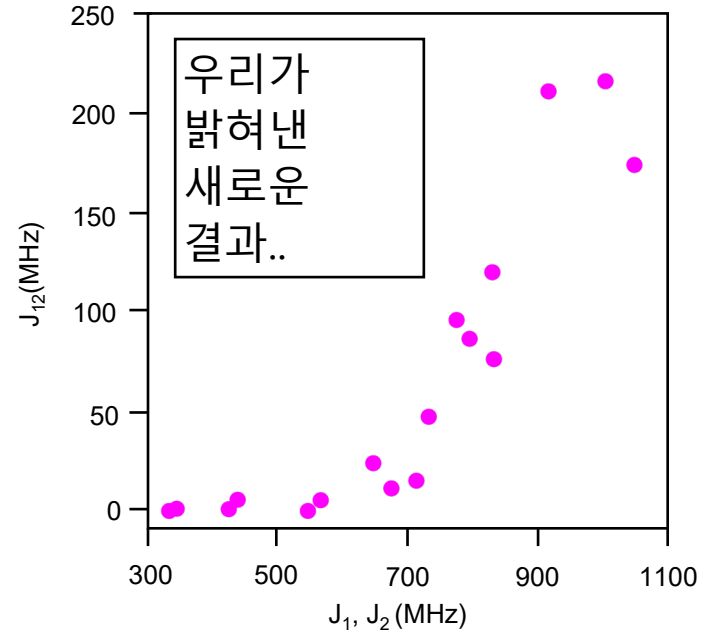
Summary of Lecture 1

Single spin qubit, Singlet-Triplet qubit

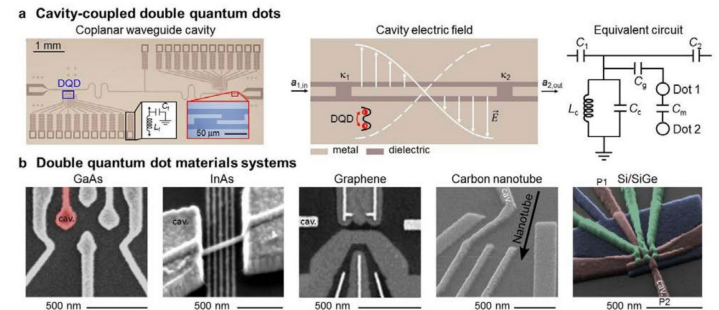
반도체 큐비트의 quality 도 이제는 다른 플랫폼에 못지 않게...

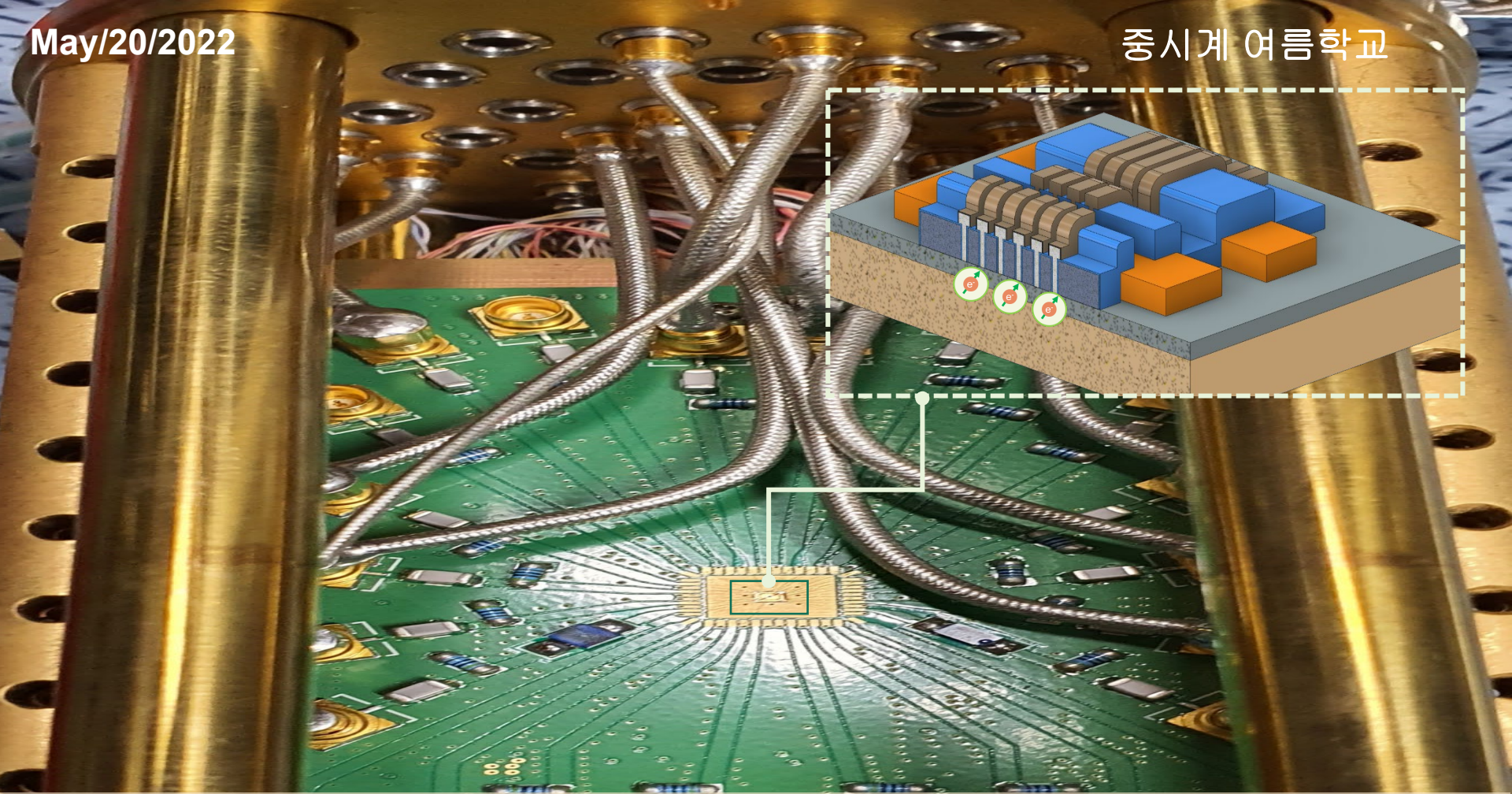


Capacitive coupling can be strong.



- 다음시간: 1. 구체적으로 3,4,6 큐비트 등은 어떻게 제어하나요? Ex. 아까 그림 보니 센서는 2개까지 밖에 없던데...
2. 멀리 떨어진 큐비트들은 어떻게 연결하나요?
3. Scaling 하는데 이슈는 ?





Quantum dot spin qubits II: multi-qubits and shuttling

(Slide courtesy : 윤종인, 장원진)

Dohun Kim

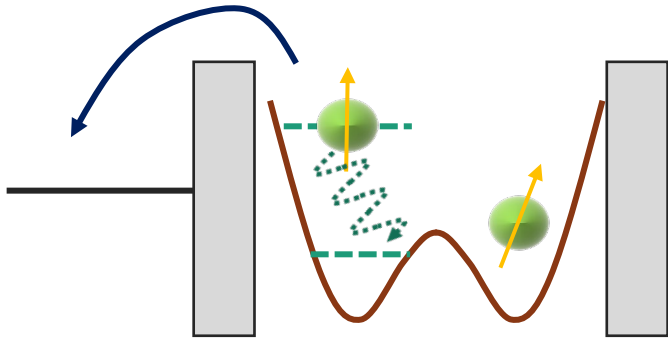
Outline

- **Background** *Recall EST & PSB, non-demolition measurements*
- **Approach** *Multi qubit initialization, manipulation, measurement*
- **Some recent achievements** *Shuttling-based long-distance connection, High-temperature operations*

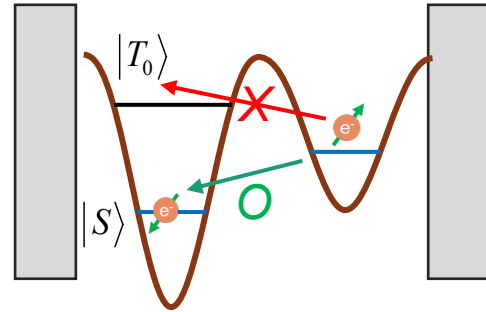
1

Background

Recall RSB & EST



Measure one electron charge change



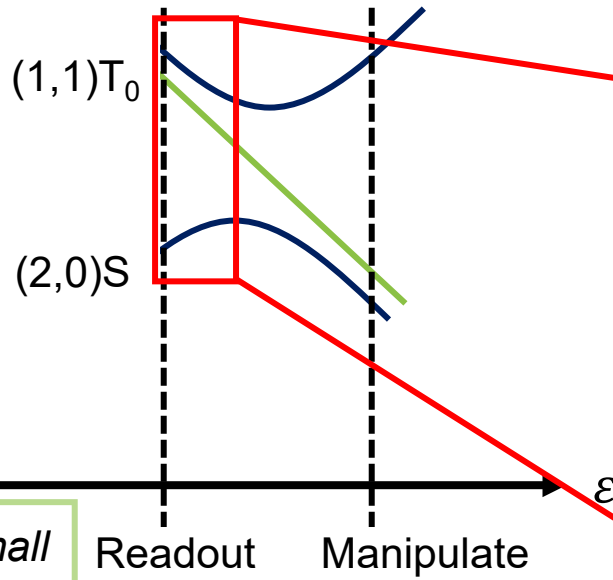
Measure relative position

Typical signal : 그리기

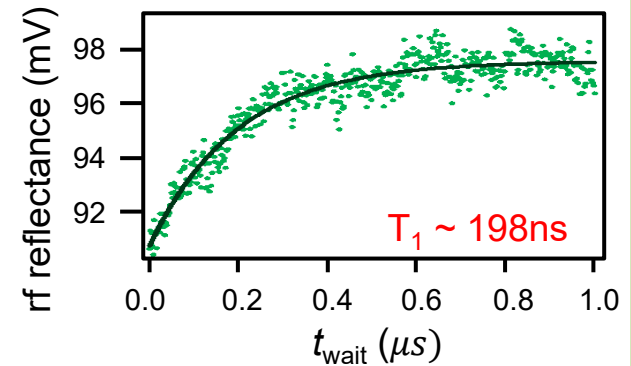
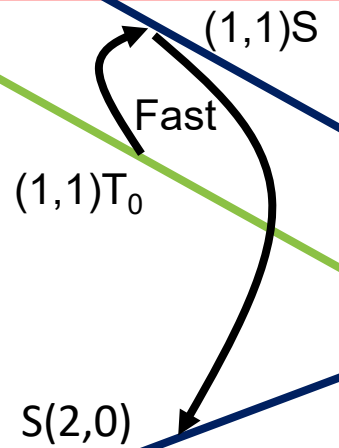
1

Background

Problem of conventional Read-out of STQ

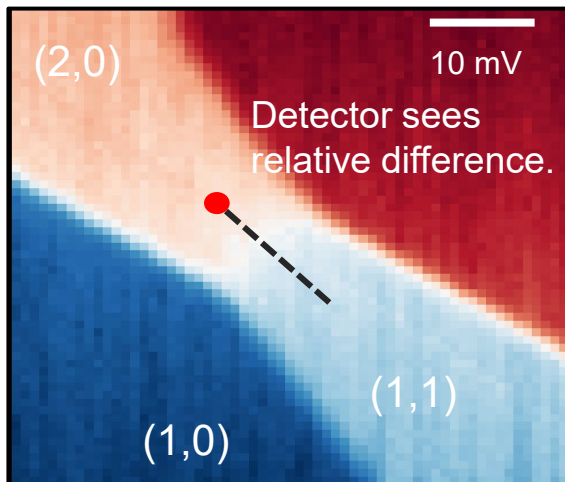


P2. fast relaxation

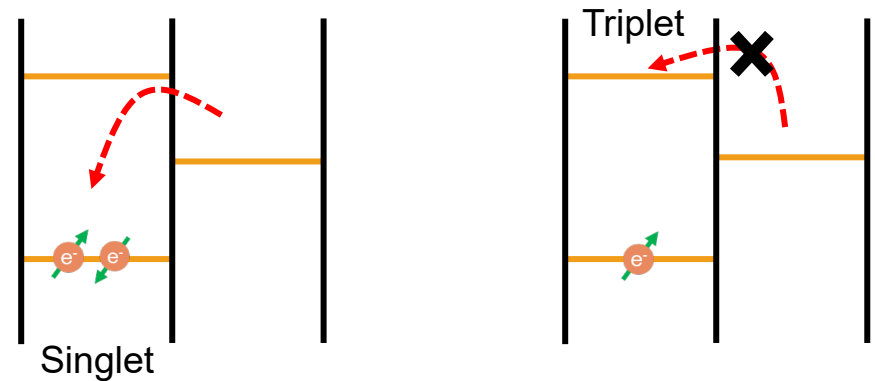


At PSB detuning, ΔB mixes S & T_0 :
 (1,1) T_0 relax to S(2,0) – fast at
 large ΔB

P1. small
Signal



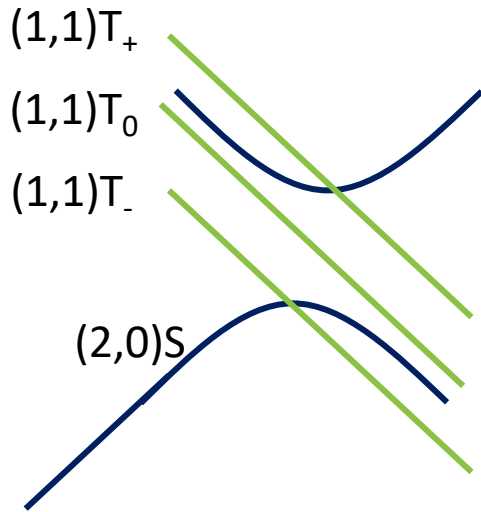
At the Readout point : *spin blockade*



1

Background

Really a problem ? Parity readout



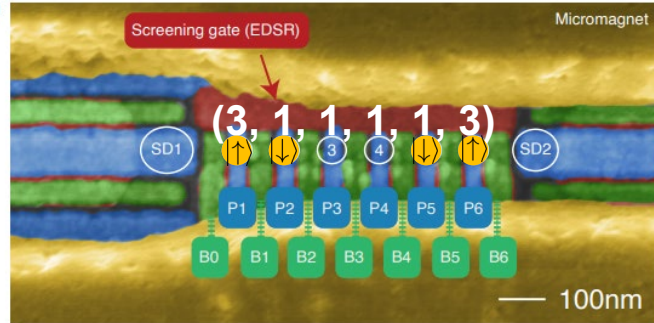
Typical signal : Readout 방법 그리기

2

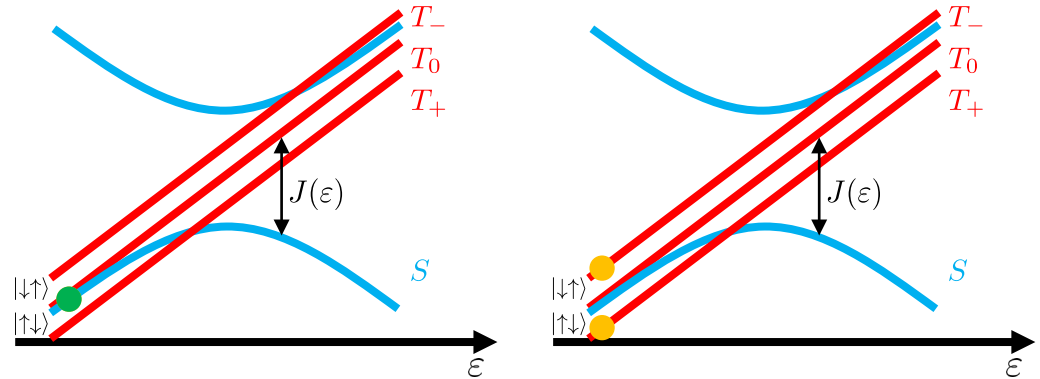
Approach

Six qubit operation : initialization

Initialization of the Spin State

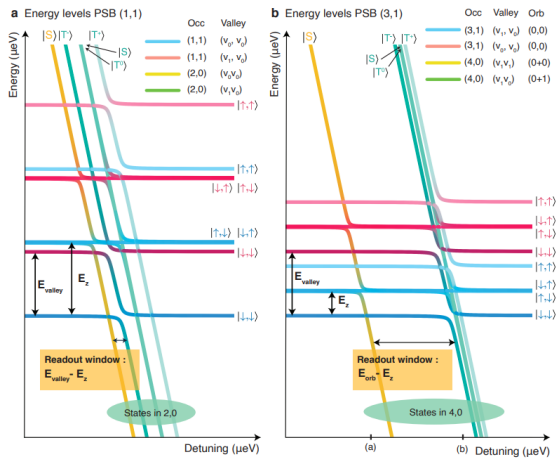


1. Parity based initialization of qubit 1-2 (5-6)

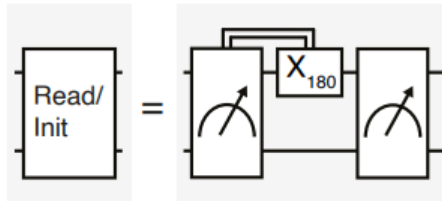


Odd Parity: T_0 relaxes well before the $10\mu\text{s}$ readout window at PSB regime

➔ Readout of state parity using PSB



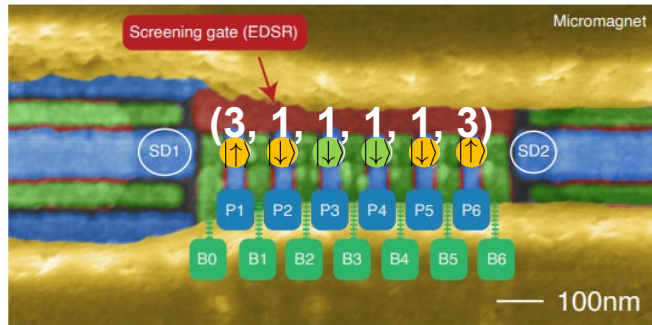
Real-time feedback initialization



1. First parity measurement
2. Burst a π -pulse on qubit 1 when even parity
3. Second Parity Measurement
4. $|\uparrow\downarrow\rangle$ state is prepared

Six qubit operation : initialization

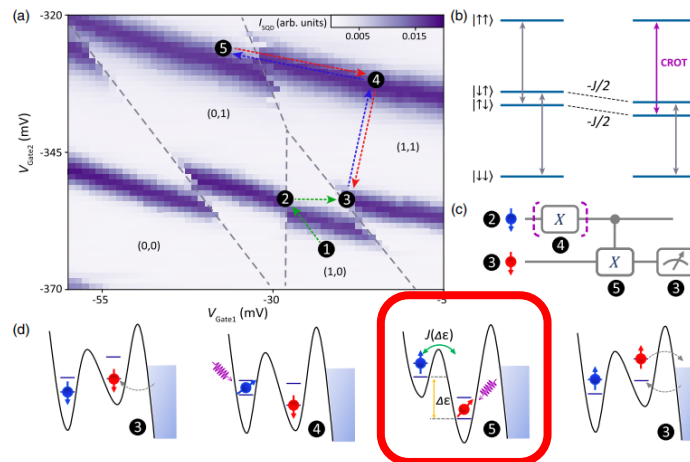
Initialization of the Spin State



Physical Review A 32.4 (1985): 2287.

1. The uncertainty introduced by the measurement should not affect the motion of the observable
 $[A_S, H_S] \approx [\sigma_z, \sigma_z] = 0$
2. The interaction with the ancilla should not affect the motion of the observable
 $[A_S, H_{int}] \approx [\sigma_z, (\sigma_z \otimes \sigma_z - 1)] = 0$

2 Quantum-Non-Demolition readout of inner spin qubits



Physical Review X 10.2 (2020): 021006.

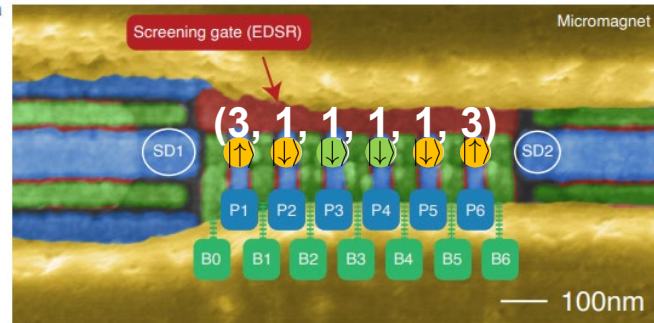
용어의 모호함 ?

2

Approach

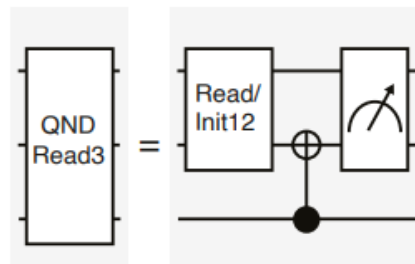
Six qubit operation : initialization

Initialization of the Spin State



2. Quantum-Non-Demolition readout of inner spin qubits

1. Initialize the ancilla qubit to the spin-down state
2. Turn on J_{int} by pulsing a virtual barrier gate and perform a CNOT gate
3. Pulse to (4,0) and perform the single-shot measurement of the ancilla qubit
4. Parity measurement prepares the desired initial states for qubit 1 and 2
5. If qubit 3 is spin-up, flip it using the π -pulsing microwave



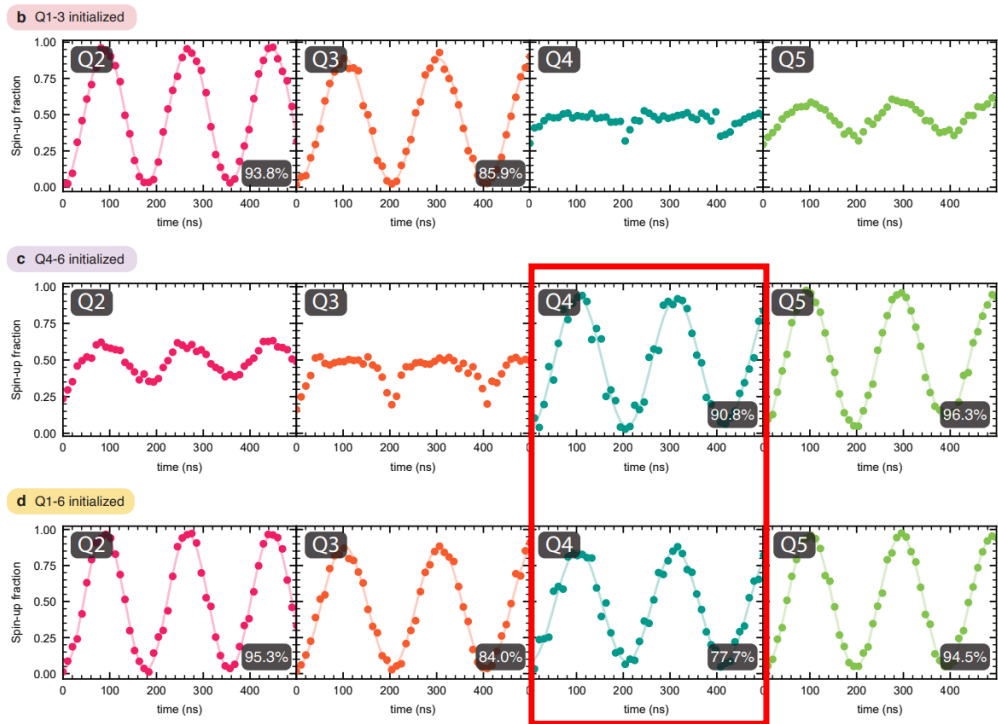
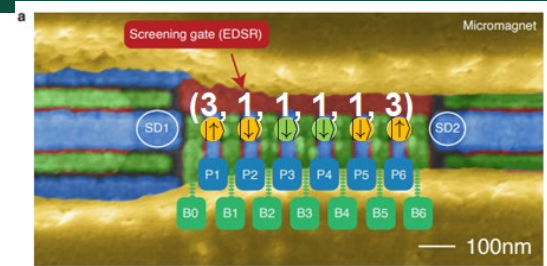
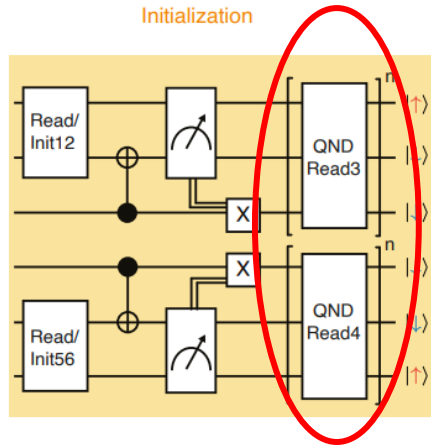
2

Approach

Six qubit operation : initialization

Initialization of the Spin State

1. Parity based initialization of qubit 1-2 (5-6)
2. Quantum-Non-Demolition readout of inner spin qubits



Initialized two, three, or all six qubits depending on the requirement of the specific quantum circuit

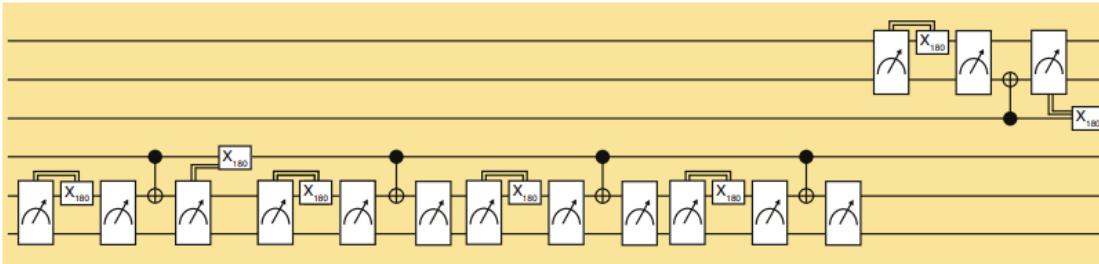
Run QND measurement three times and **post-select** runs with three identical QND readout outcome (except for GHZ state preparation and tomography, where the **majority vote** is used)

2

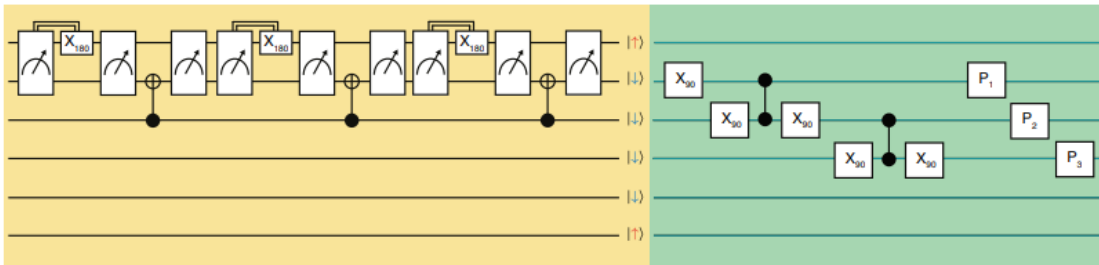
Approach

Six qubit operation : readout

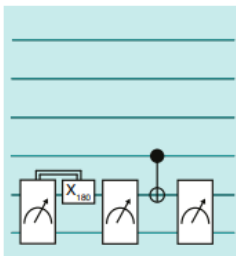
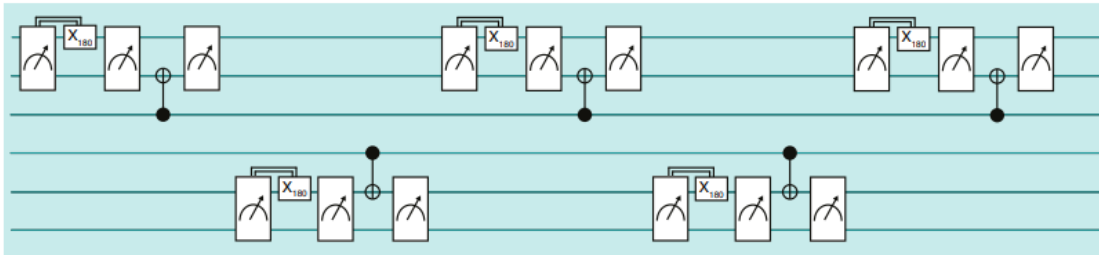
Initialization



Q234 GHZ-state preparation



Readout

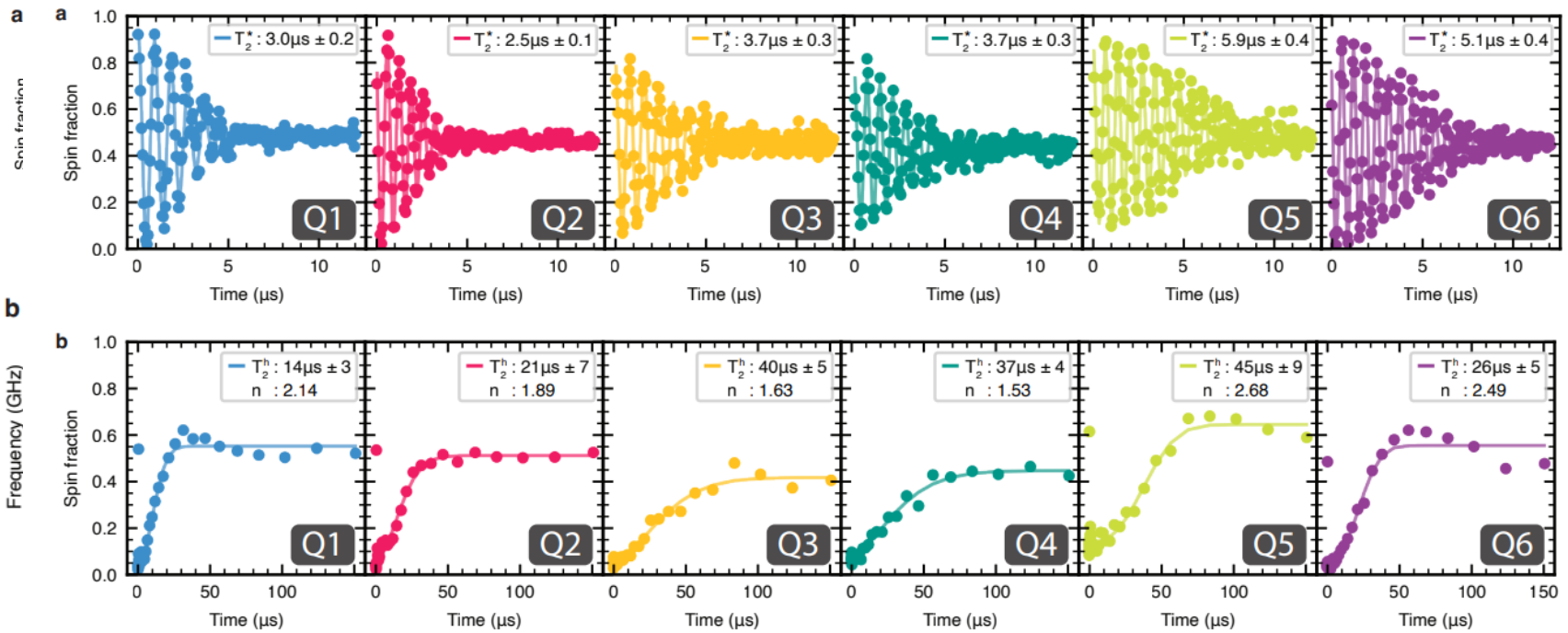


2

Approach

Six qubit operation : operation

1. EDSR Based Rabi Oscillation

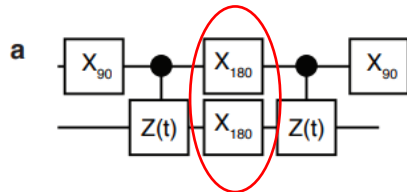


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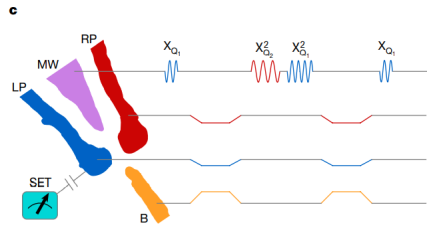
Approach

Six qubit operation : operation

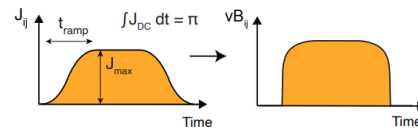
2. Two Qubit Gate (C-Phase) by Virtual Barrier Gate Pulse



Apply π to both Q1 and Q2, which offsets the oscillation by J_s and J_A yet preserves the oscillation by J_{int}



Nature 601.7893 (2022): 343-347.



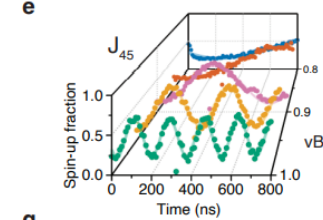
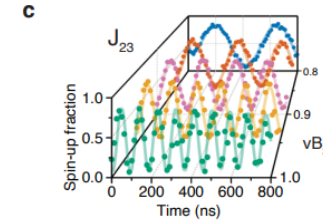
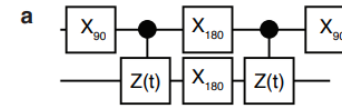
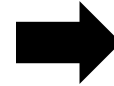
$$W(t, r) = \begin{cases} \frac{1}{2} \left[1 - \cos\left(\frac{2\pi t}{\tau_p}\right) \right] & 0 \leq t \leq \frac{\tau_p}{2} \\ 1 & \frac{\tau_p}{2} < t < t_p - \frac{\tau_p}{2} \\ \frac{1}{2} \left[1 - \cos\left(\frac{2\pi(t_p - t)}{\tau_p}\right) \right] & t_p - \frac{\tau_p}{2} \leq t \leq t_p \end{cases}$$

Nature 601.7893 (2022): 343-347.

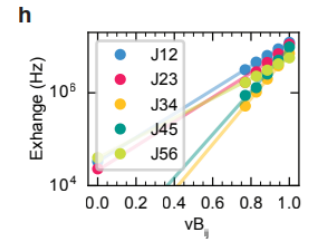
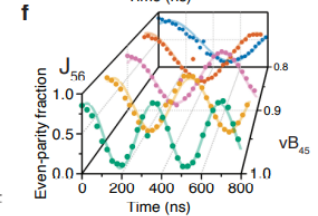
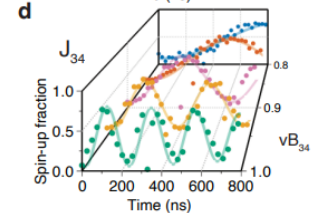
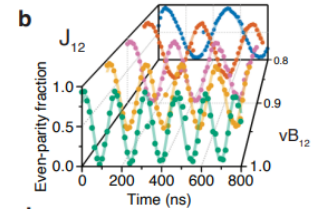
Tukey window with a ramp time of 3

$$t_{ramp} = \frac{3}{\sqrt{\delta B^2 + J_{max}^2}}$$

Physical Review A 90.2 (2014): 022307.



(MHz)	J_{12}	J_{23}	J_{34}	J_{45}	J_{56}
J_{12} on	12.1	0.023	0.018	≤ 0.03	0.040
J_{23} on	≤ 0.05	11.1	≤ 0.03	≤ 0.03	0.040
J_{34} on	0.050	≤ 0.03	6.6	≤ 0.07	0.042
J_{45} on	0.038	≤ 0.03	0.031	9.8	0.250
J_{56} on	0.033	≤ 0.03	≤ 0.02	≤ 0.03	5.4
J_i off	0.039	0.015	≤ 0.03	0.020	0.028



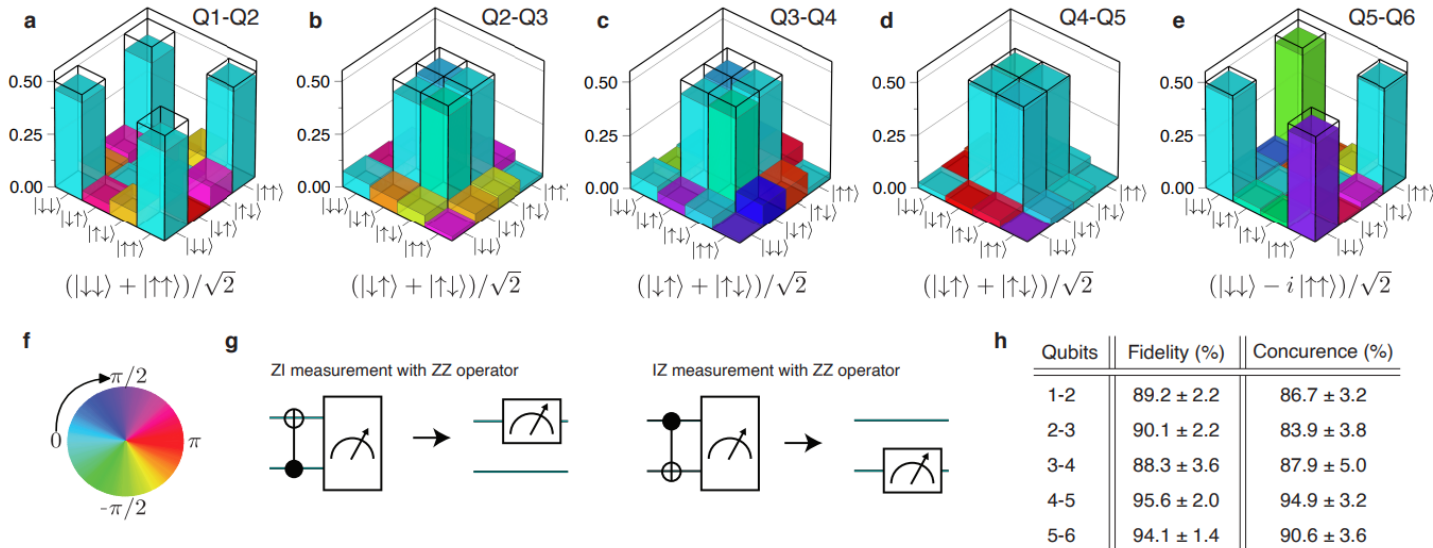
i CPhase CPT i

2

Approach

Six qubit operation : operation

3. Bell State Tomography/GHZ State Tomography

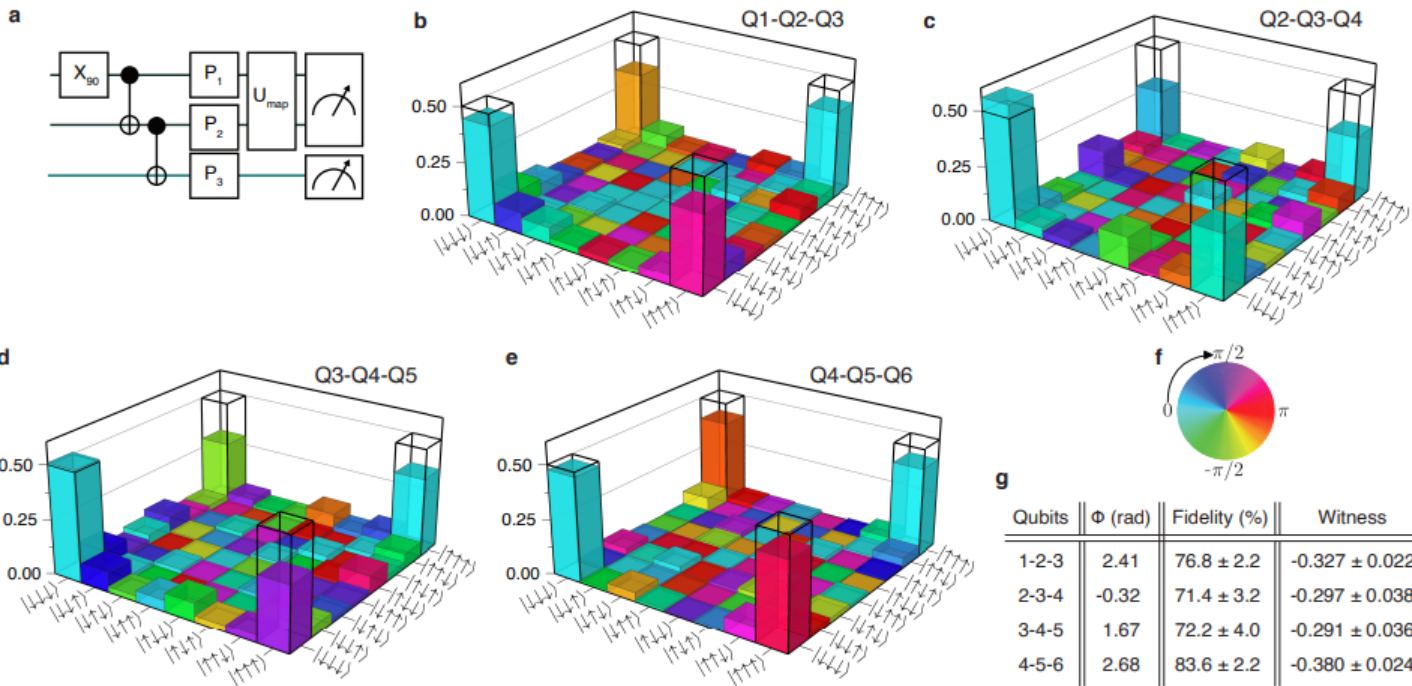


2

Approach

Six qubit operation : operation

4. GHZ State Tomography

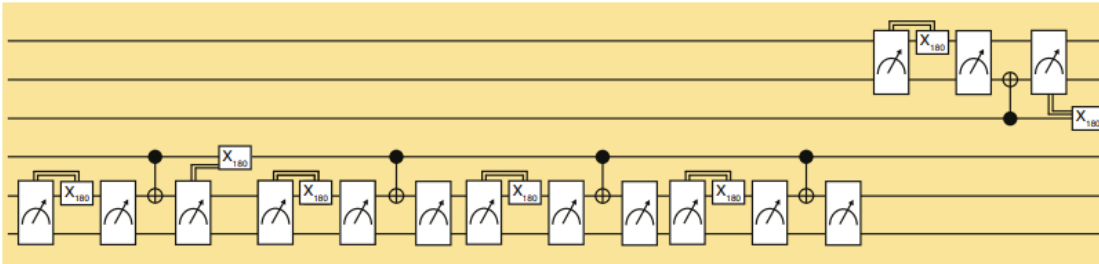


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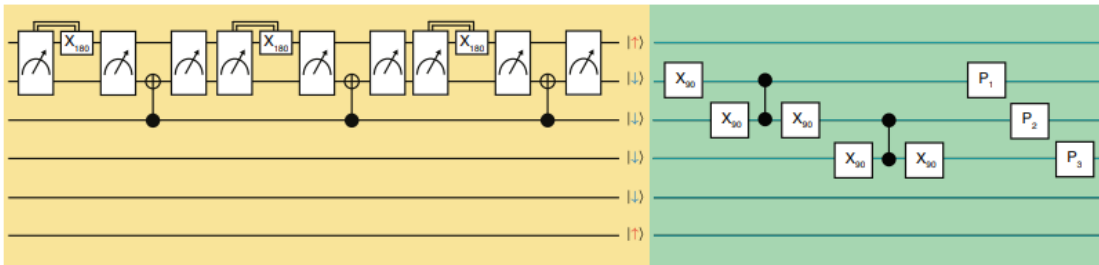
Approach

Six qubit operation : 전체회로 recall

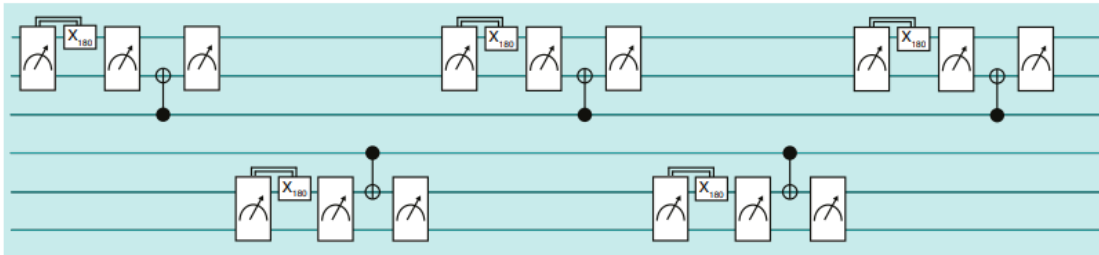
Initialization



Q234 GHZ-state preparation



Readout

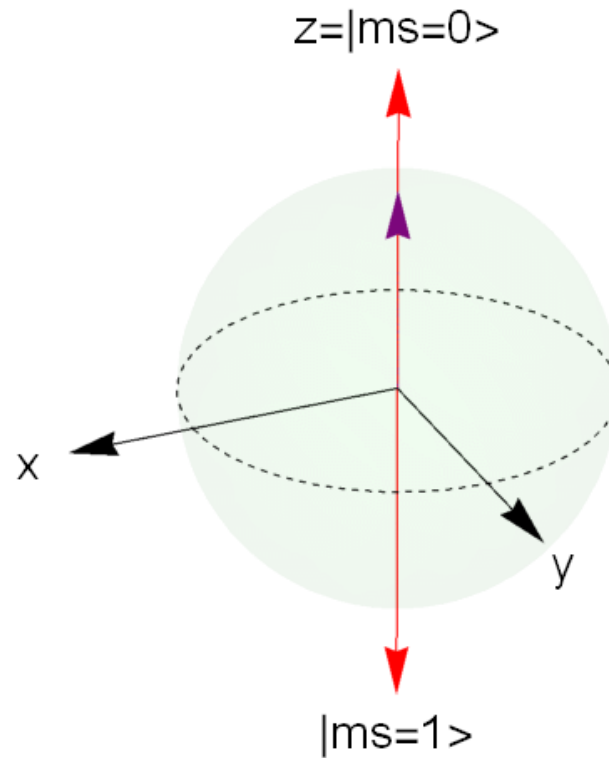


2

Approach

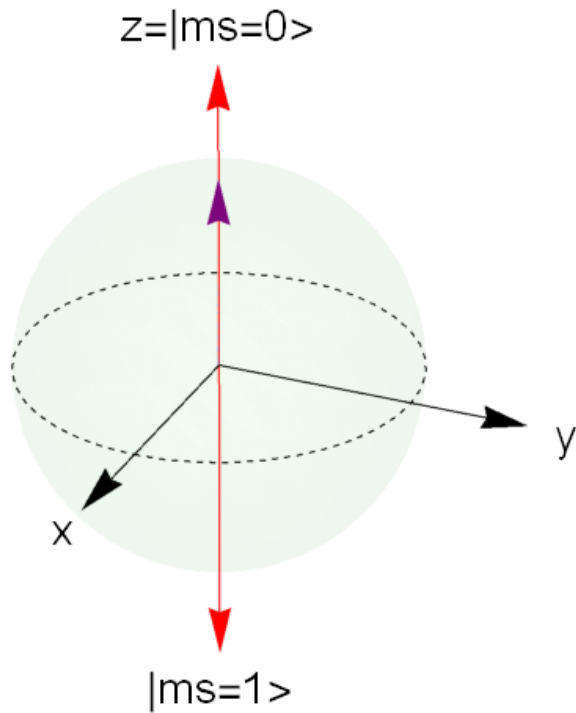
One more technique : Spin-echo

Ramsey sequence

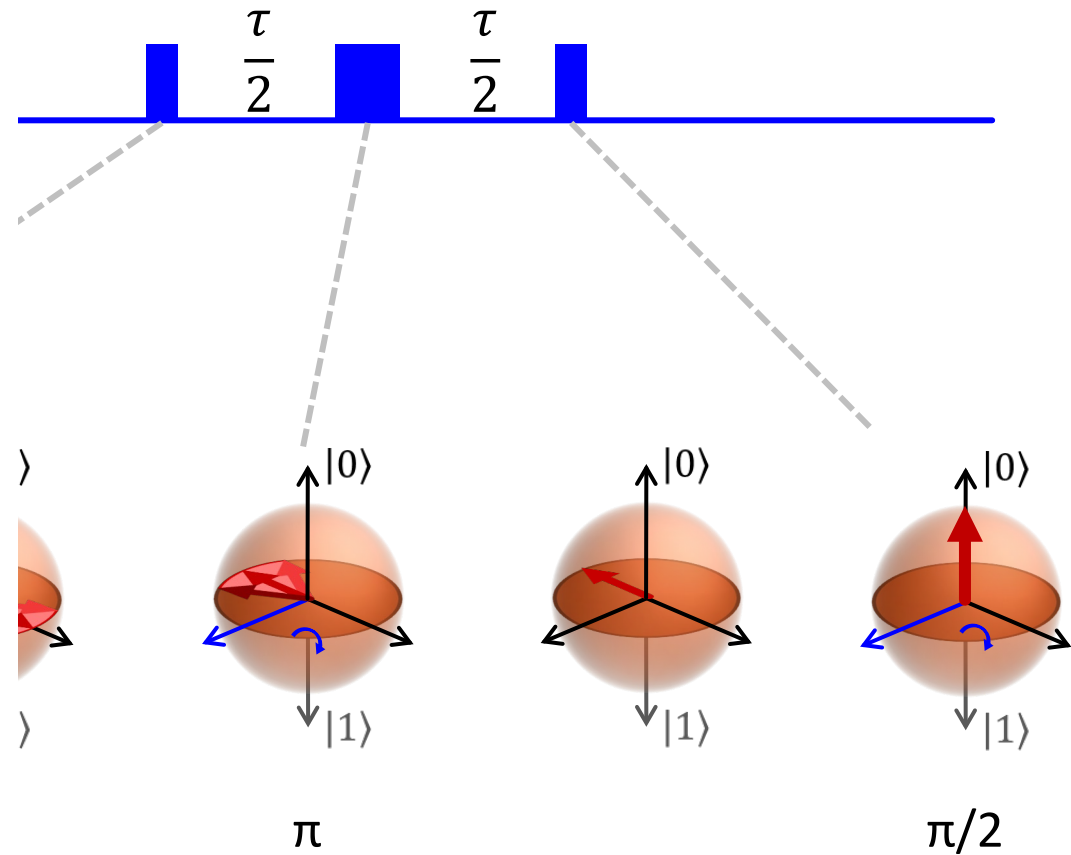


One more technique : Spin-echo

Spin echo



o pulse sequence



이를 π 펄스를 이용하여 상쇄시켜줌

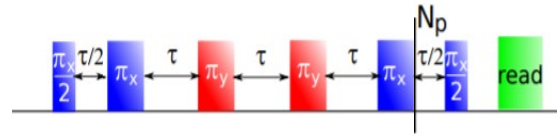
2

Approach

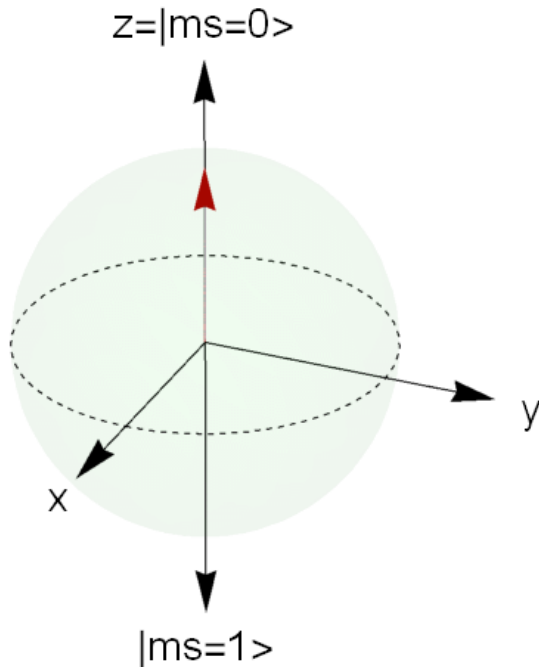
One more technique : Spin-echo

Ex: CPMG (Carr-Purcell-Mieboom-Gill) pulse

Cpmg sequence



CPMG XY4



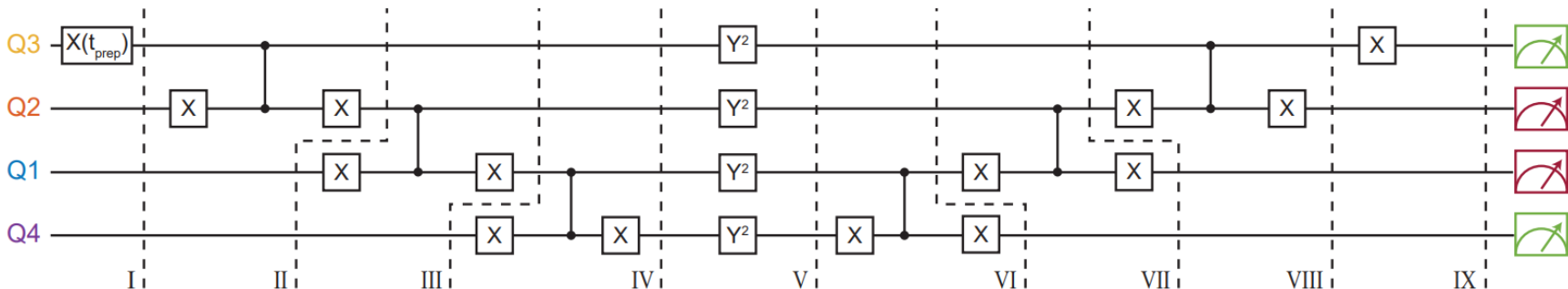
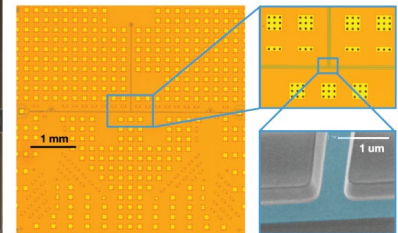
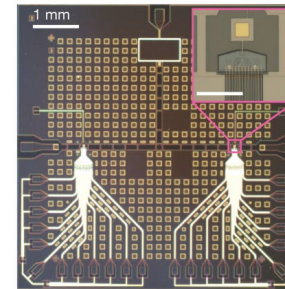
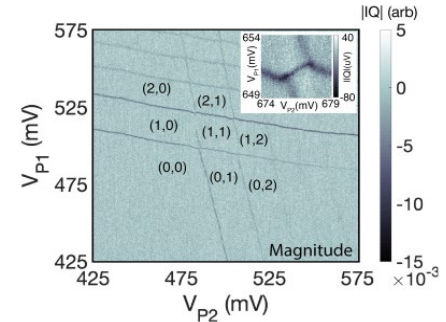
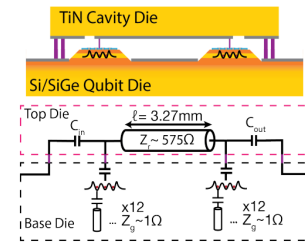
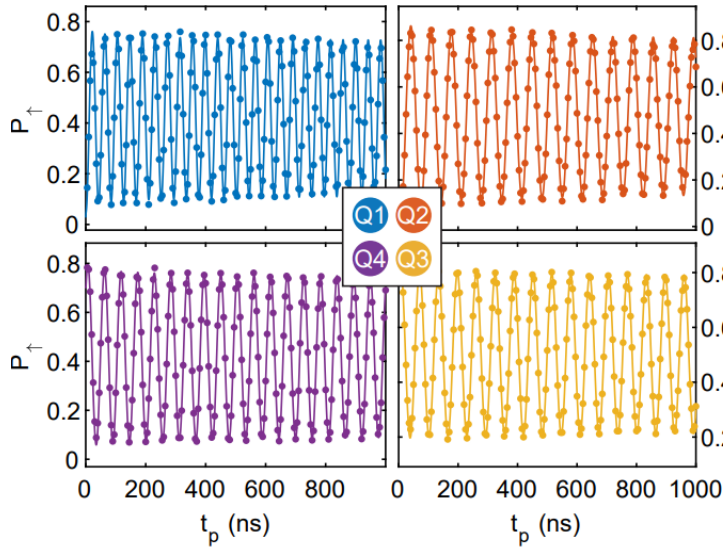
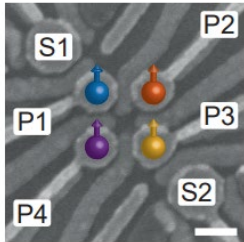
Dynamic decoupling 의 핵심 :
dynamic decoupling pulse
sequence 는 frequency filter,
이를 이용하면 environment 의
noise spectrum 측정 가능 - 좀
더 advanced course 에서...

2

State of the art in single-spin qubits

Example: Si, GaAs, Ge.. Boosting up results

Most recent developments : Germanium 4 qubit processing & 3D integration

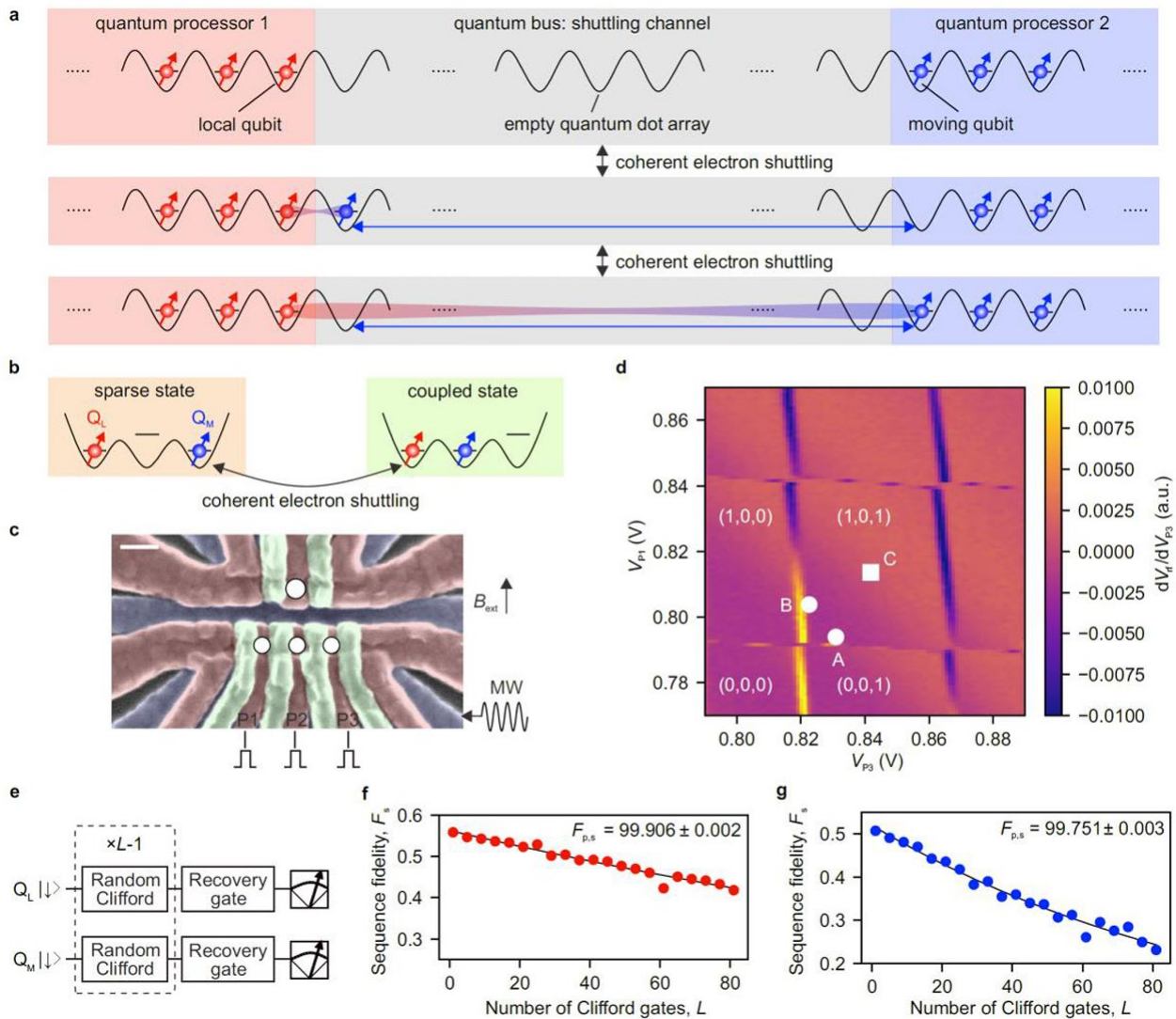


quTech, Delft Sep. 2020
M.Eriksson group UW Nov. 2020

3

Recent developments

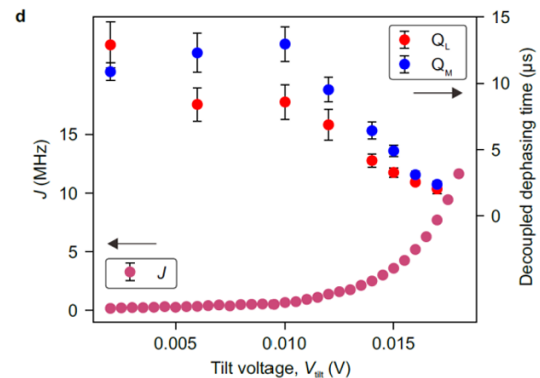
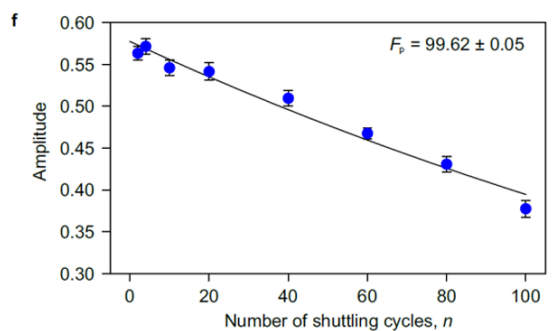
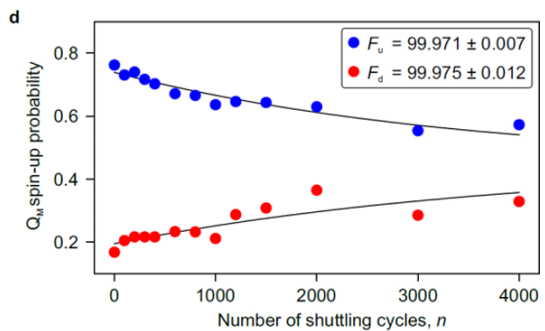
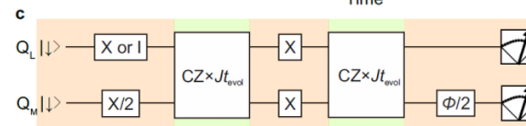
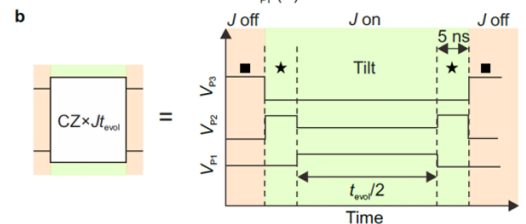
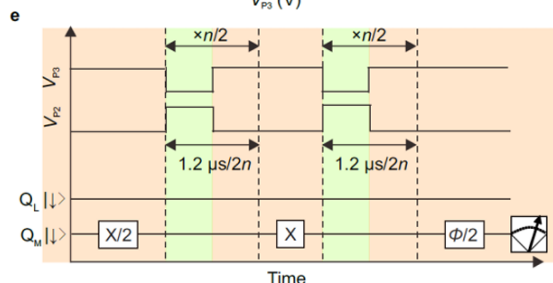
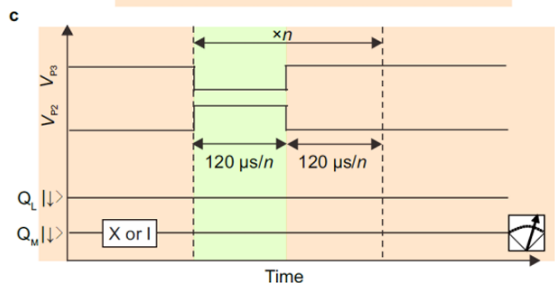
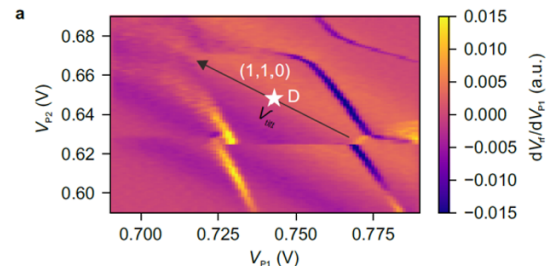
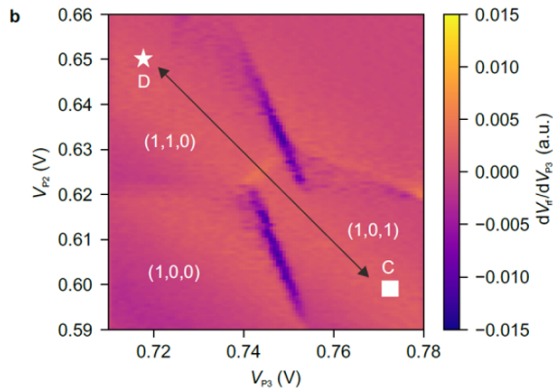
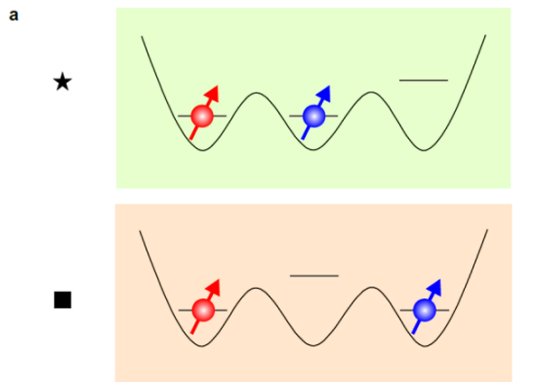
Coherent Shuttling



3

Recent developments

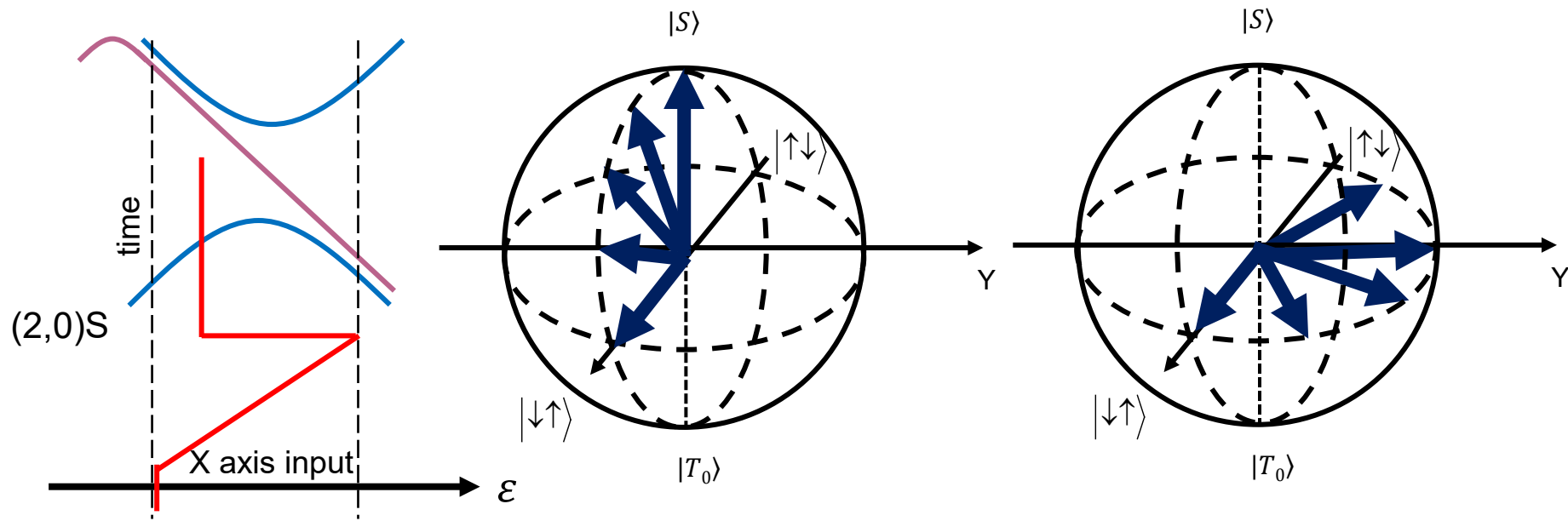
Coherent Shuttling



3

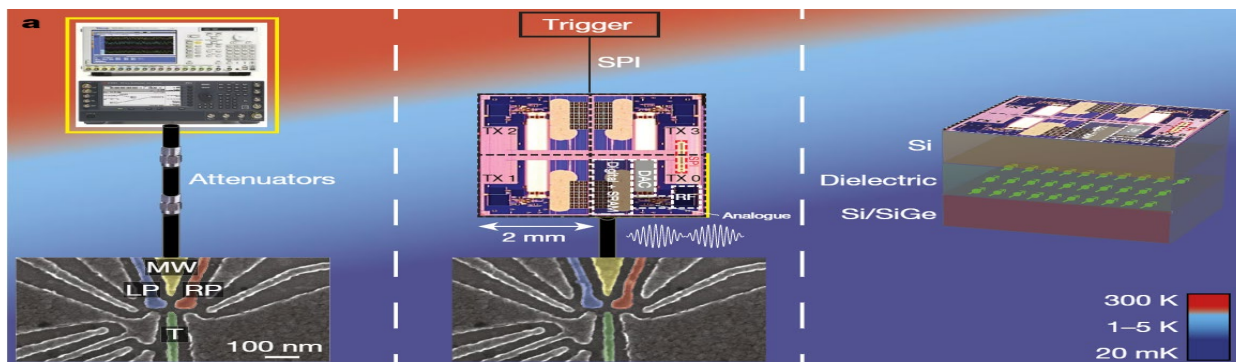
Recent developments

Other than shuttling : spin exchange without moving

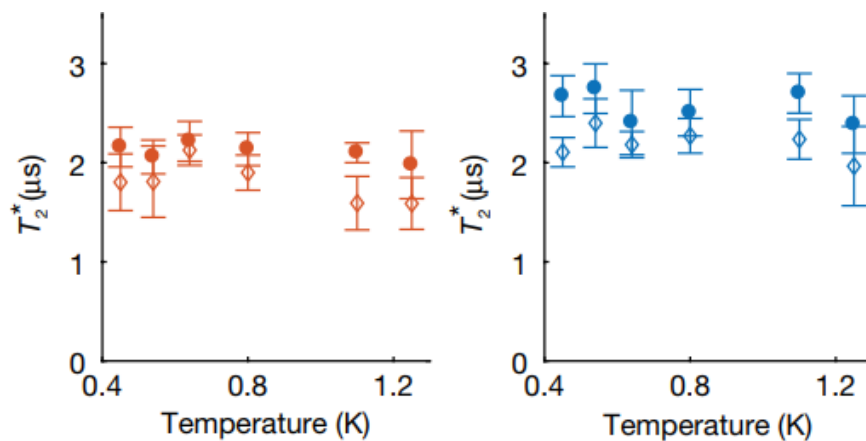
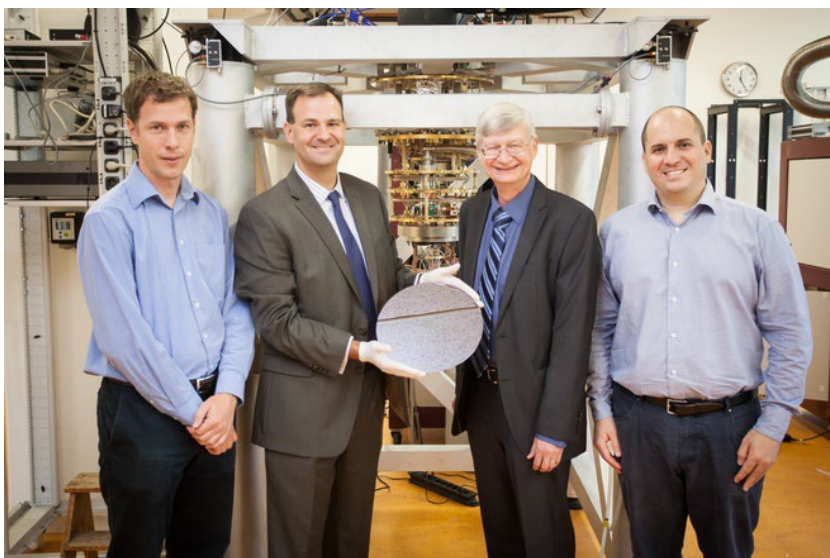


Article

Universal quantum logic in hot silicon qubits

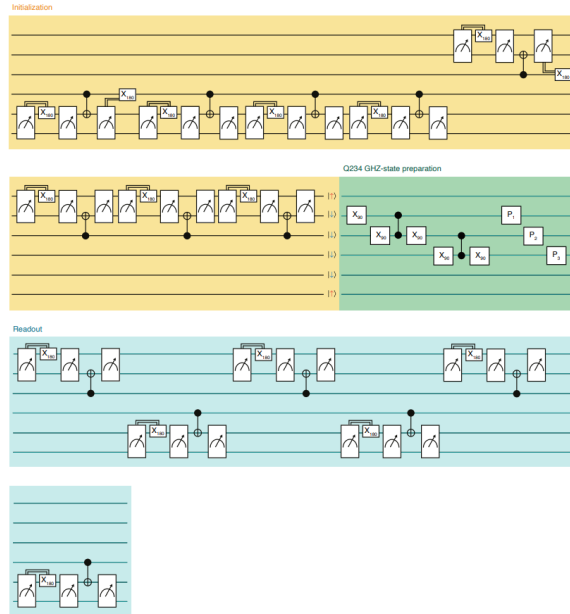
L. Petit et al, *Nature* **580**, 355 (2020)

QuTech / Intel.

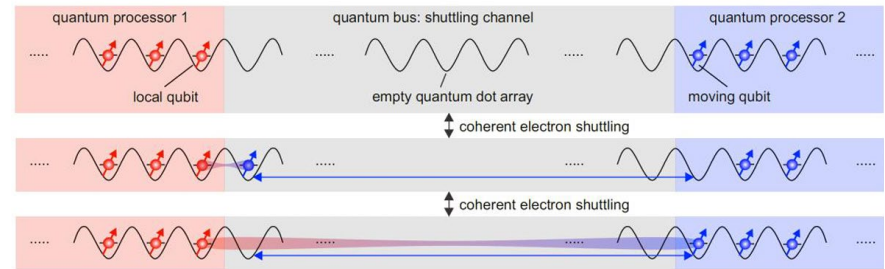


Summary of Lecture 2

Multi qubit operation : 종합선물세트



Toward larger array: shuttling, exchange



결론: 반도체 양자컴퓨팅 – 어렵지만 promising developments